

Grid Slabs.

Panelled Beams.

نسألكم الدعاء

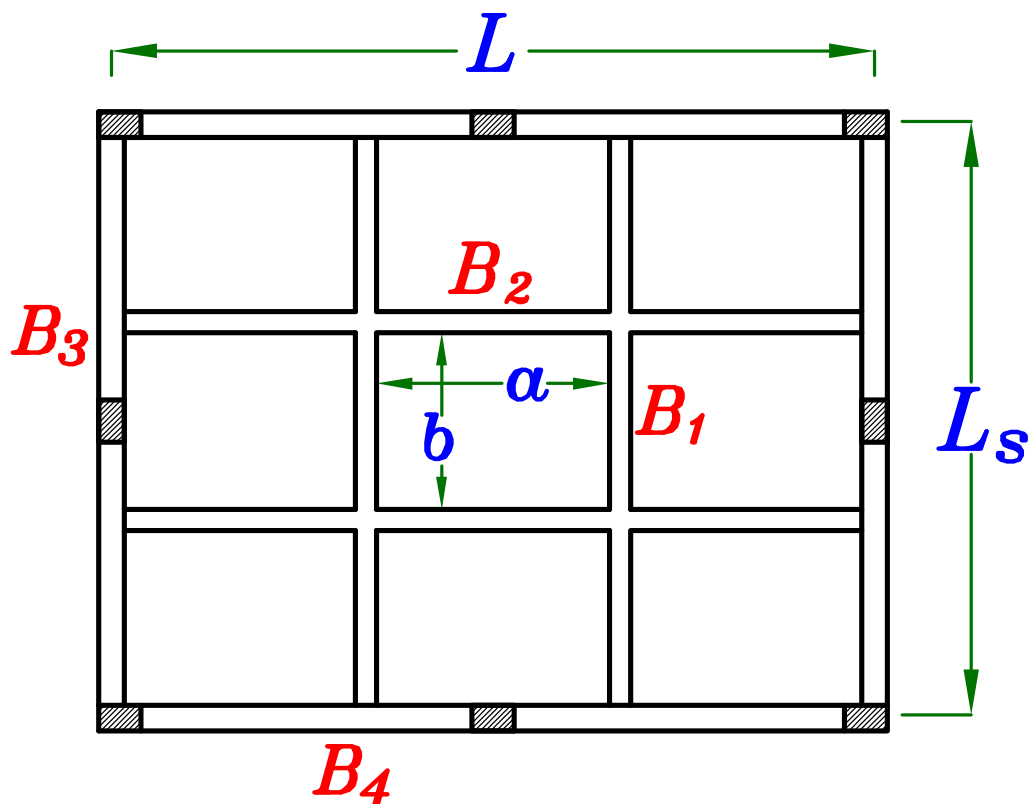
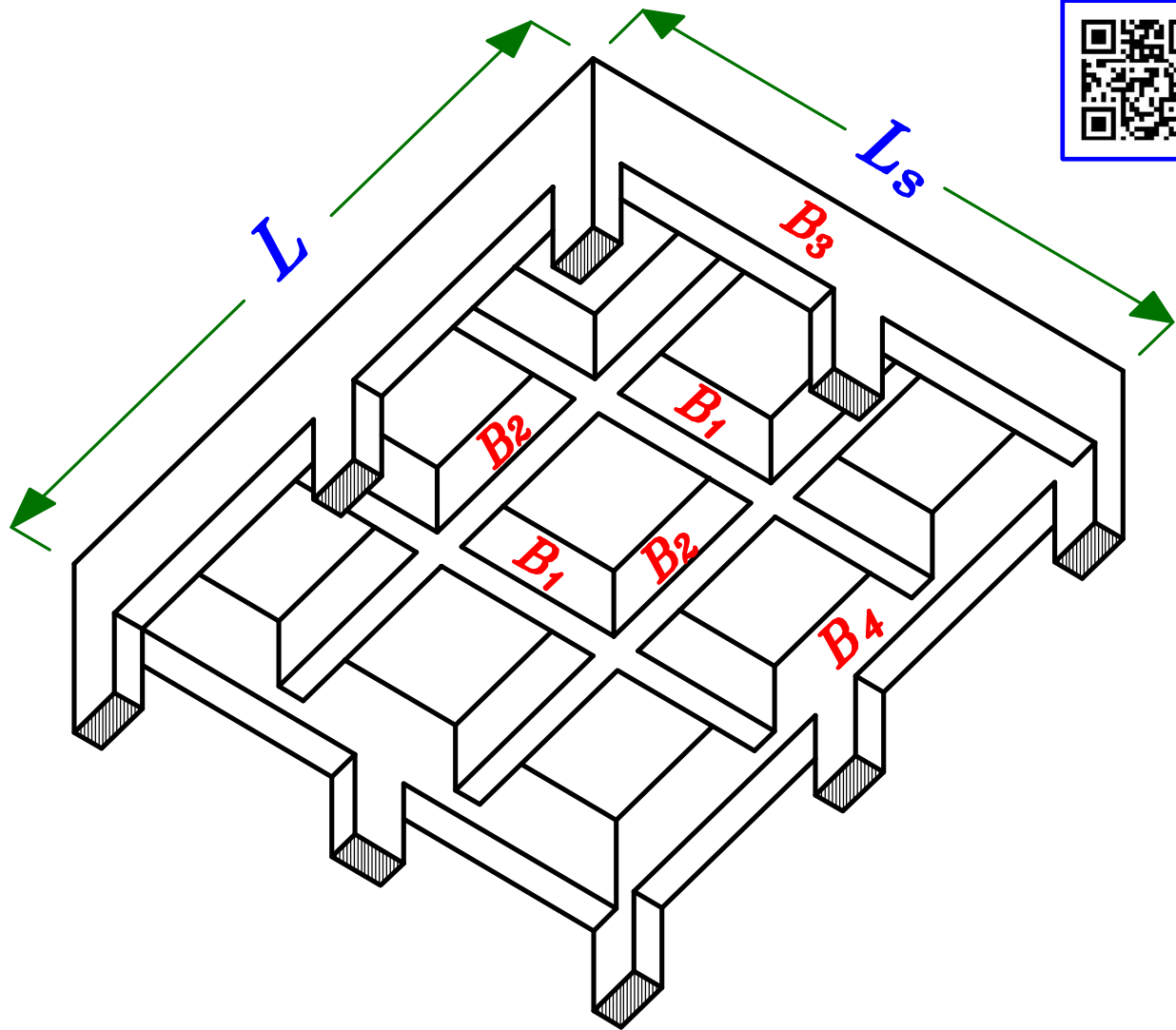
IF you download the Free **APP. RC Structures**  on your smart phone or tablet, you will be able to play illustrative movies For any paragraph that has a QR code icon 

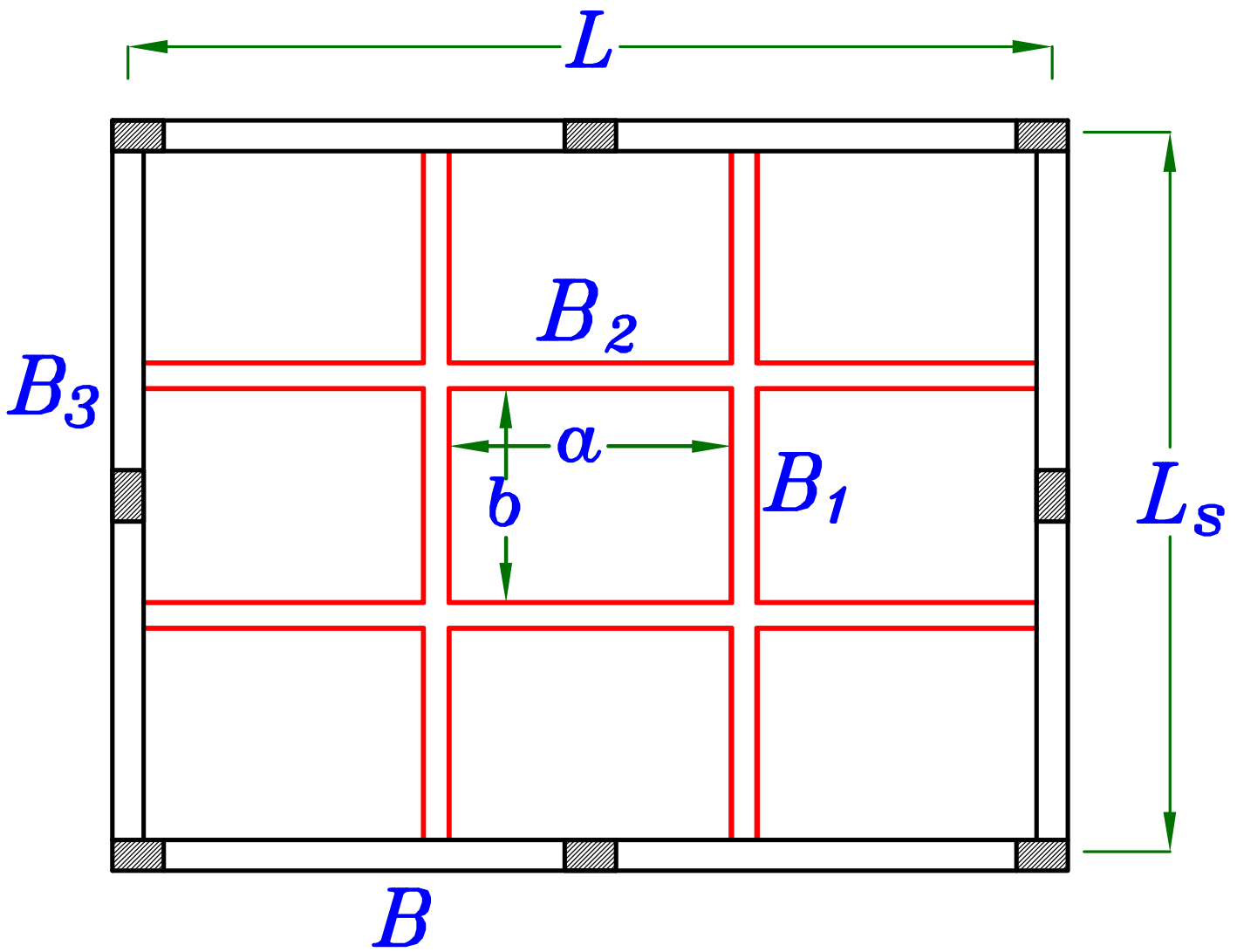
إذا حملت تطبيق **RC Structures**  على تليفونك المحمول او اللوح السطحي ستستطيع أن تشغل أفلام شرح للمقاطع التي تحتوى على رمز 

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Introduction.





— ال **Panelled Beams** هي عبارة عن كمّرات متقاطعه B_1, B_2 مكوّنه شبكه من الكمّرات لتعمل **Grid Action** .

— و عند تقاطع هذه الكمّرات مع بعضها تكوّن بينها بلاطات صغيره $(a * b)$

و هذه البلاطات إما أن تكون **Solid Slab or Hollow Blocks**

— يفضل أن تكون المسافات بين الكمّرات الداخليه $(a \text{ or } b)$ من $(2.0 \text{ m} \rightarrow 5.0 \text{ m})$.

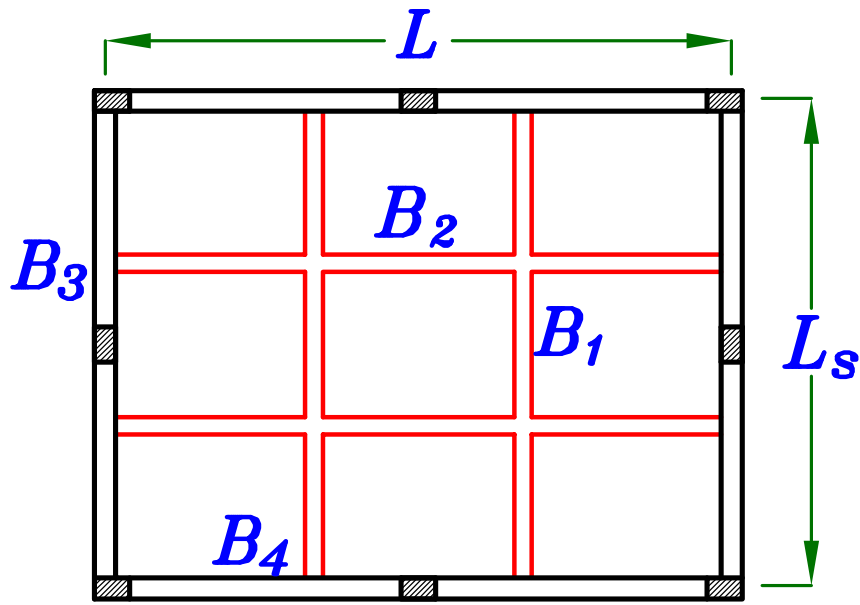
و لا يشترط أن تكون المسافات بين الكمّرات مسافات متساويه .

— تستخدم ال **Panelled Beams** للبلاطات ذات المساحات الكبيره $(80 \text{ m}^2 \rightarrow 150 \text{ m}^2)$

بدون وضع أعمده فى الداخل و اذا زادت المساحه عن ذلك نأخذ تأثير الاعمده

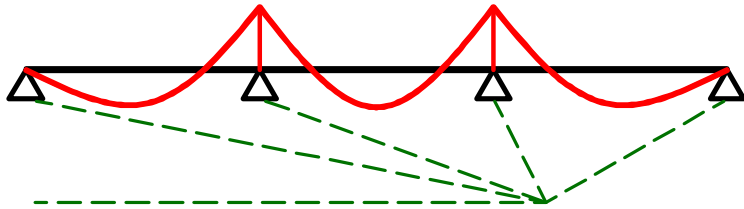
و نعمل **Panelled Frames** و فى هذه الحاله ممكن أن تصل المساحه الى (500 m^2)

— ممكن وضع أعمده خارجيه لتقليل ال **B.M.** على الكمّرات الخارجيه B_3, B_4 .

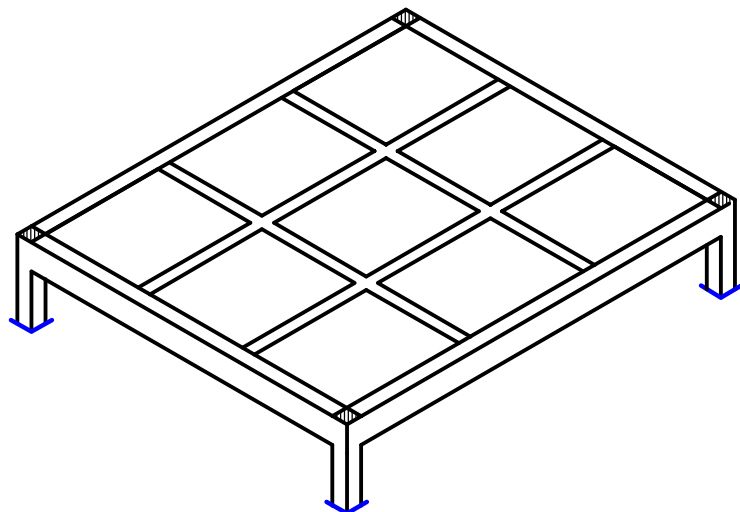


البلاطات محموله على الكمرات المتقاطعه **Panelled Beams** و الكمرات ال **Panelled Beams** محموله على الكمرات الخارجيه **Edge Beams** و الكمرات ال **Edge Beams** محموله على الاعمده .

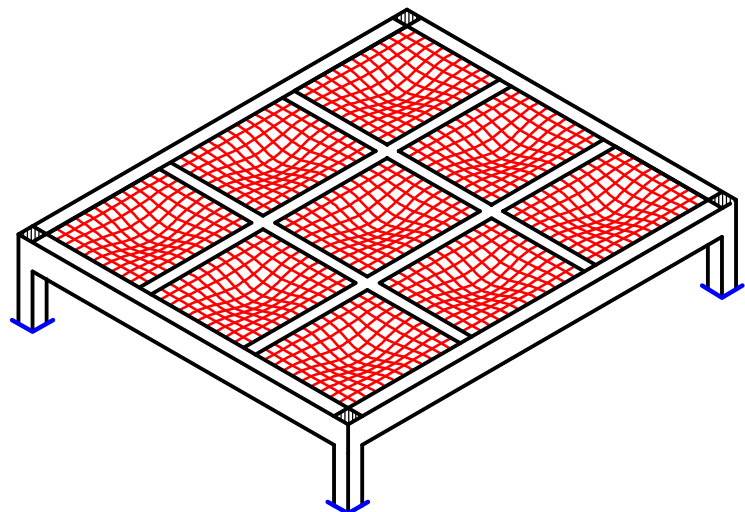
لان ال **Stiffness** للكمات ال **Panelled** أكبر بكثير من البلاطه اذاً البلاطه تعتبر محموله على ال **Panelled Beams** و ال **Edge Beams** اي اننا اعتبرنا الكمرات ال **Panelled** و ال **Edge Beams** كأنها **Rigid Supports** للبلاطه .



Edge & Panelled Beams
Rigid Supports



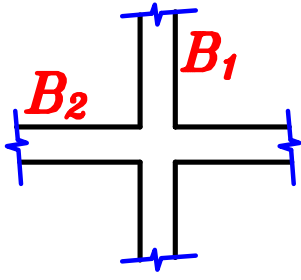
Before Loading



After Loading

ال **Panelled Beams** تكون شبكه من الكمرات محموله على الكمرات الخارجيه فقط .
والكمرات ال **Panelled** المكونه للشبكه لا يوجد اياً منها تحمل الاخرى .

أى لا يوجد كمره حامله و كمره محموله .

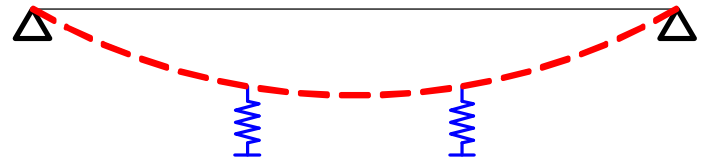
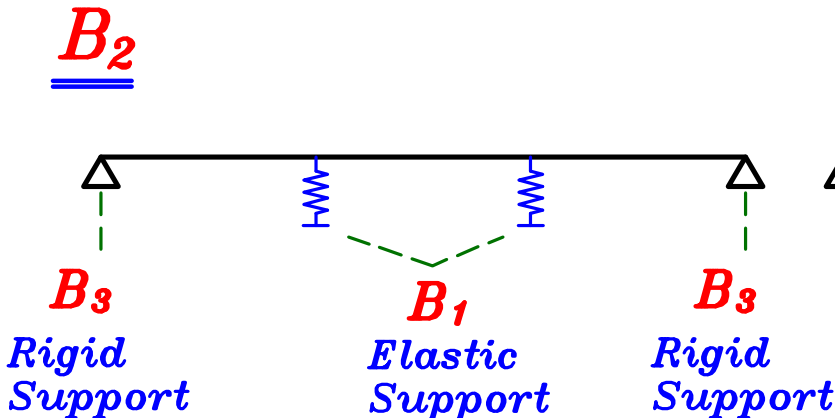
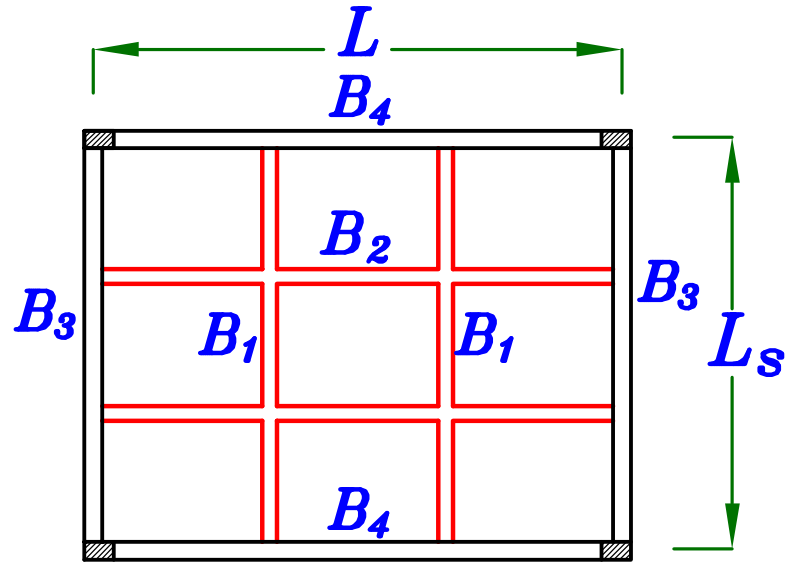
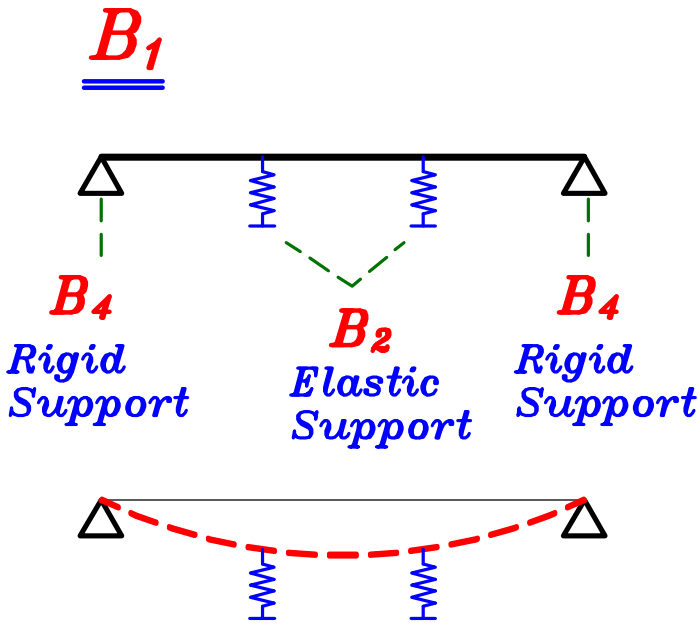


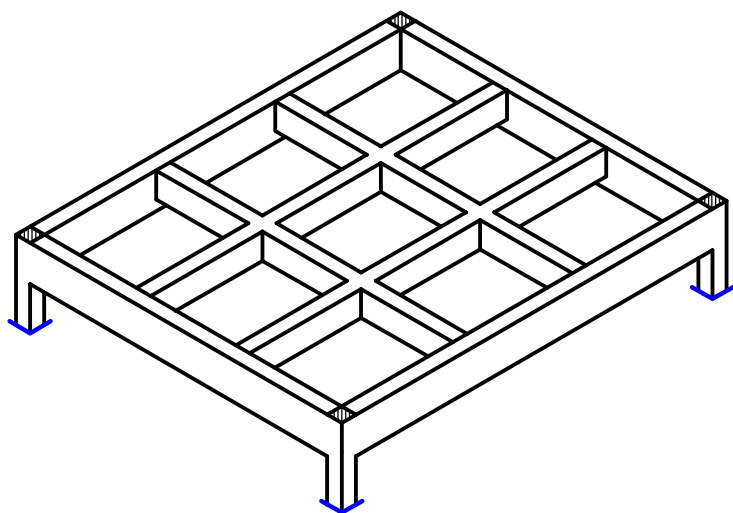
لذا عند رسم تقاطع الكمرات فى ال **Plan** ترسم كما بالشكل

و الفائده من عمل الشبكه هو انه لا توجد كمره تحمل الاخرى .

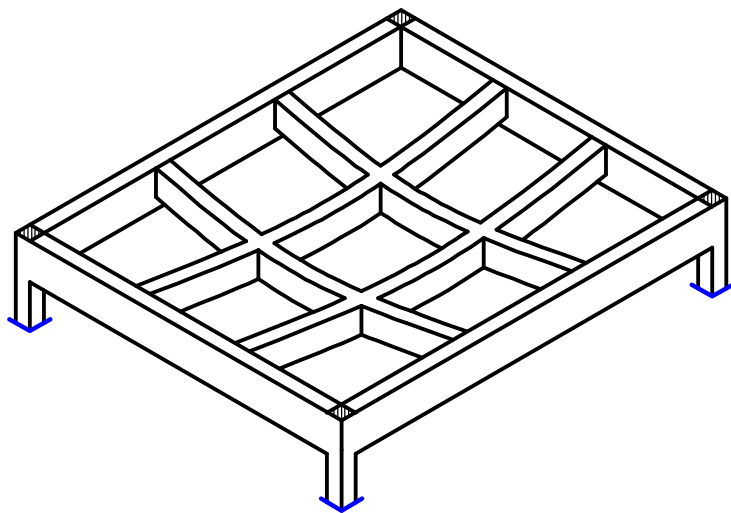
فيتوزع الحمل فى الاتجاهين فيقل ال **Deflection** و بالتالى تقل قيمه ال **moment** و بالتالى عند التصميم تكون كميه الخرسانه و الحديد المطلوبين اقل و بالتالى تكون الكمرات أرخص .

كل كمره **Panelled** تعمل بالنسبه للكمرة العموديه عليها كأنها **Elastic Support**



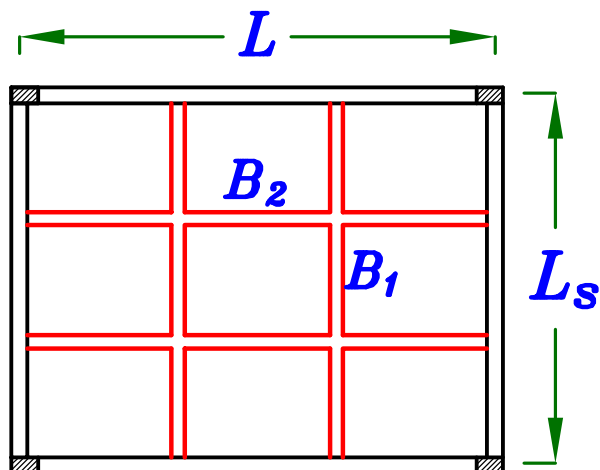


Before Loading



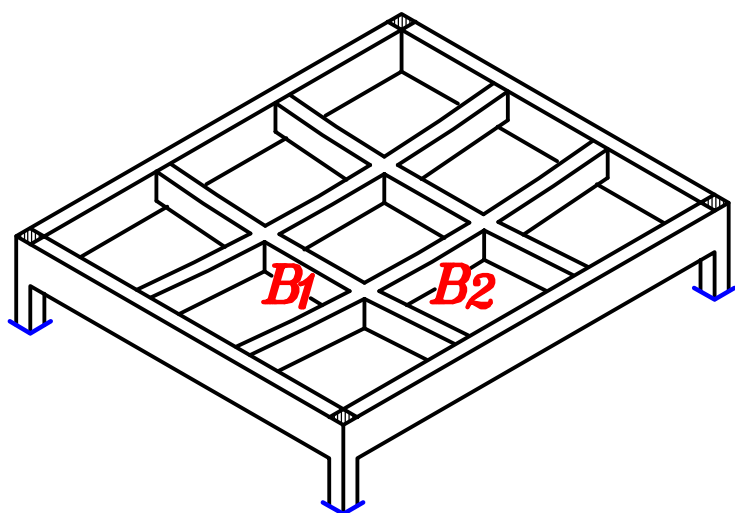
After Loading

و لكي نضمن أن الكمرات الـ **Panelled** لا تحمل الكمرات الـ **Panelled** العموديه عليها .
يجب أن تكون الـ **Stiffness** لكل من الكمرتين تقريباً متساويه .



Stiffness

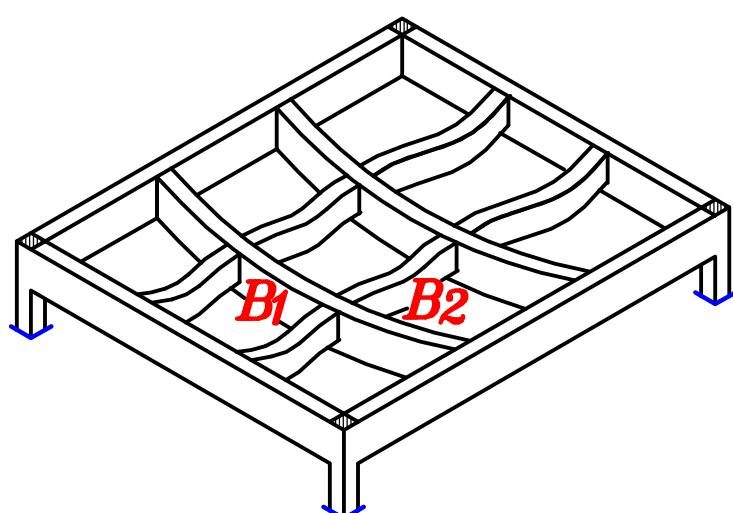
$$\left(\frac{E I}{L_s} \right) B_1 \approx \left(\frac{E I}{L} \right) B_2$$



Stiffness $B_1 \approx$ Stiffness B_2

Panelled Beams

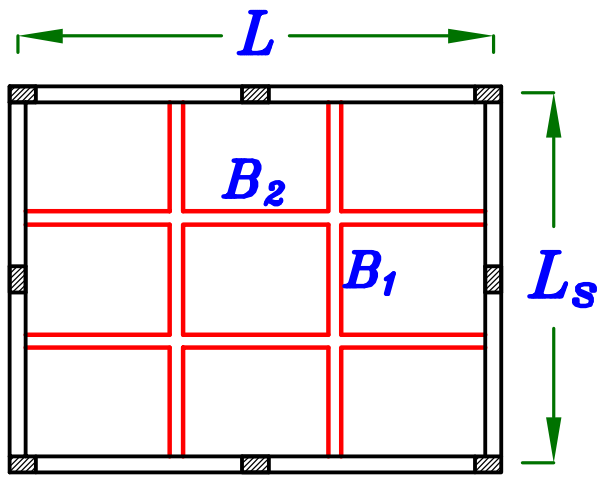
لا توجد كمره محموله على الاخرى من B_1 و B_2



Stiffness $B_1 >$ Stiffness B_2

Secondary Beams & Girders

الكمرة B_2 محموله على الكمره B_1



Stiffness

$$\left(\frac{EI}{L_s} \right) B_1 \approx \left(\frac{EI}{L} \right) B_2$$

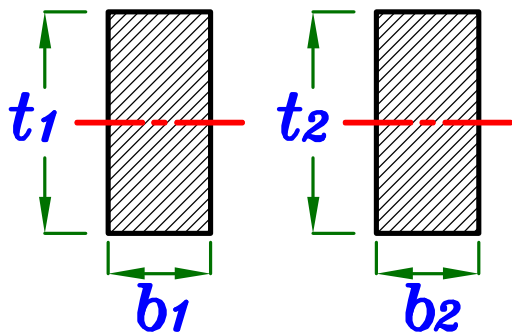
* $E \rightarrow$ **Material of the Beam.**

أى يجب أن تكون ال **Material** للكمرتين واحده (خرسانه مسلحه)

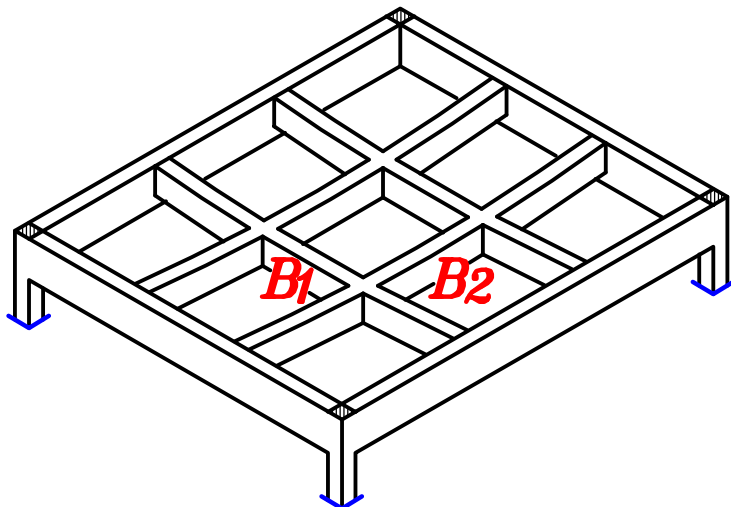
$$(E)_{B_1} = (E)_{B_2}$$

* $I \rightarrow$ **Dimensions of the Section.**

أى يجب أن تكون أبعاد القطاع لكلا الكمرتين متساوى $b_1 = b_2$, $t_1 = t_2$

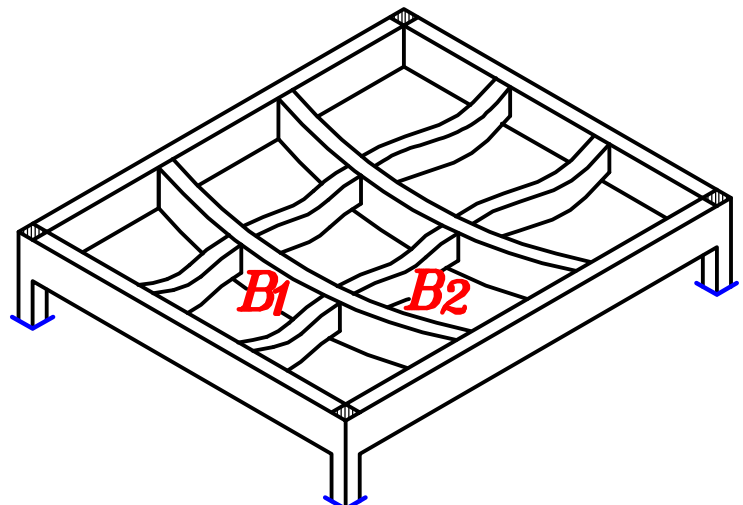


$$(I)_{B_1} = (I)_{B_2}$$



$$(I)_{B_1} = (I)_{B_2}$$

لا توجد كمره محموله على الاخرى من B_1 و B_2



$$(I)_{B_1} \gg (I)_{B_2}$$

الكمرة B_2 محموله على الكمره B_1

* $L \rightarrow$ Length of the Beam.

أى يجب أن يكون طول الكمرتين تقريباً متساوى .

$$(L)_{B_1} \simeq (L)_{B_2}$$

و حتى اذا كان الطولان مختلفان $(L)_{B_1} \neq (L)_{B_2}$ يجب ان يكون الفرق بينهم قليل .

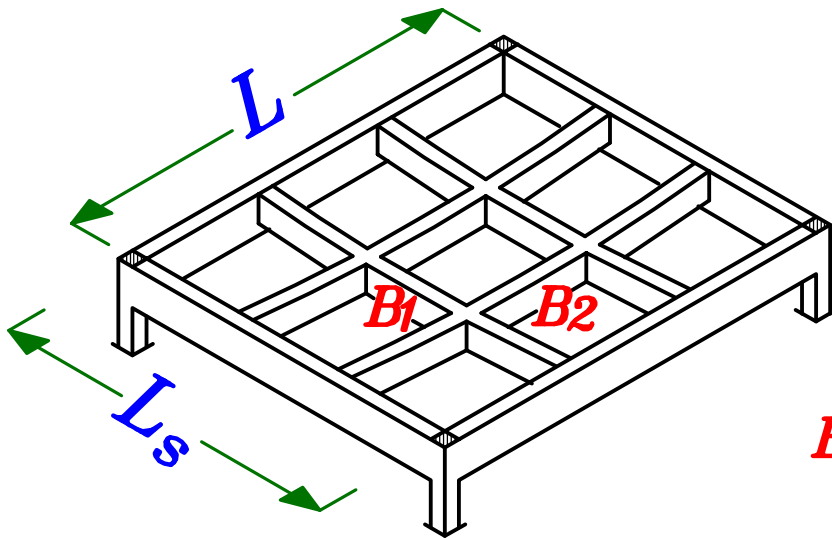
فى الكود

$$\frac{L}{L_s} \geq 1.5$$

لذا شرط فى البلاطات ال *Panelled Beams*

يفضل عملياً

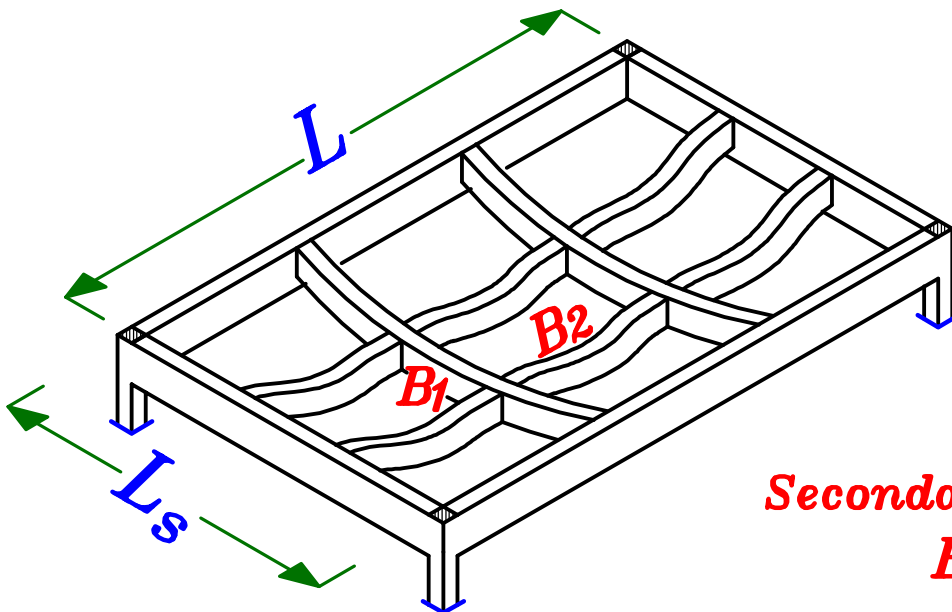
$$\frac{L}{L_s} \geq \frac{4}{3}$$



$$\frac{L}{L_s} \geq \frac{4}{3}$$

Panelled Beams

لا توجد كمره محموله على الاخرى من B_1 , B_2



$$\frac{L}{L_s} > \frac{4}{3}$$

Secondary Beams & Girders

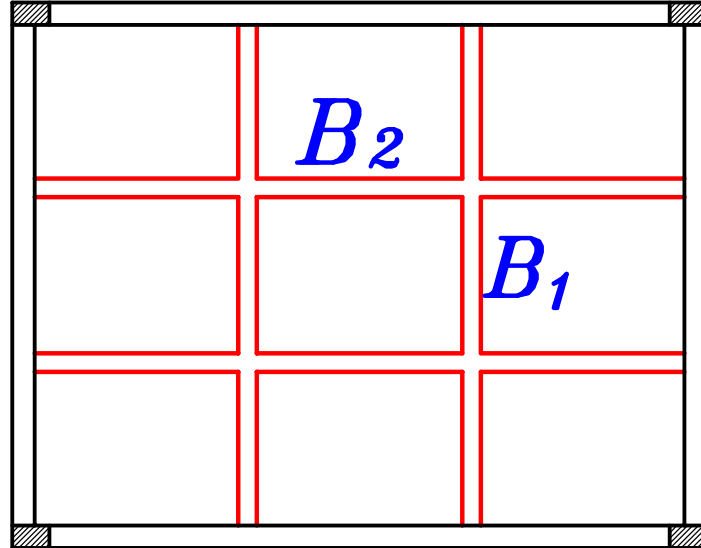
الكمرة B_2 محموله على الكمره B_1

Types of Panelled Beams.

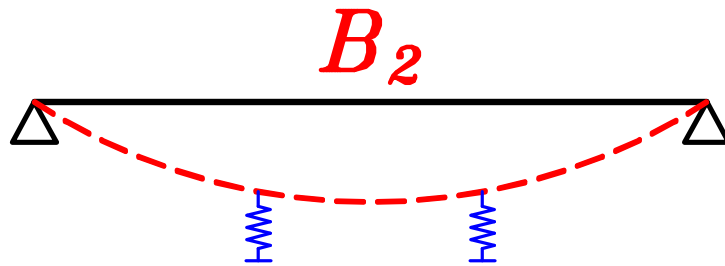


① Simple Panelled Beams.

Simple & Perpendicular. Panelled Beams.



Deflection



B.M.D.

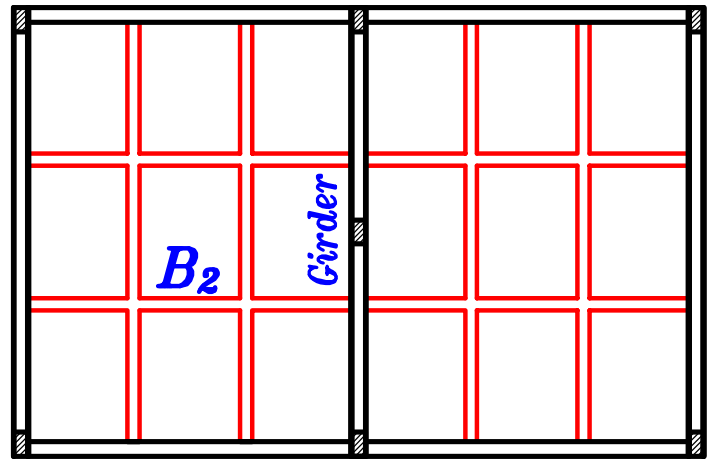
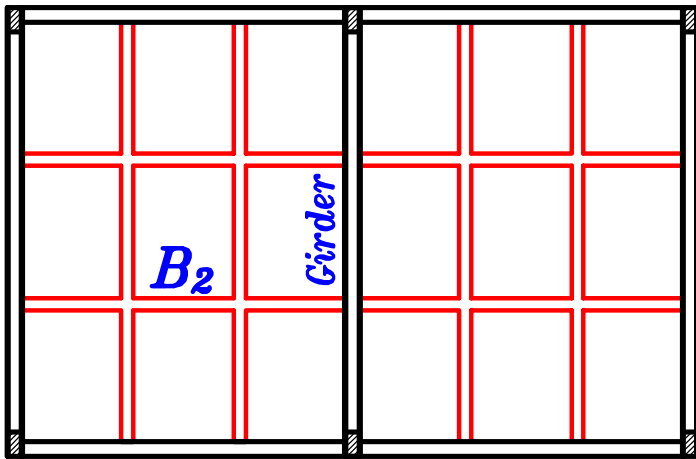
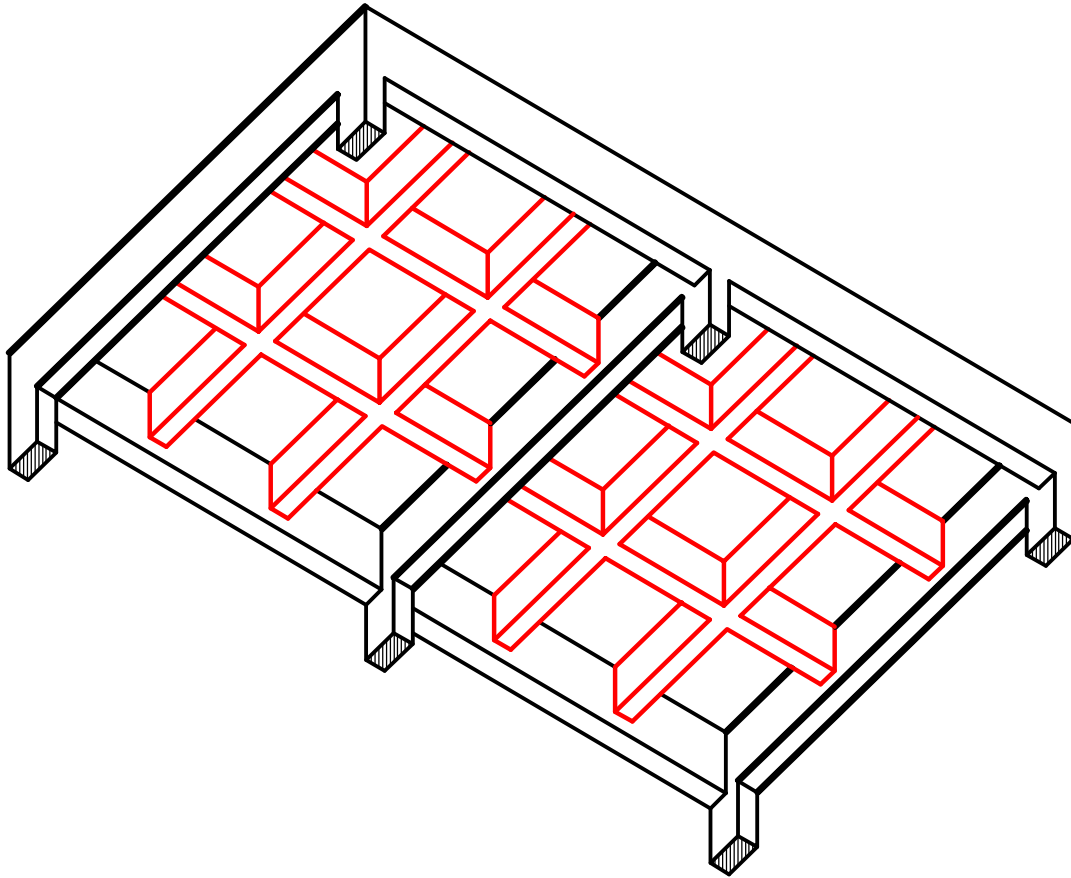


*M * Reduction Factor*

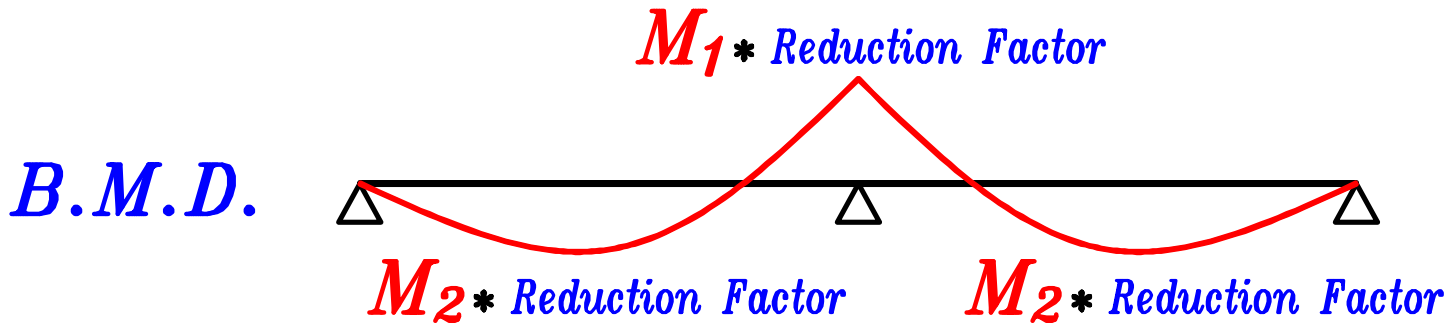
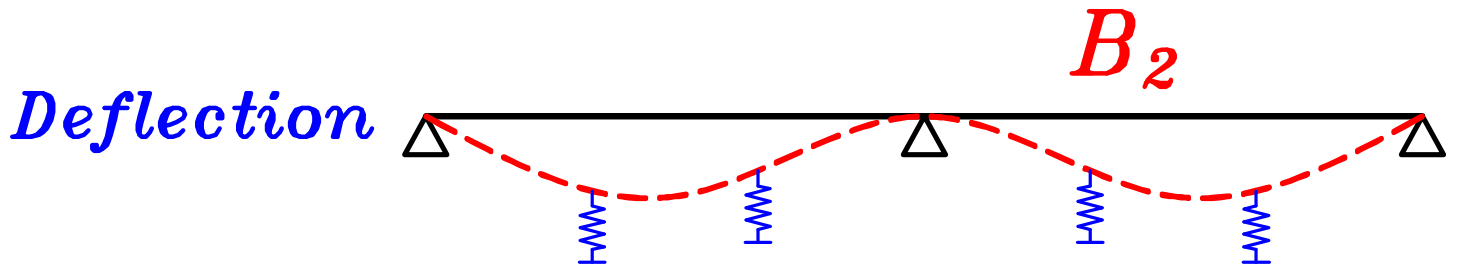
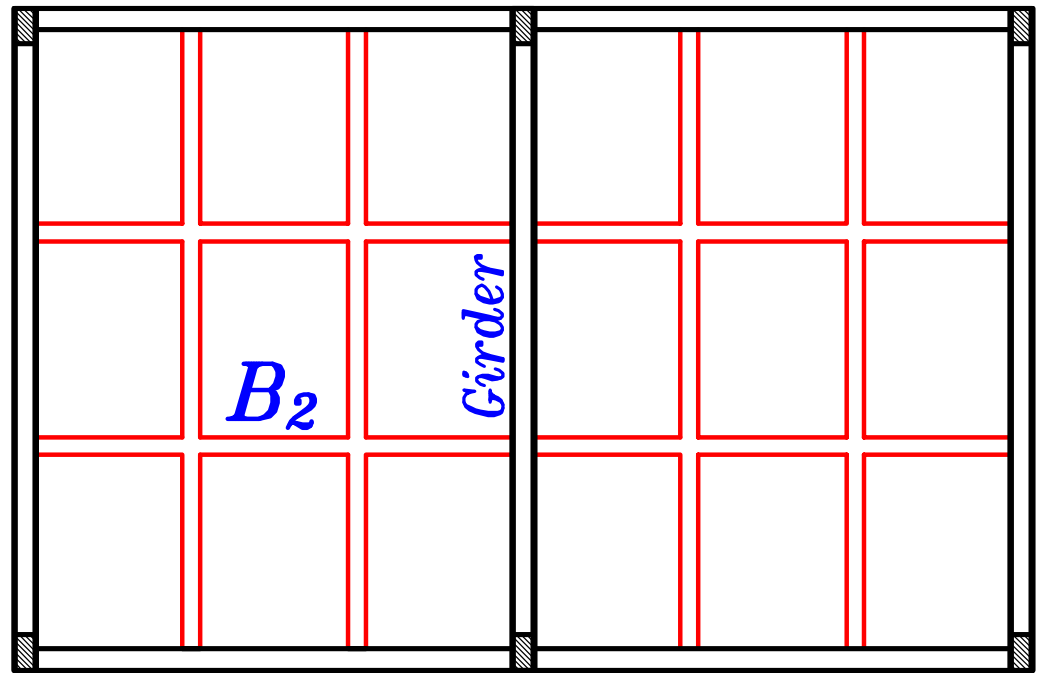
سيتم حساب ال *Reduction Factor* لاحقاً

سيتم دراسته هذا النوع فى هذا الملف .

② Continuous Panelled Beams.



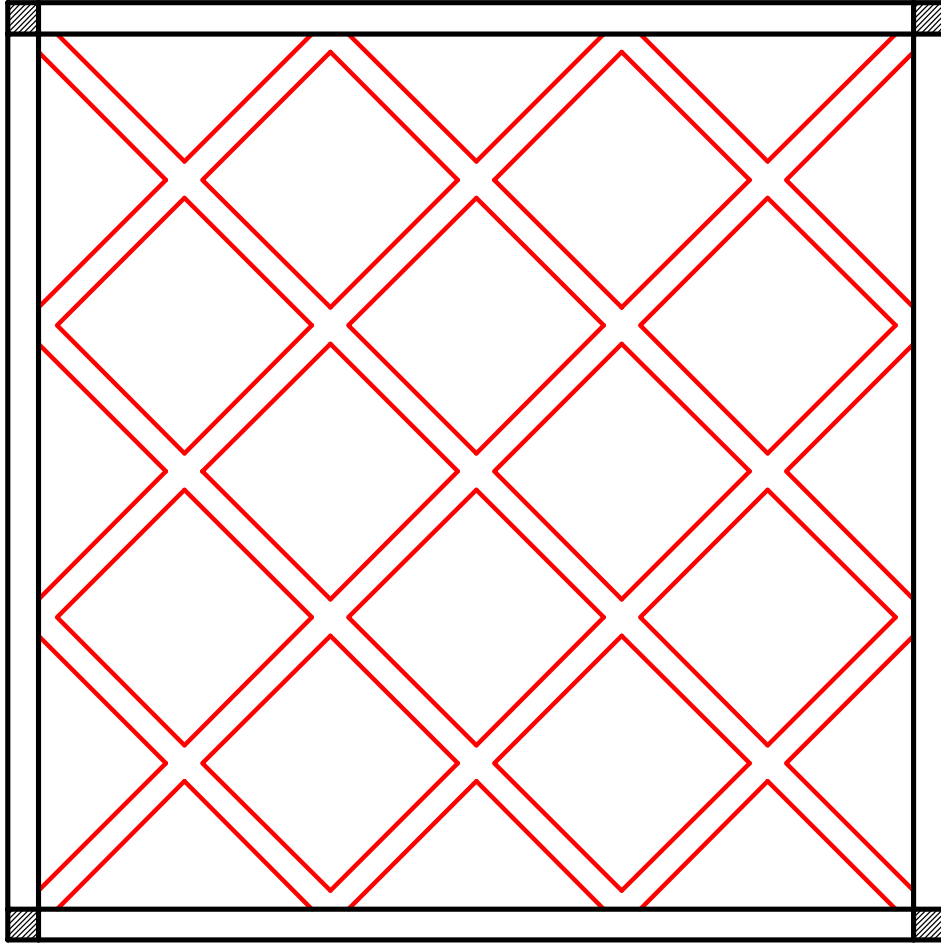
لكى نضمن ان ال **Girder** سيحمل الكمره **B₂**
يجب ان تكون ال **Stiffness** لل **Girder** اكبر بكثير من الكمره **B₂**
إما عن طريق زياده أبعاد قطاع ال **Girder** لزياده ال **I** لل **Girder**
او وضع عمود فى منتصف ال **Girder** لتقليل ال **L** لل **Girder**



لن نستطيع حساب الـ *Reduction Factor* بالطرق اليدويه
لذا سنضطر لحساب الـ *Continuous Panelled beams*
عن طريق الكمبيوتر .

لن يتم دراسته هذا النوع فى هذا الملف .

③ Skew Panelled Beams.



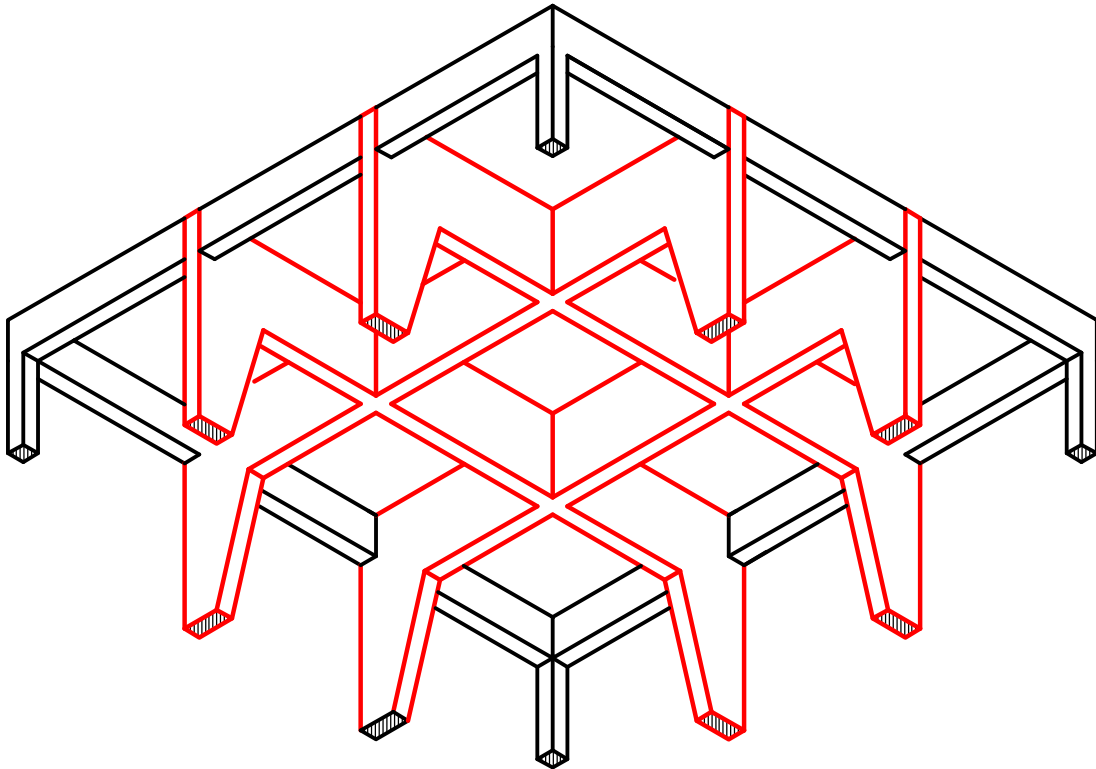
لان أطوال الكمرات مختلفه فتكون **Stiffness** الكمرات مختلفه
و بالتالى يكون توزيع الاحمال مختلف .

لن نستطيع حساب ال **Reduction Factor** بالطرق اليدويه
لذا سنضطر لحساب ال **Skew Panelled Beams**
عن طريق الكمبيوتر .

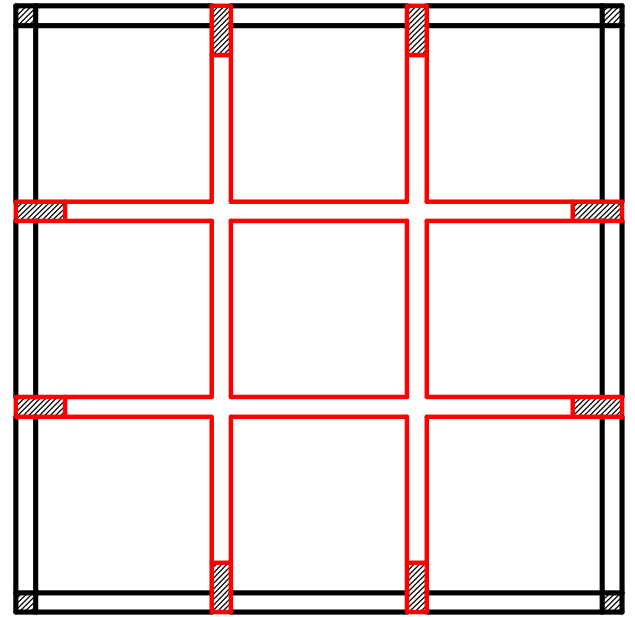
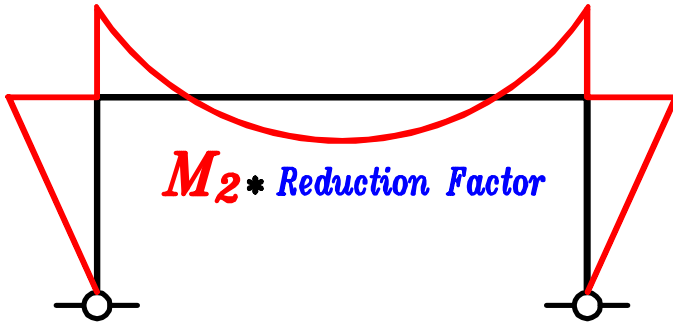
لن يتم دراسته هذا النوع فى هذا الملف .

④ Panelled Frames.

Simple & Perpendicular. Panelled Frames.



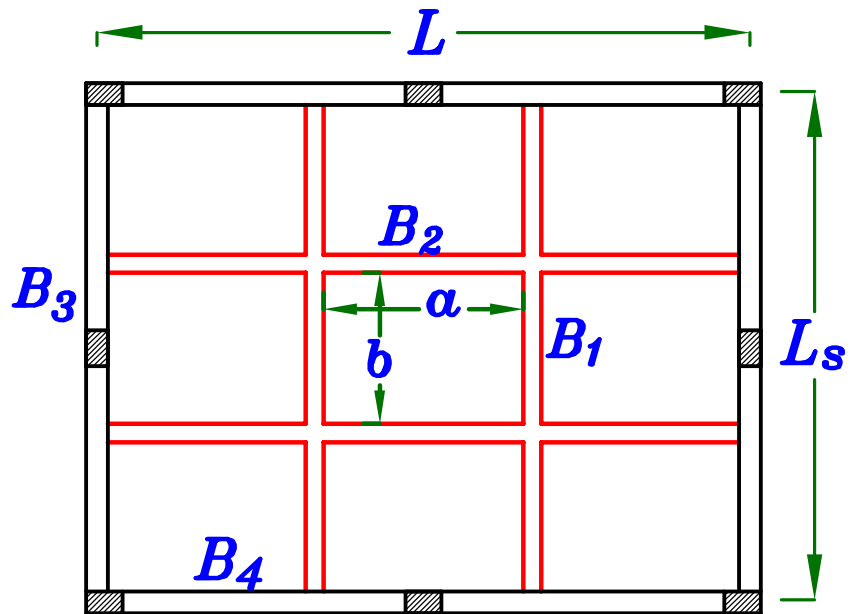
M_1 * Reduction Factor



لن نستطيع حساب ال *Reduction Factor* بالطرق اليدويه
لذا سنضطر لحساب ال *Panelled Frames* عن طريق الكمبيوتر .

لن يتم دراسته هذا النوع فى هذا الملف .

Simple Panelled Beams.



Steps of Design.

- ① **Design the slabs.** (Two way slab يفضل أن تكون)
(Solid or Hollow Blocks Slabs) ($a * b$)

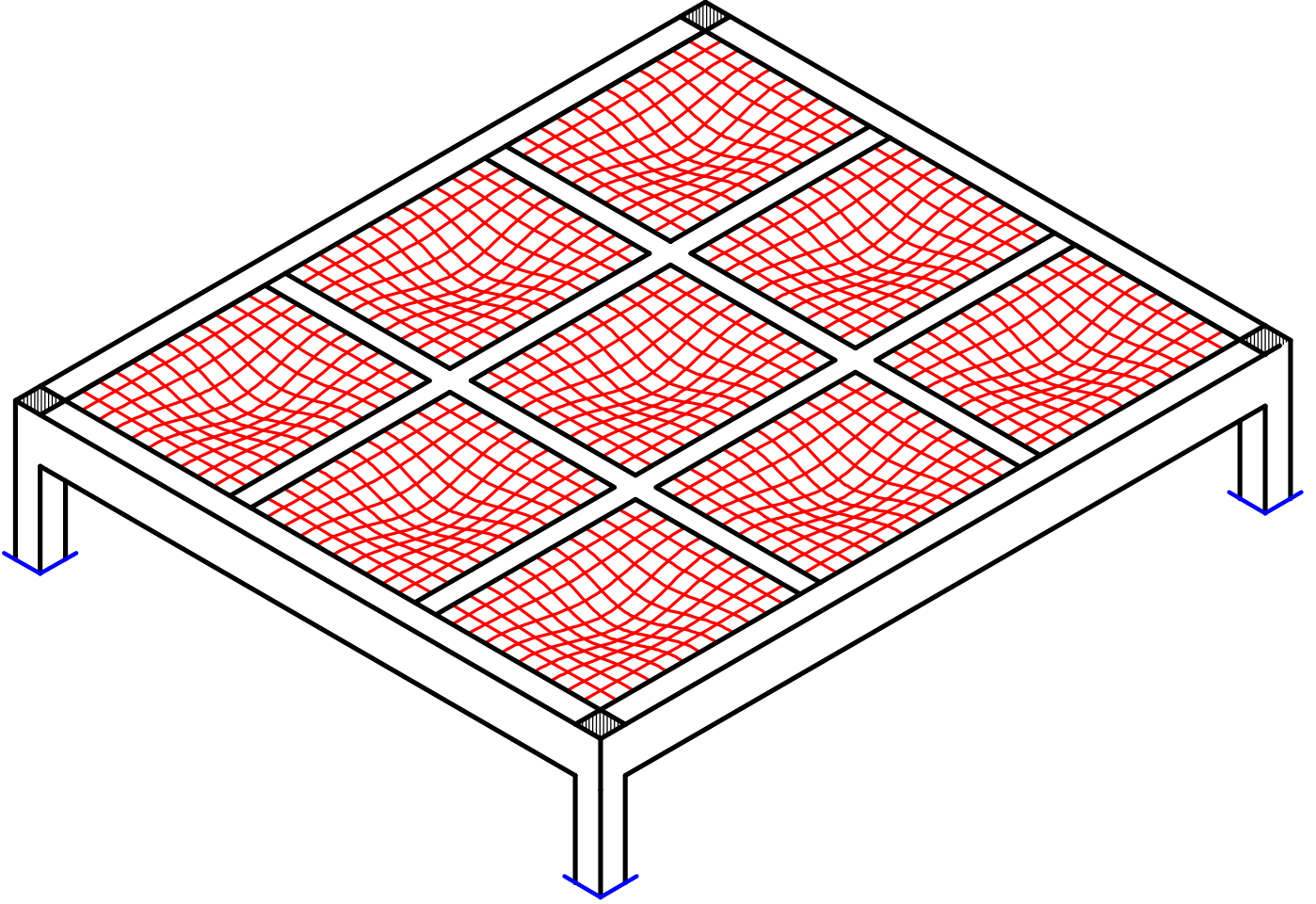
- a- Choose the Thickness of the Slab (t_s).
- b- Get the Loads on the Slab (w_s).
- c- Get the Load Factors α, β .
- d- Take a strips in the slab (at the Load direction)
And then Get (B.M.) on the Slab & Design the slab.
- e- Draw Details of RFT. of the slab in plan.

- ② **Design the Panelled Beams.** (B_1, B_2)

- a- Get Dimensions of the beams. (b, t).
- b- Get the average Load on the Slab. (w_{av}).
- c- Calculate α, β (For the hall area) By using Grashoff.
- d- Get the Loads on the Panelled Beam & Calculate the B.M.
- e- Calculate the reduction Factor of the B.M. ($\frac{\sin \theta}{\sin 90}$)
- f- Design the Panelled Beam.
- g- Draw Details of RFT. For the Panelled Beams.

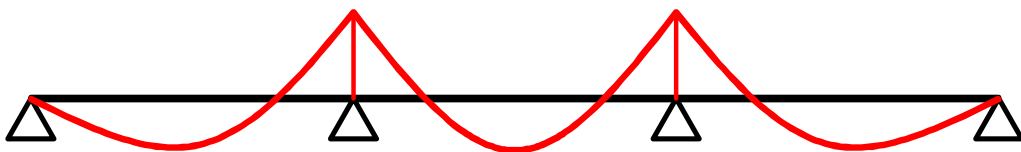
- ③ **Design the Edge Beams.**
(The Exterior Beam) (B_3, B_4)

① Design the slabs.



لان ال **Stiffness** للكمرات ال **Panelled** أكبر بكثير من البلاطه
اذا البلاطه تعتبر محموله على ال **Panelled Beams** و ال **Edge Beams**
اي اننا اعتبرنا الكمرات ال **Panelled** و ال **Edge Beams**
كأنها **Rigid Supports** للبلاطه .

لان شريحه البلاطه محموله على اكثر من **2 supports** اذا تعتبر شريحه **Continuous**



شريحه فى البلاطه

• يتم تصميم البلاطات سواء كانت **Solid or Hollow** بالخطوات العاديه لتصميم البلاطات .

IF all The Slabs are Two way Solid Slabs.

a- Choose the Thickness of the Slab. (t_s).

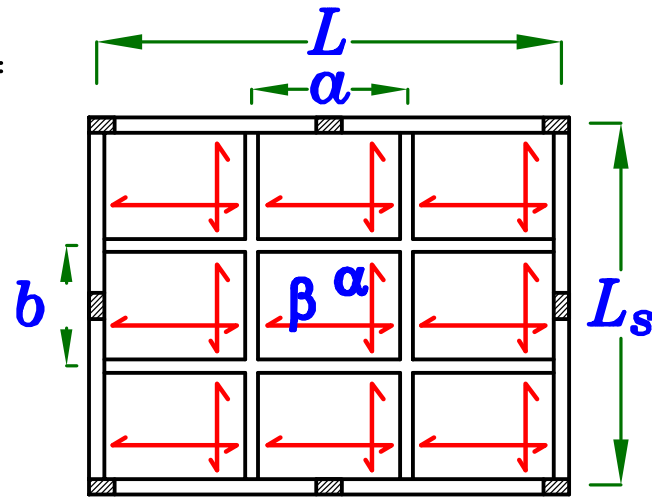
Take $t_s = \frac{L_s}{35 \text{ or } 40 \text{ or } 45}$ where: $L_s = (b)$

b- Get the Loads on the Slab. (w_s).

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 L.L.$$

c- Get the Load Factors α , β

Get $r = \frac{m L}{m' L_s} = \frac{m \alpha}{m' b}$



① IF $L.L. \leq 5.0 \text{ kN/m}^2$

Use **C.P.** (Code of Practice)

الحالة العامة

$$\alpha = 0.5 r - 0.15$$

$$\beta = \frac{0.35}{r^2}$$

② IF $L.L. > 5.0 \text{ kN/m}^2$ Use **Grashoff**

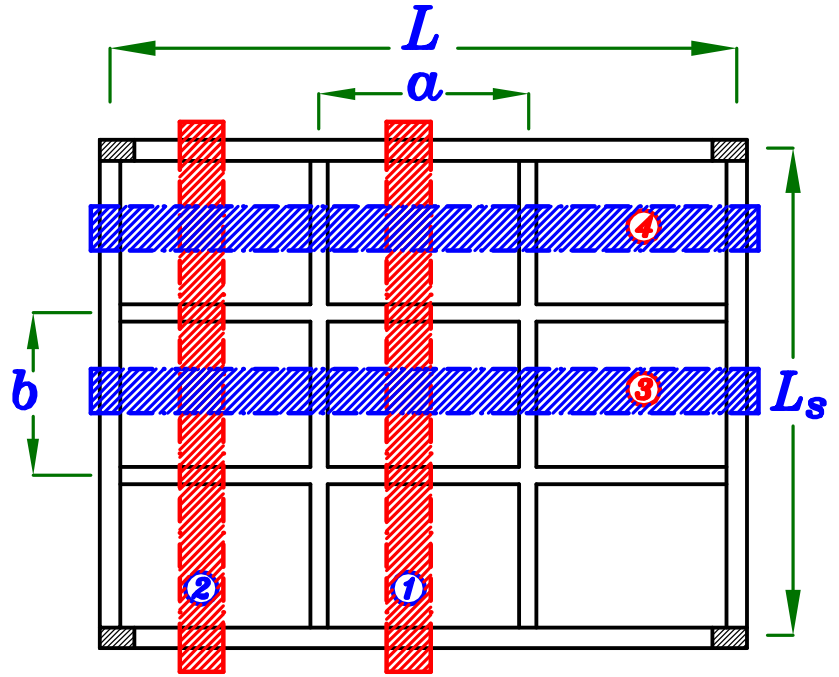
$$\alpha = \frac{r^4}{1 + r^4}$$

$$\beta = \frac{1}{1 + r^4}$$

d- Take a strips in the slab (at the Load directions)
And then Get the Bending Moments (B.M.) on the Slab.
& Design the slab.

تؤخذ ال **Strips**
 حسب شكل البلاطة

فى هذا الشكل يوجد **4 Strips**



Strips at α direction.

Take Cover For Short Dir.
 = **20 mm** (**α Dir.**)

$$d_{\alpha \text{ Dir.}} = t_s - 20 \text{ mm}$$

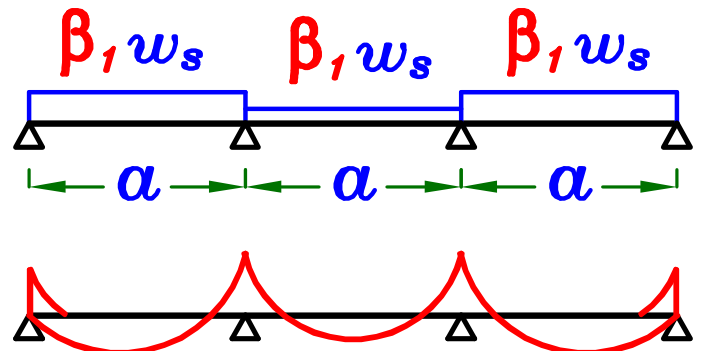
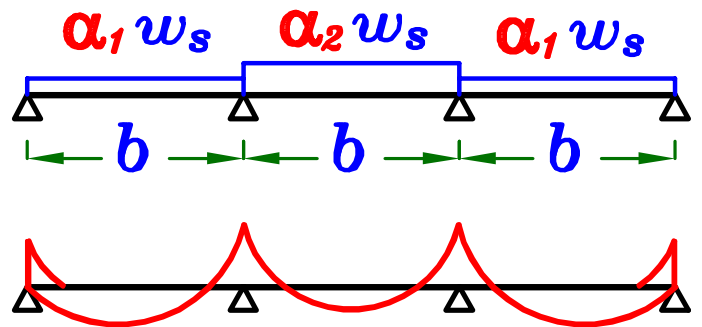
Then get **$A_s \alpha$**

Strips at β direction.

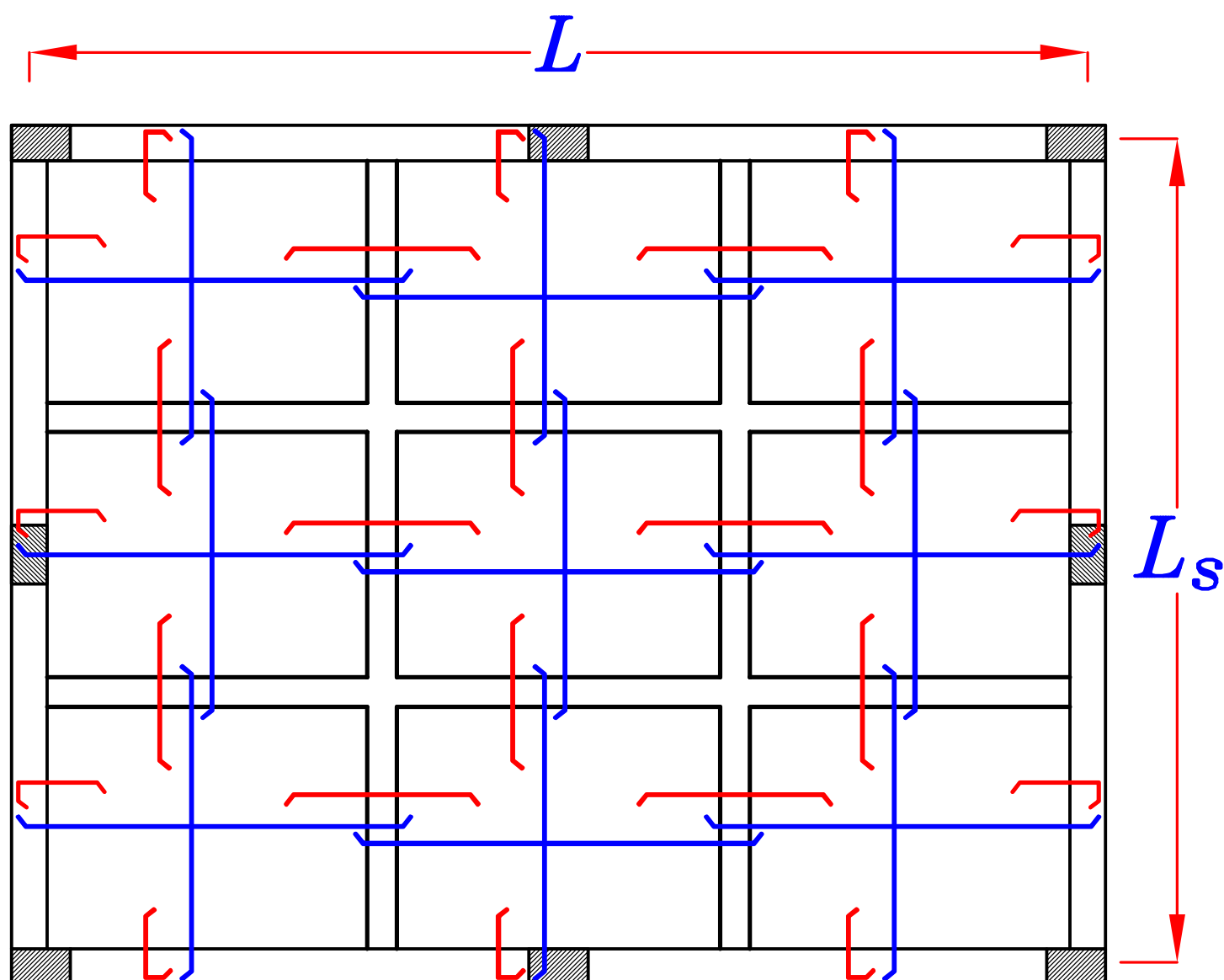
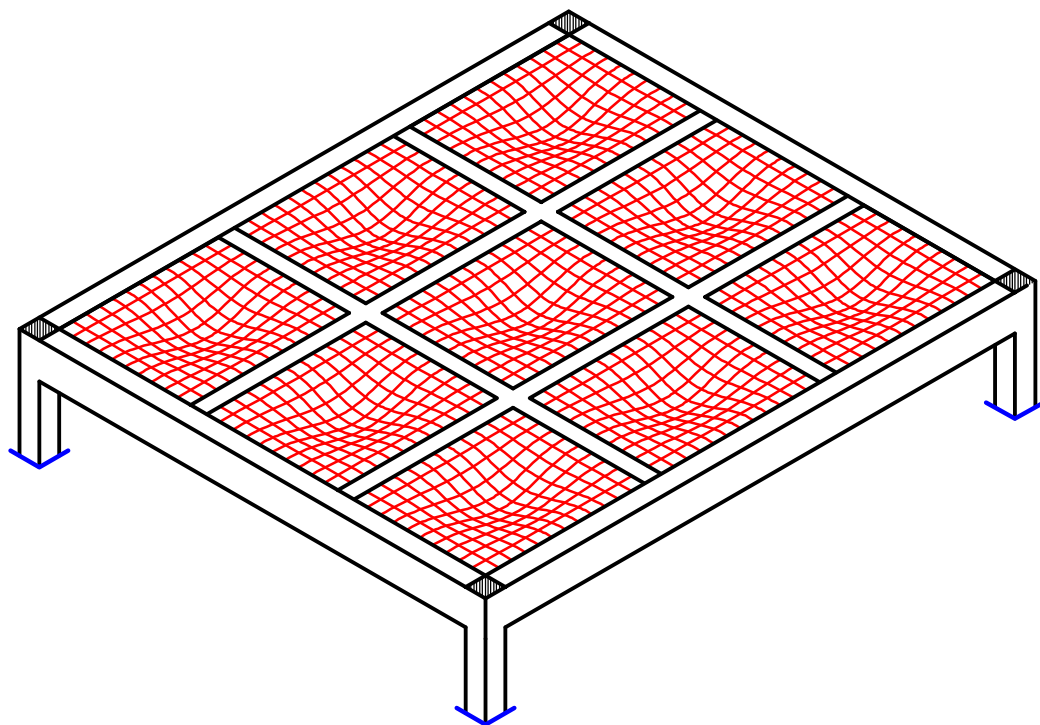
Take Cover For Long Dir.
 = **30 mm** (**β Dir.**)

$$d_{\beta \text{ Dir.}} = t_s - 30 \text{ mm}$$

Then get **$A_s \beta$**



e - Draw Details of RFT. For the slab.



② Steps of Design the Panelled Beams.

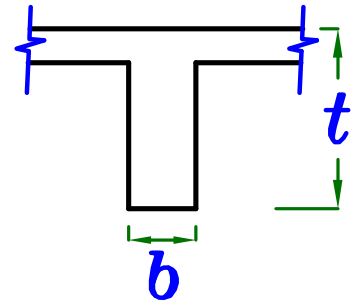


- 1 – Get Dimensions of the beams. (b, t).
- 2 – Get the average Load on the Slab. (w_{av}).
- 3 – Calculate α, β (For the hall area) By using Grashoff.
- 4 – Get Loads on the Panelled Beam & Calculate the B.M.
- 5 – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$
- 6 – Design the Panelled Beam.
- 7 – Draw Details of RFT. For the Panelled Beams.

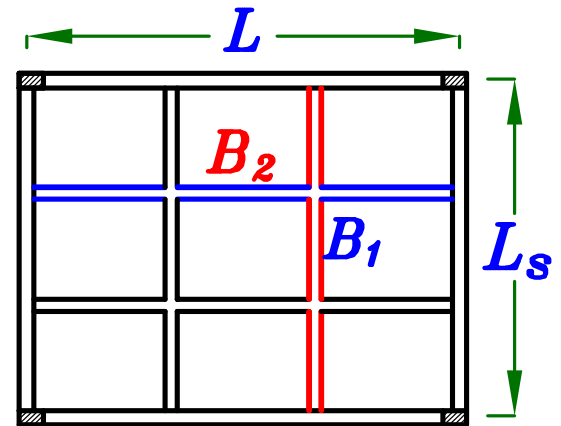
α - Get the Dimensions of the beam. (b, t)



- Take $b = 250 \text{ mm}$ or $= 300 \text{ mm}$



لان الكمرات B_1, B_2 مكونه شبكه
اذاً عند وجود **Load** سيتوزع على مساحة اكبر
اذاً قيمه ال **Deflection** للكمرات ستقل
اذاً قيمه ال **moment** للكمرات ستقل
اذاً لن نحتاج قيمه t كبيره للكمرات .



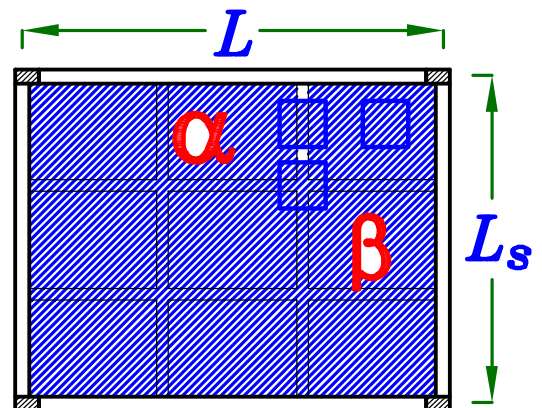
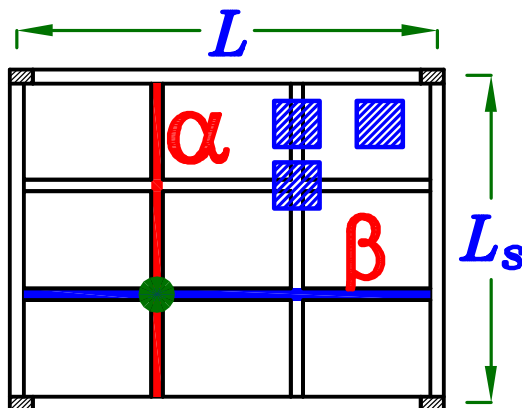
- Take t For B_1, B_2

$$t = \frac{L_s}{16} = \checkmark \text{ mm}$$

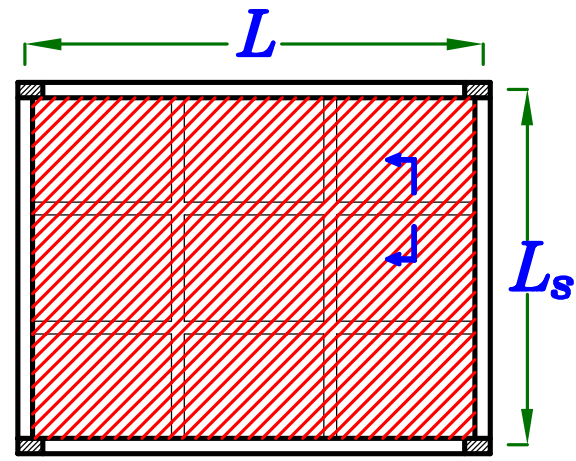
تقرب لأقرب ٥. مم بالزيادة

b - Get the average Load on the Slab. ($w_{av.}$)

اذا وضع حمل عند تقاطع كمرتين معا سيتوزع على الكمرتين بنسبه α, β
و يتم حساب قيمتي α, β بطريقه **Grashoff** ولكن قوانين **Grashoff** مستنتجه
على أساس ان الحمل كله منتظم أى أن وزن المتر المربع متساوى على كل المساحه .
لذا نعمل على فرض ان الحمل كله منتظم بحساب قيمه ($w_{av.}$)



نعتبر أن السقف عبارة عن بلاطة كبيرة
 ولة وزن مكافئ ($w_{av.}$)



$$w_{av.} = \frac{\sum \text{Weight}}{\text{Area}} = \checkmark \text{ kN/m}^2$$

$$w_{av.} = \frac{\text{Total Weight of slabs} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

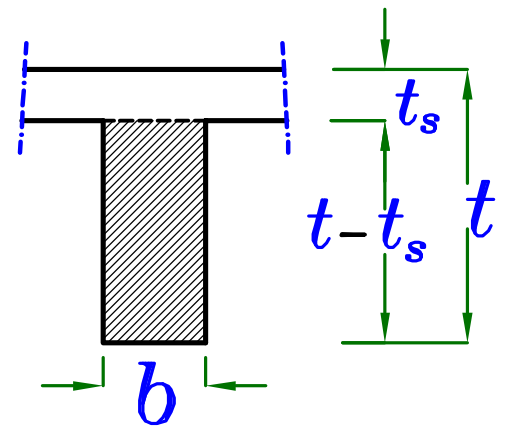
وزن المتر المربع من البلاطة

$$\begin{aligned} \text{Total Weight of slabs} &= w_s * \text{Total area} \\ &= w_s * (L * L_s) \end{aligned}$$

Total Weight of Panelled Beams =

Volume of all Panelled Beams * δ_c

$$b(t - t_s) [\text{مجموع أطوال الكمرات الـ panelled}] * \delta_c$$

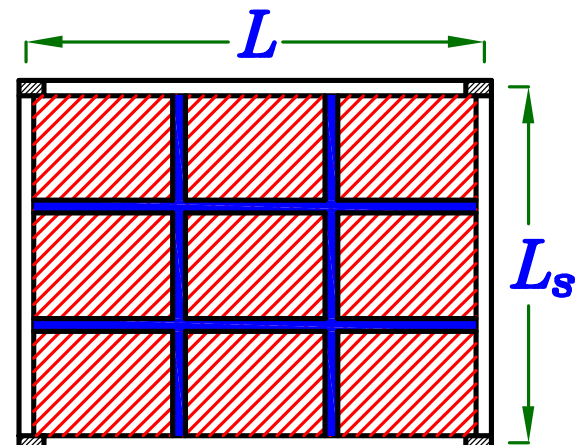


مجموع أطوال الكمرات الداخلية فى هذا المثال

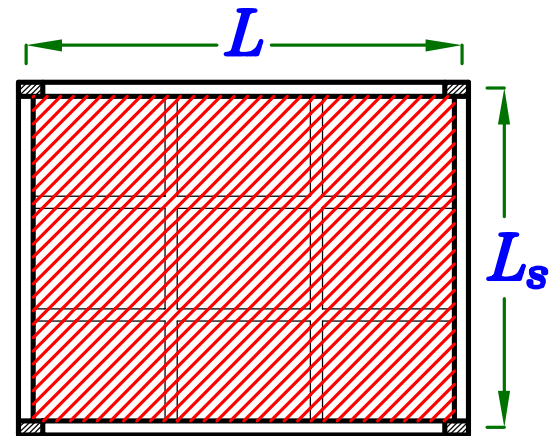
$$\sum L = (2L + 2L_s)$$

Total Weight of Panelled Beams =

$$1.4 * b(t - t_s)(2L + 2L_s) * \delta_c$$



1 – IF the slabs is Solid slabs only.

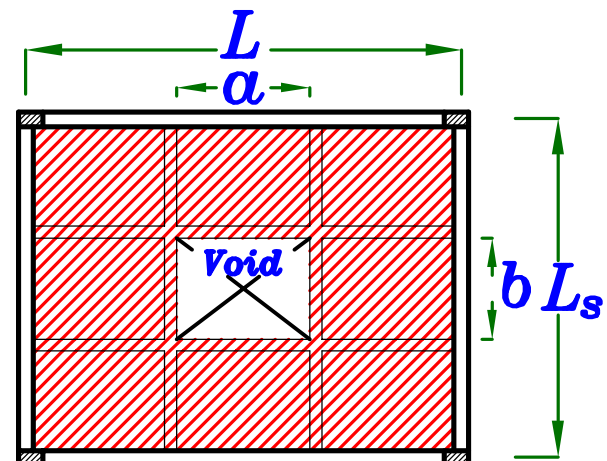


$$W_{av.} = \frac{\text{Total Weight of slabs} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

$$W_{av.} = \frac{W_s * (L * L_s) + \text{Total Weight of Panelled Beams}}{L * L_s}$$

$$W_{av.} = W_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s}$$

2 – IF the slabs is Solid slabs with Void.

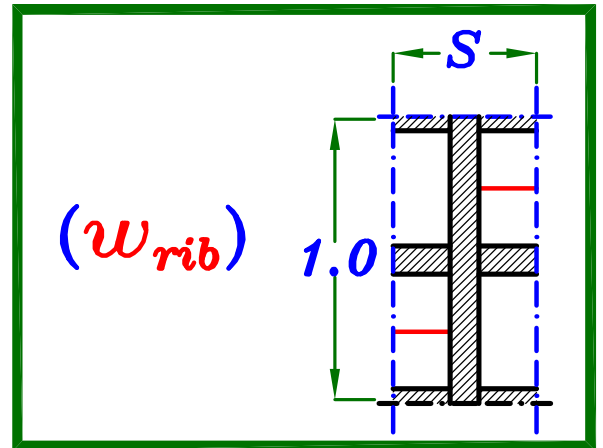
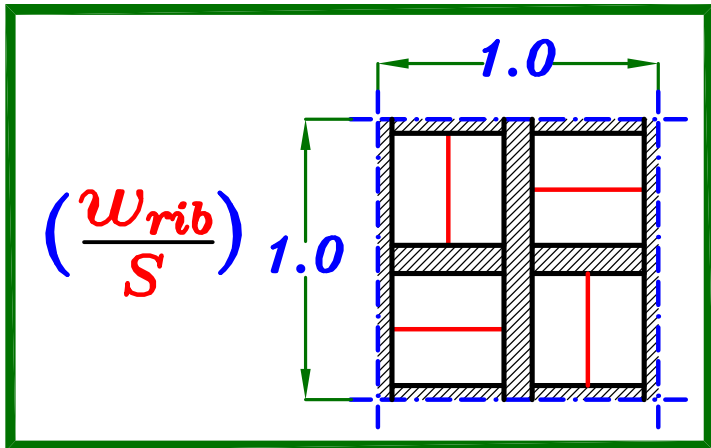


$$W_{av.} = W_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s - \alpha * b}$$

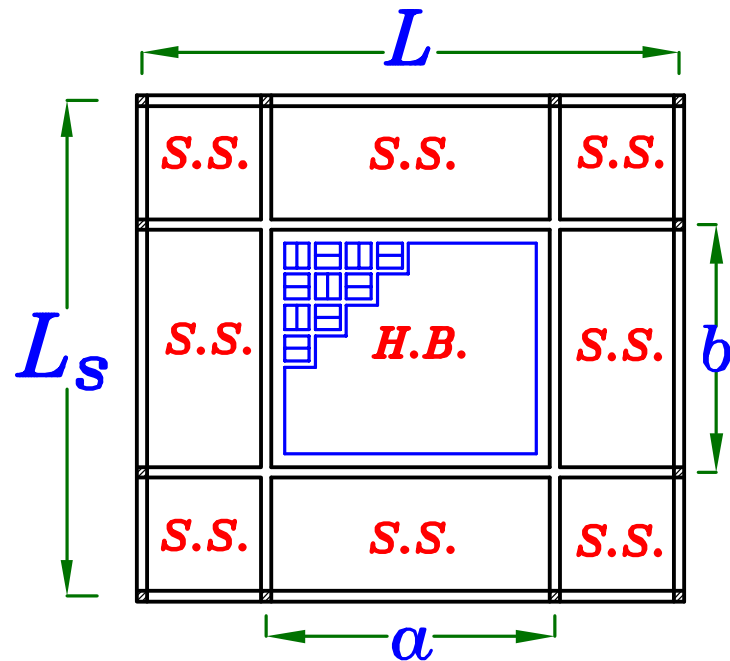
3 – IF the slabs is Solid & Hollow Blocks Slabs.

(W_{rib}) هو وزن مساحة $(1.0 m * S)$ من البلاطة ال **H.B.**

∴ لحساب وزن $(1.0 m * 1.0 m)$ من البلاطة ال **H.B.** $\left(\frac{W_{rib}}{S}\right) =$



$$W_{av.} = \frac{\sum \text{Weight}}{\text{Area}} = \checkmark \text{ kN/m}^2$$



$$W_{av.} = \frac{\text{Total Weight of Solid slabs} + \text{Total Weight of H.B. slabs} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

$$W_{av.} = \frac{w_s * \text{area (s.s.)} + \left(\frac{W_{rib}}{S}\right) * \text{area (H.B.)} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

$$W_{av.} = \frac{w_s * (L * L_s - a * b) + \left(\frac{W_{rib}}{S}\right) * (a * b) + [1.4 * b (t - t_s) (2L + 2L_s) * \delta_c]}{L * L_s}$$

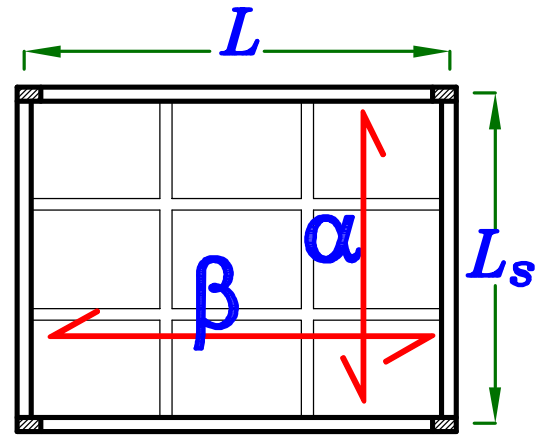
C- Calculate α , β By using Grashoff.



بعد تحويل الحمل كله الى حمل منتظم نستطيع الان ان نحسب قيم α , β عن طريق *Grashoff* و لاننا نحسب قيم α , β للكمات ال *Panelled* و ليس للبلاطات و لاننا ندرس الكمات ال *Simple Panelled Beams* فقط اذا دأها ستكون قيمه m , m' دأها تساوى 1.0

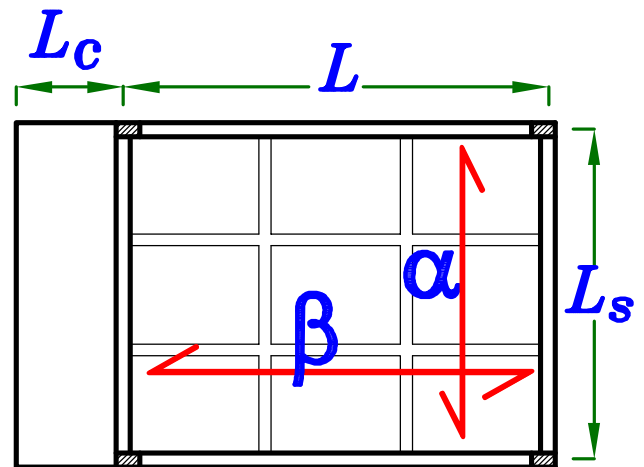
$$m = 1.0 , m' = 1.0$$

$$r = \frac{m L}{m' L_s} = \frac{(1.0) L}{(1.0) L_s}$$



$$m = 1.0 , m' = 1.0$$

$$r = \frac{m L}{m' L_s} = \frac{(1.0) L}{(1.0) L_s}$$



نستخدم *Grashoff* لحساب كلا من α , β

Grashoff _____

$$\alpha = \frac{r^4}{1 + r^4}$$

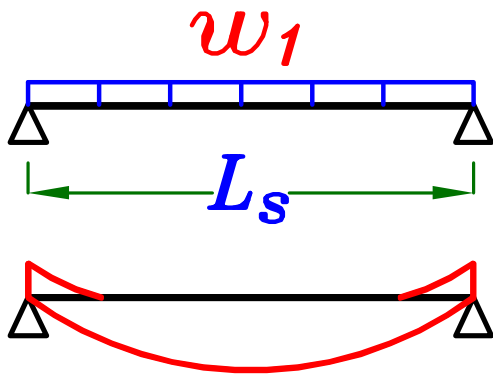
$$\beta = \frac{1}{1 + r^4}$$



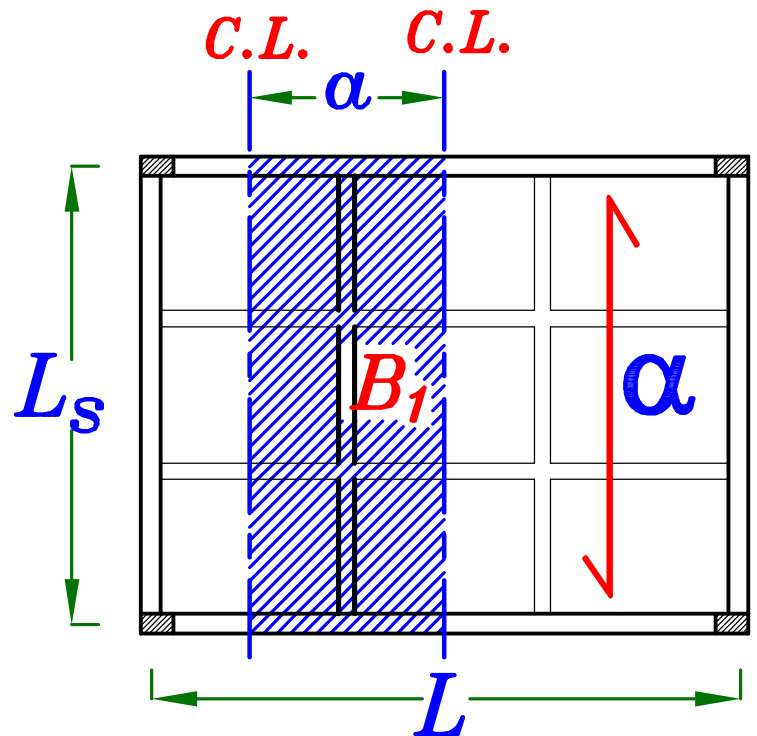
Load Distribution لحساب الاحمال فوق كل كمره **Panelled** لن نستطيع عمل **Panelled** لانه فى الكمرات ال **Panelled** لا يوجد كمرات تحمل الاخرى
اى ان الحمل الكلى يتوزع على الكمرات فى الاتجاهين بنسب α , β
لذا نعتبر كل كمره تحمل نفس احمال الشريجه التى عرضها من **C.L.** البلاطه على يمين الكمره الى **C.L.** البلاطه على يسار الكمره .

For B_1

$$w_1 = w_{av.} * \alpha * \alpha$$



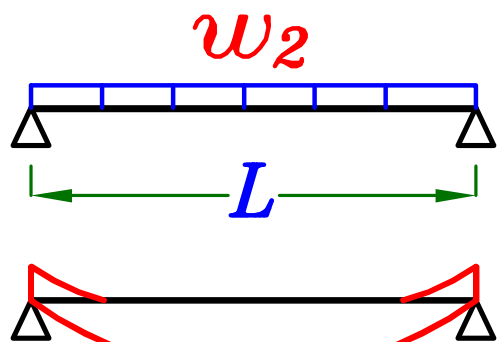
M * Reduction Factor



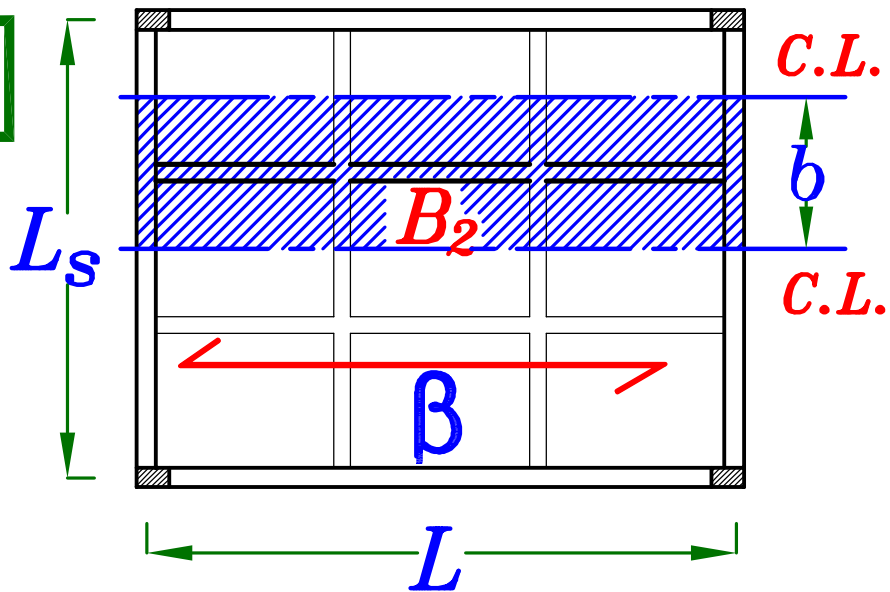
$$M_1 = \frac{w_1 * L_s^2}{8} * \text{Reduction Factor}$$

For B_2

$$w_2 = w_{av.} * b * \beta$$



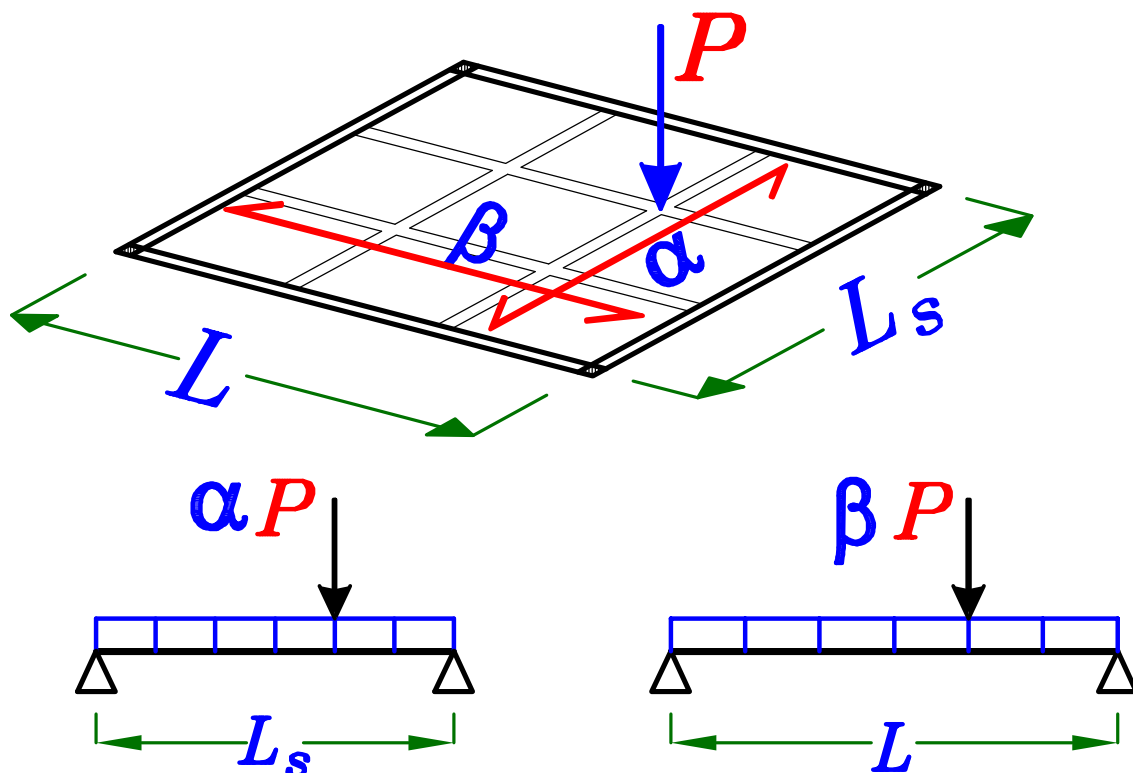
M * Reduction Factor



$$M_2 = \frac{w_2 * L^2}{8} * \text{Reduction Factor}$$

ملحوظه

عند وجود حمل مركزى (P) واقع على تقاطع كمرتين يتوزع على الكمرتين بنسب α , β



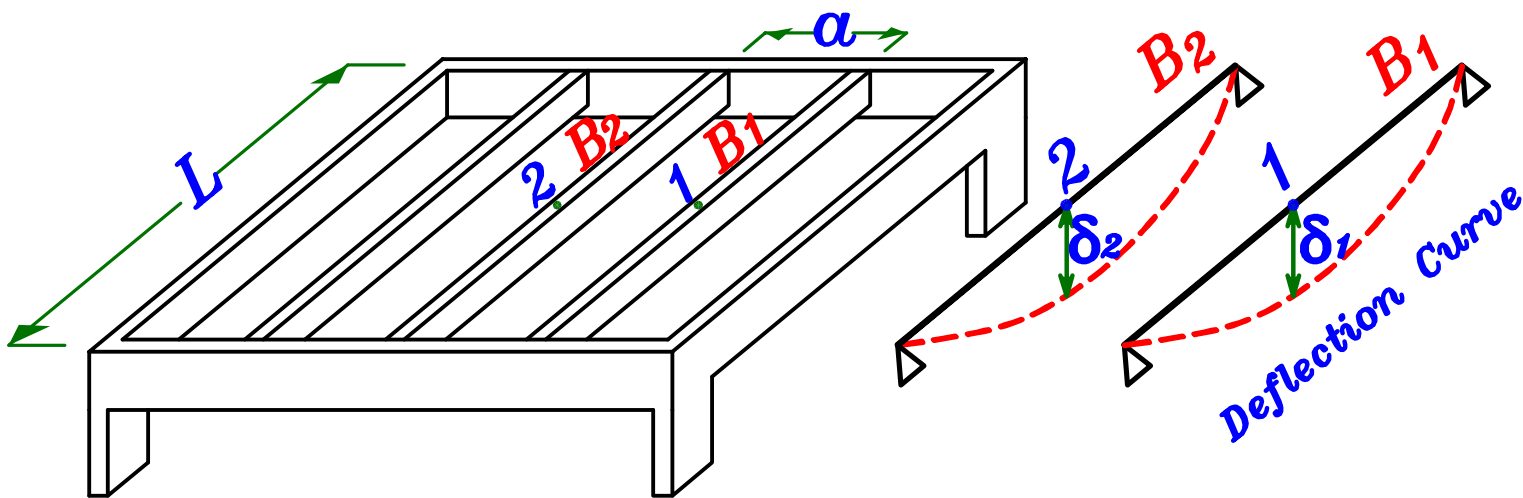
E- Calculate the reduction Factor of the B.M.



بعد حساب ال **moment** على الكمرات ال **panelled** نحتاج لتقليل هذا ال **moment** لوجود الكمرات فى شبكة **Grid Action**

و لفهم تأثير ال **Grid Action** و تحديد قيمه ال **Reduction Factor** نشرح فى المثال التالى :

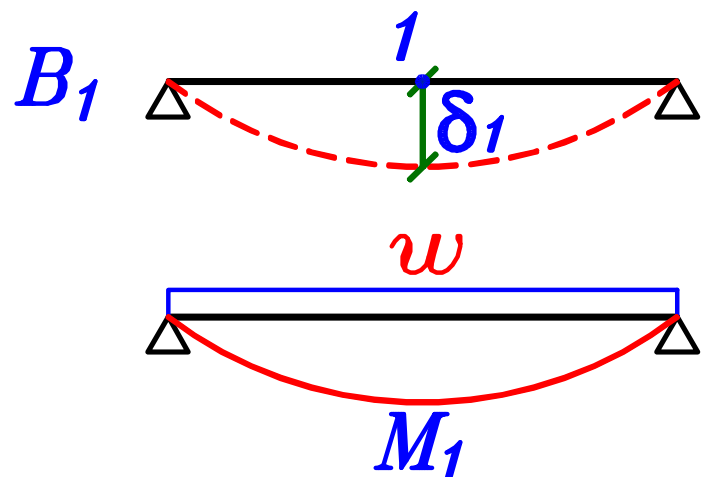
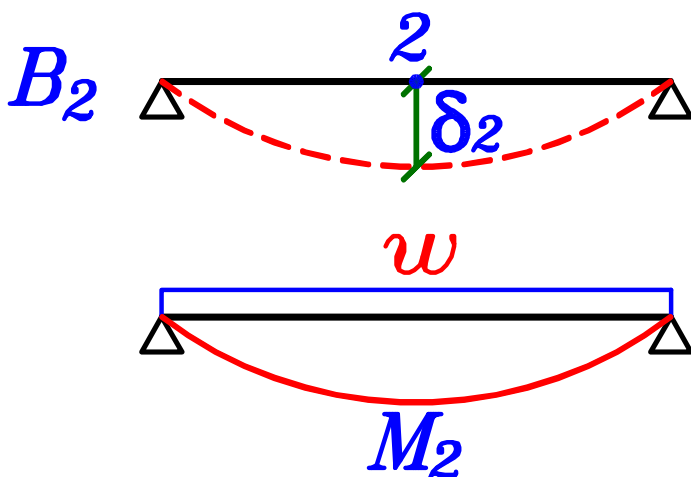
اذا كانت الكمرات B_1, B_2 موضوعة على مسافات متساويه α



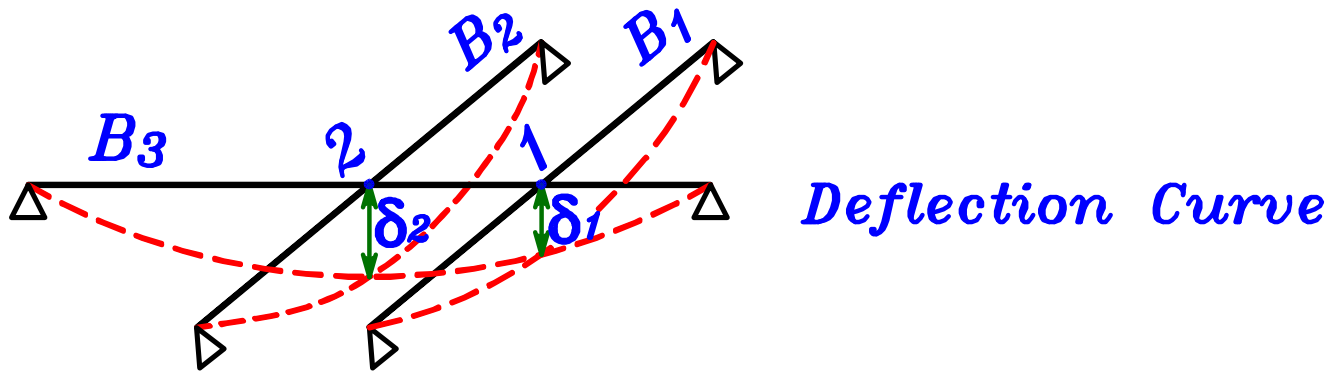
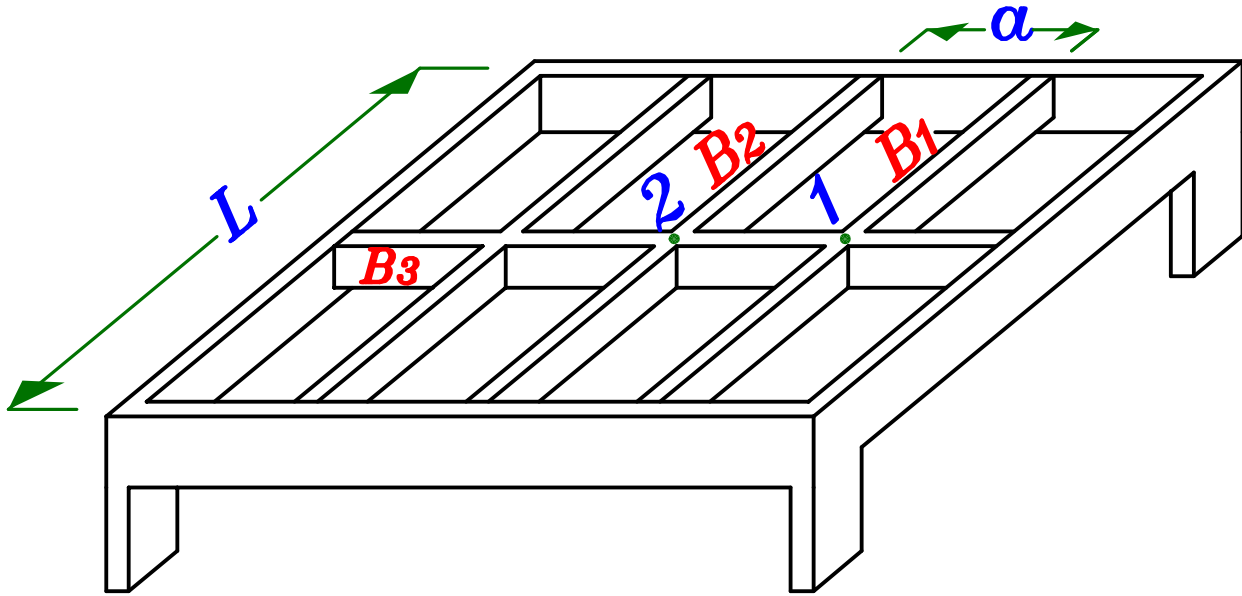
ستحمل الكمرتين نفس الحمل $w = w_1 = w_2 = w_{av} * \alpha$

و بالتالى سيكون ال **Deflection** للکمرتين متساوى . $\therefore \delta_1 = \delta_2$

و بالتالى سيكون ال **moment** للکمرتين متساوى . $\therefore M_1 = M_2$



إذا وضعنا الكمره B_3 عموديه على الكمرتين B_1, B_2 فى المنتصف تماماً .
 أى اننا ربطنا الكمرتين B_1, B_2 بكمره عموديه عليهم .

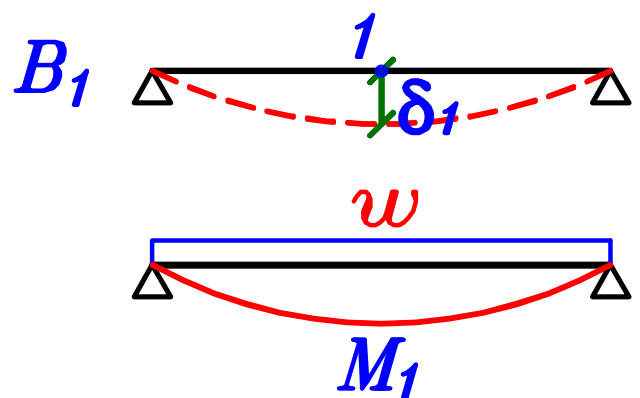
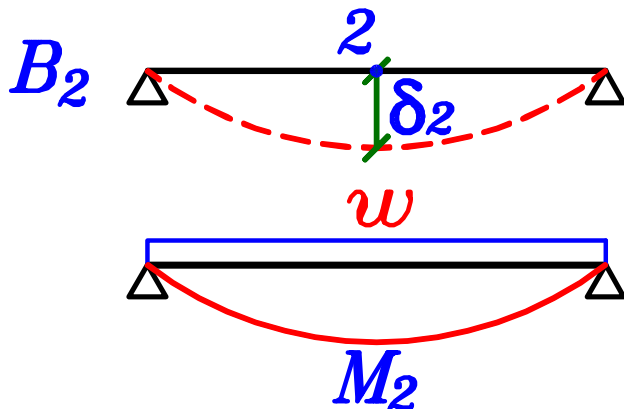


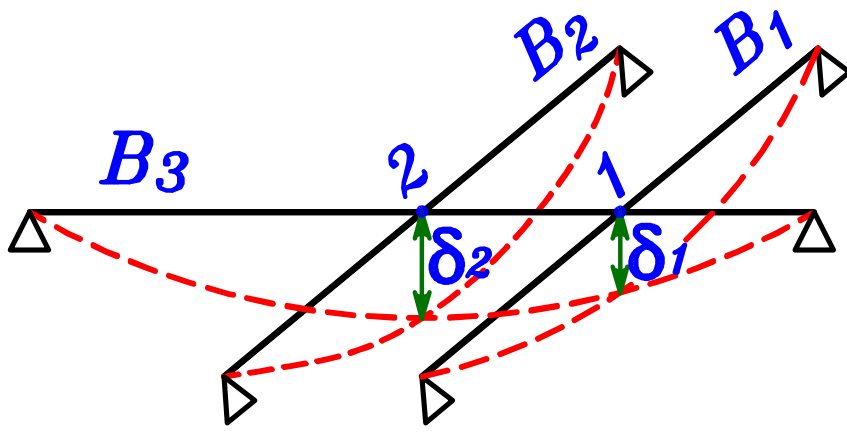
فى هذه الحاله سيكون ال **Deflection** للکمره B_1 أقل من ال **Deflection** للکمره B_2 التى فى المنتصف .

ستحمل الكمرتين نفس الحمل $w = w_1 = w_2 = w_{av.} * \alpha$

و لكن **Deflection** الكمرتين غير متساوى . $\therefore \delta_1 < \delta_2$

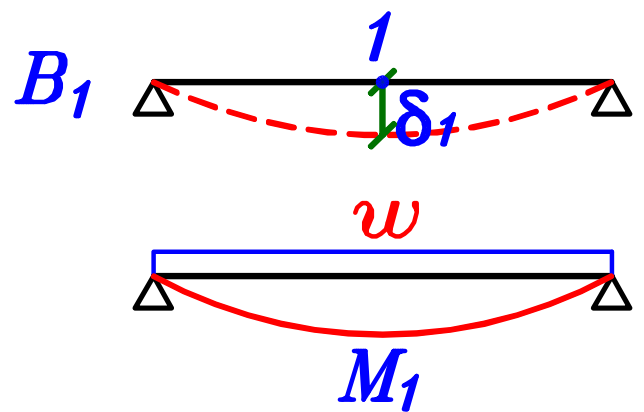
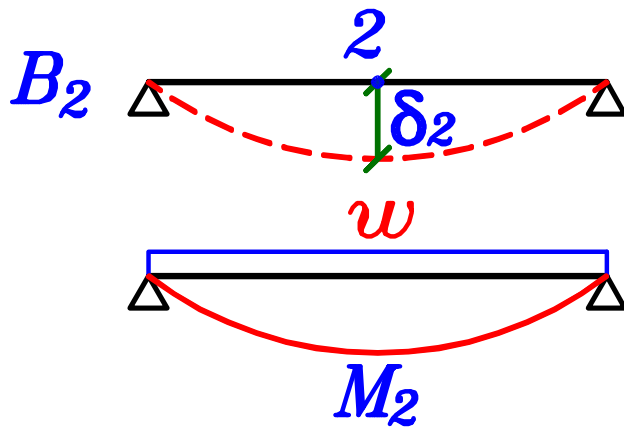
و بالتالى سيكون ال **moment** للکمرتين غير متساوى . $\therefore M_1 < M_2$





و لحساب قيمه ال **Reduction Factor** للكمرة **B₁** يساوى $\left(\frac{\delta_1}{\delta_2}\right)$

حيث δ_1 هى قيمه ال **Deflection** عند تقاطع الكمره المطلوبه **B₁** مع الكمره العموديه عليها **B₃**
حيث δ_2 هى قيمه اكبر **Deflection** عند الكمره العموديه عليها **B₃**



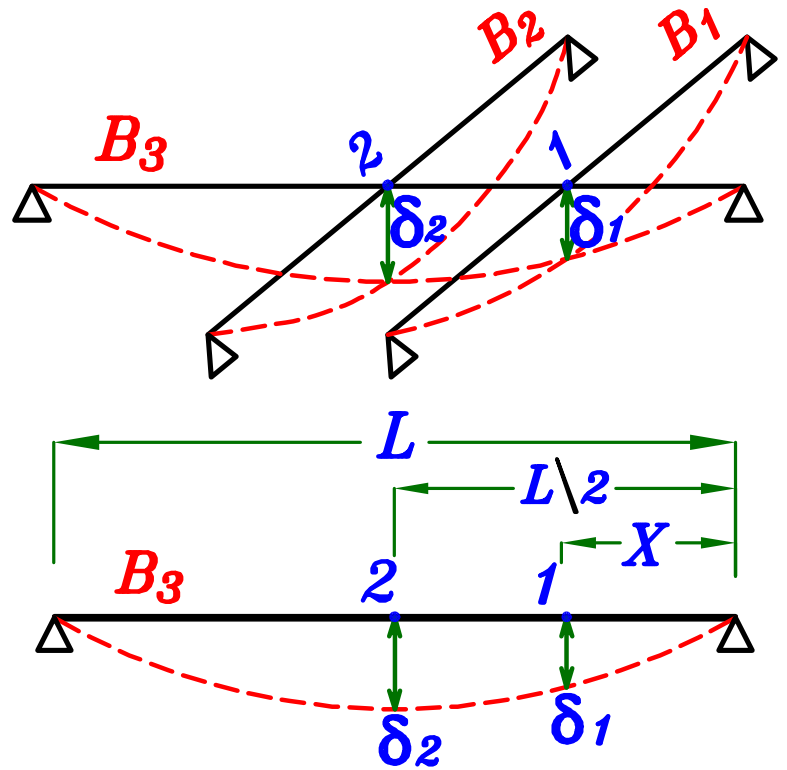
$$M_2 = w * \frac{L^2}{8} \text{ --- لا يوجد لها Reduction Factor لانها فى المنتصف تماما ---}$$

$$M_1 = w * \frac{L^2}{8} * \text{Reduction Factor}$$

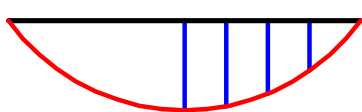
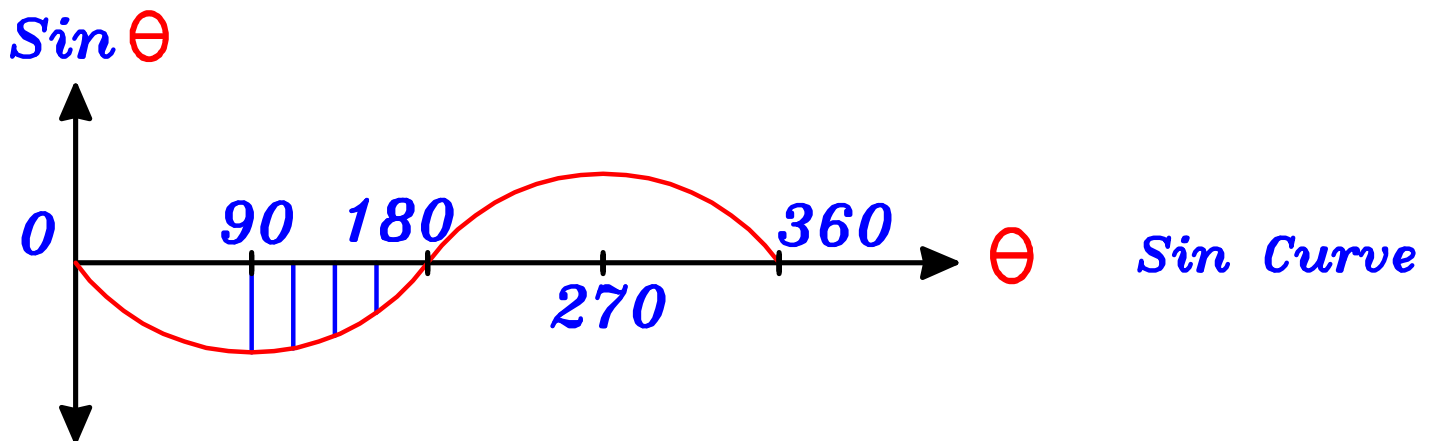
Where $\text{Reduction Factor} = \left(\frac{\delta_1}{\delta_2}\right)$

و لحساب قيمه ال **Reduction Factor** للكمرة **B₁** يساوى $\left(\frac{\delta_1}{\delta_2}\right)$

نحتاج لحساب النسبة $\left(\frac{\delta_1}{\delta_2}\right)$ من شكل ال **Deflection** للكمرة **B₃** (الكمرة العمودية على الكمره المطلوبه)



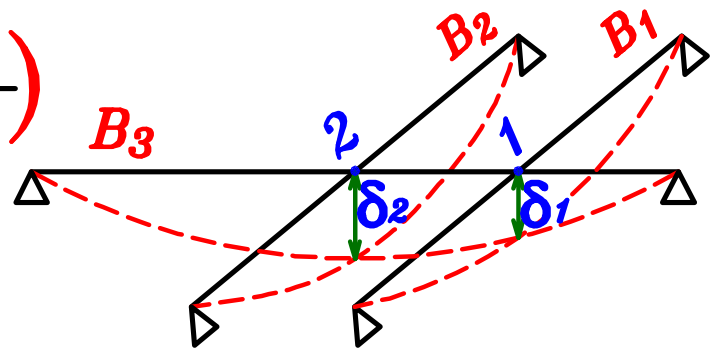
وجد ان شكل ال **Sin Curve** يشبه تماما شكل ال **Deflection Curve** للكمرات ال **Simple**



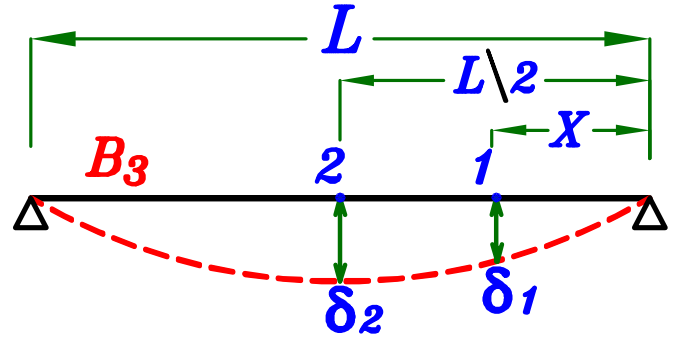
Deflection Curve For Simple Beam

To Calculate

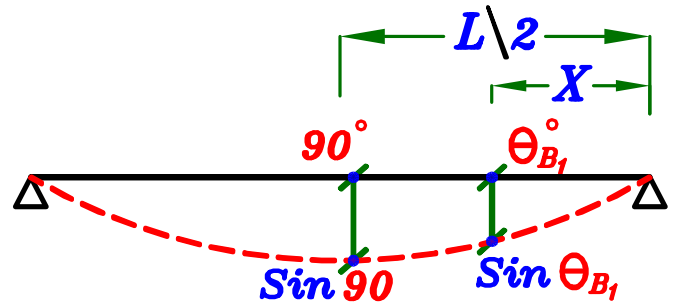
The Reduction Factor = $\left(\frac{\delta_1}{\delta_2}\right)$



Deflection Curve



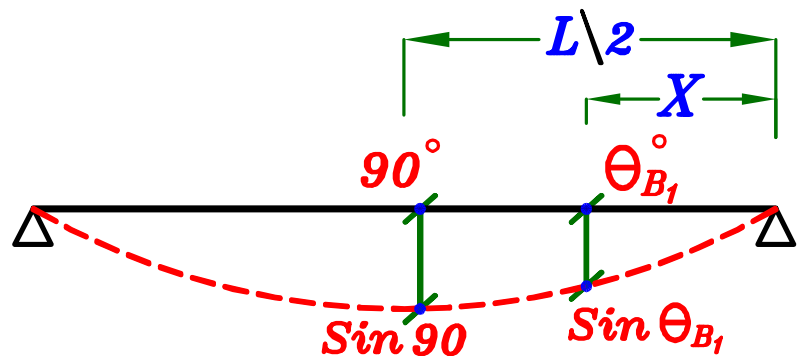
Sin. Curve



$$\therefore \text{Reduction Factor} = \left(\frac{\delta_1}{\delta_2}\right) = \frac{\sin \theta_{B_1}}{\sin 90}$$

To Calculate θ_{B_1}

$$\frac{\theta_{B_1}}{90} = \frac{X}{L/2}$$

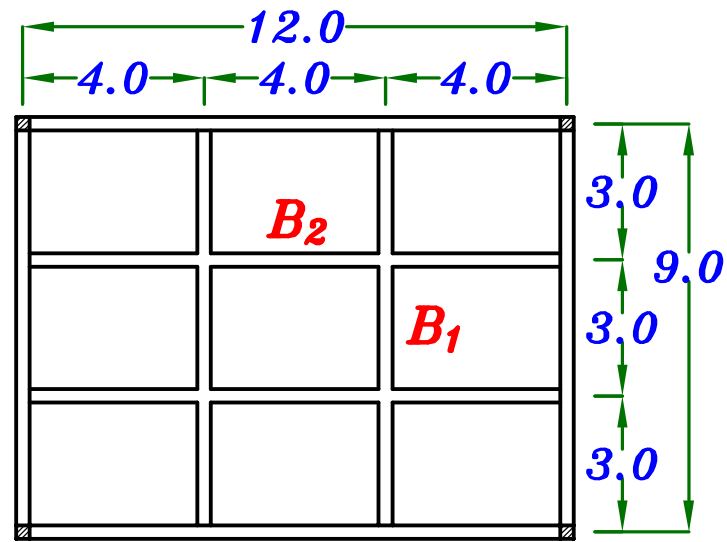


Sin. Curve

$$\therefore \theta_{B_1} = \frac{X}{(L/2)} * 90^\circ$$

Examples.

Calculate the
Reduction Factor
For Beams B_1, B_2

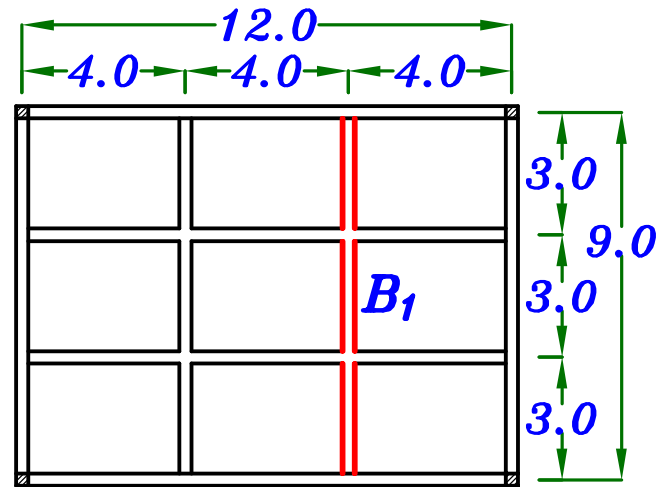


B_1

$$X = 4.0 \text{ m} , \quad \frac{L}{2} = \frac{12.0}{2} = 6.0 \text{ m}$$

$$\Theta_{B_1} = \frac{4.0}{6.0} * 90^\circ = 60^\circ$$

$$M_1 = w_1 * \frac{9^2}{8} * \frac{\sin 60^\circ}{\sin 90^\circ}$$



ملحوظه ممكن اخذ $X = 8.0 \text{ m}$ بدلا من 4.0 m

$$\Theta_{B_1} = \frac{8.0}{6.0} * 90^\circ = 120^\circ \text{ فتكون قيمه}$$

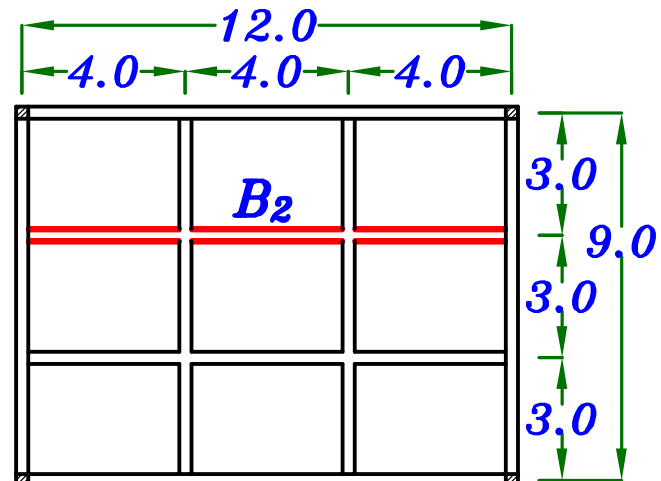
فتكون نفس النتيجة لان $\sin 60^\circ = \sin 120^\circ$

B_2

$$X = 3.0 \text{ m} , \quad \frac{L}{2} = \frac{9.0}{2} = 4.5 \text{ m}$$

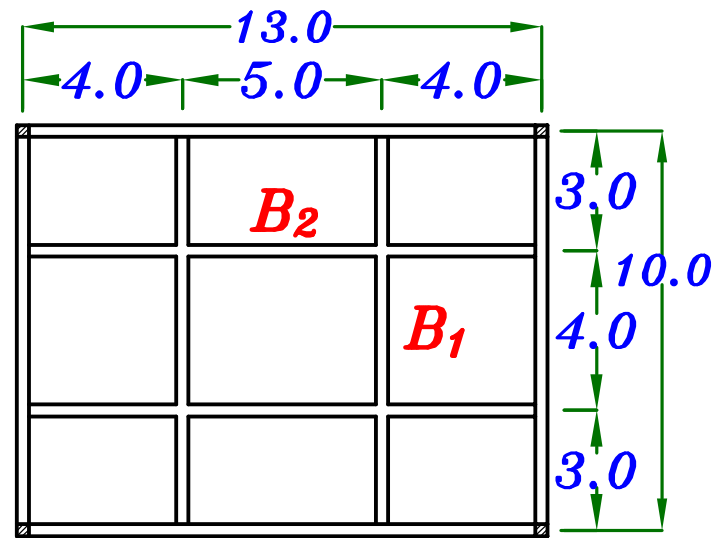
$$\Theta_{B_2} = \frac{3.0}{4.5} * 90^\circ = 60^\circ$$

$$M_2 = w_2 * \frac{12^2}{8} * \frac{\sin 60^\circ}{\sin 90^\circ}$$



Examples.

Calculate the
Reduction Factor
For Beams B_1, B_2

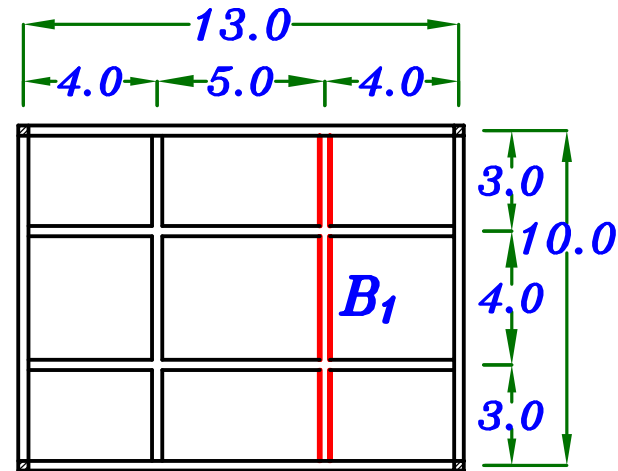


B_1

$$X = 4.0 \text{ m} , \quad \frac{L}{2} = \frac{13.0}{2} = 6.5 \text{ m}$$

$$\Theta_{B_1} = \frac{4.0}{6.5} * 90^\circ = 55.38^\circ$$

$$M_1 = w_1 * \frac{10^2}{8} * \frac{\sin 55.38^\circ}{\sin 90^\circ}$$

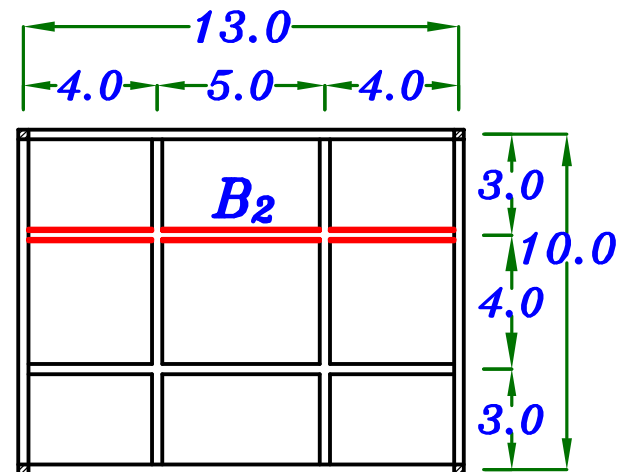


B_2

$$X = 3.0 \text{ m} , \quad \frac{L}{2} = \frac{10.0}{2} = 5.0 \text{ m}$$

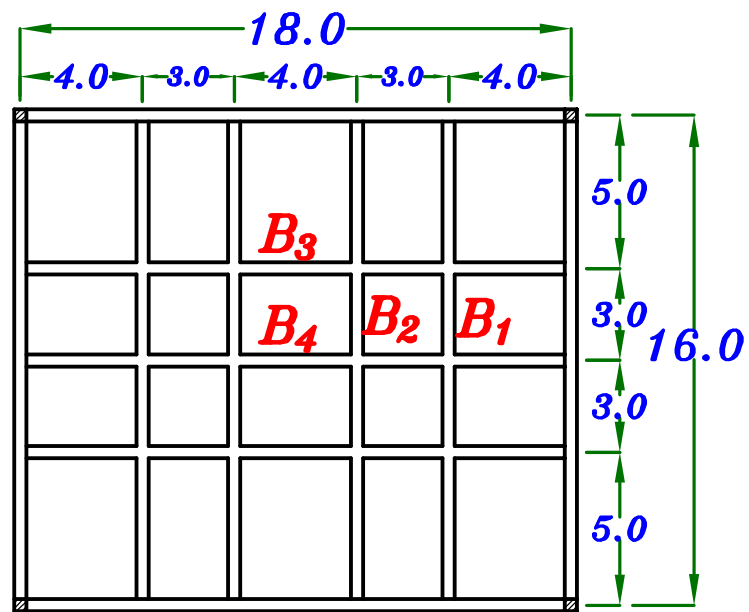
$$\Theta_{B_2} = \frac{3.0}{5.0} * 90^\circ = 54.0^\circ$$

$$M_2 = w_2 * \frac{13^2}{8} * \frac{\sin 54.0^\circ}{\sin 90^\circ}$$



Examples.

Calculate the
Reduction Factor For
Beams B_1, B_2, B_3 & B_4

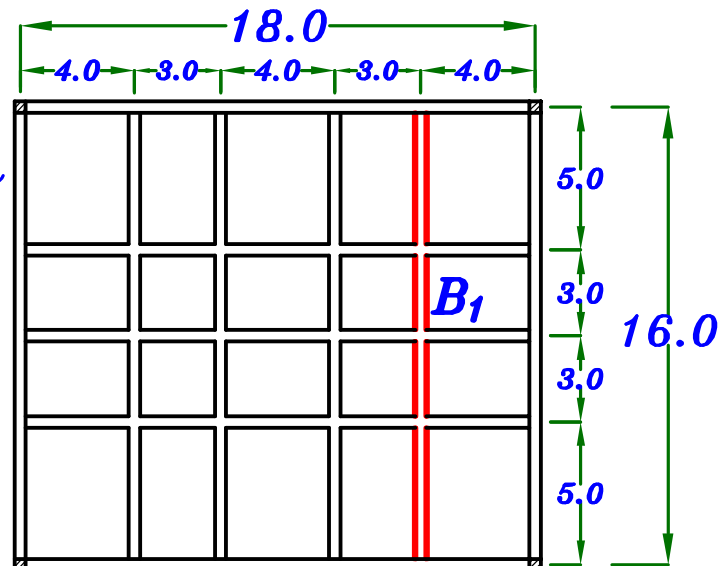


B_1

$$X = 4.0 \text{ m} , \frac{L}{2} = \frac{18.0}{2} = 9.0 \text{ m}$$

$$\Theta_{B_1} = \frac{4.0}{9.0} * 90^\circ = 40^\circ$$

$$M_1 = w_1 * \frac{16^2}{8} * \frac{\sin 40^\circ}{\sin 90^\circ}$$

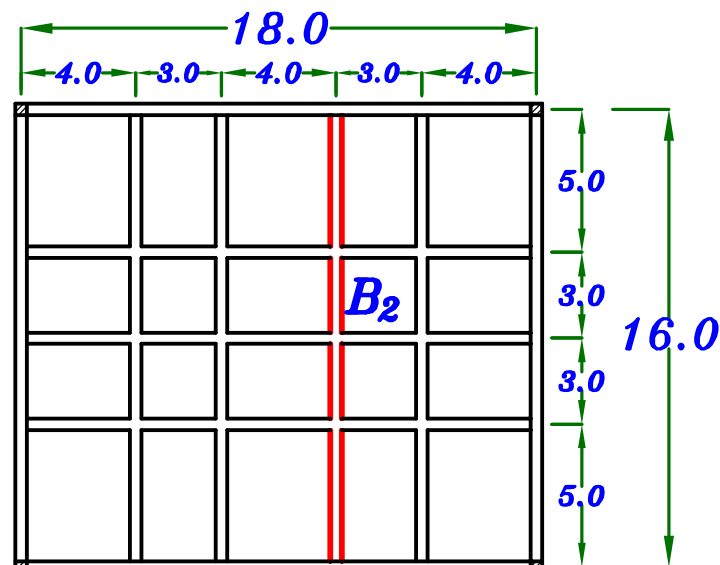


B_2

$$X = 7.0 \text{ m} , \frac{L}{2} = \frac{18.0}{2} = 9.0 \text{ m}$$

$$\Theta_{B_2} = \frac{7.0}{9.0} * 90^\circ = 70^\circ$$

$$M_2 = w_2 * \frac{16^2}{8} * \frac{\sin 70^\circ}{\sin 90^\circ}$$

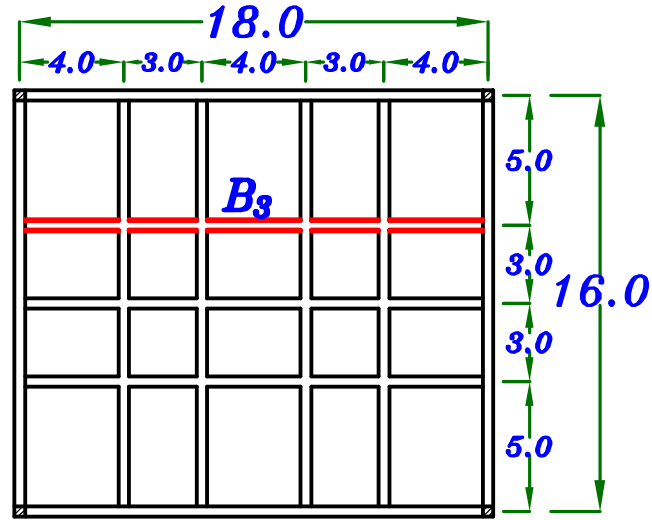


B_3

$$X = 5.0 \text{ m} , \frac{L}{2} = \frac{16.0}{2} = 8.0 \text{ m}$$

$$\theta_{B_3} = \frac{5.0}{8.0} * 90^\circ = 56.25^\circ$$

$$M_3 = w_3 * \frac{18^2}{8} * \frac{\sin 56.25^\circ}{\sin 90^\circ}$$

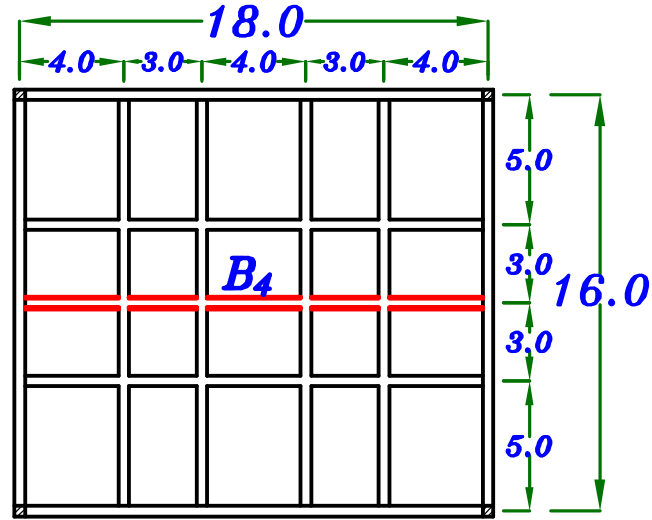


B_4

$$X = 8.0 \text{ m} , \frac{L}{2} = \frac{16.0}{2} = 8.0 \text{ m}$$

$$\theta_{B_4} = \frac{8.0}{8.0} * 90^\circ = 90^\circ$$

$$M_4 = w_4 * \frac{18^2}{8} * \frac{\sin 90^\circ}{\sin 90^\circ}$$



ملحوظه

إذا كانت الكمره فى منتصف البحر تماما ستكون $\theta = 90^\circ$ أى أن $\frac{\sin \theta}{\sin 90} = 1.0$

أى لا يوجد **Reduction Factor** فتكون قيمه ال **moment** كبيره

أى أنه لم يتم الاستفاده من ال **Grid Action** فى تقليل ال **moment**

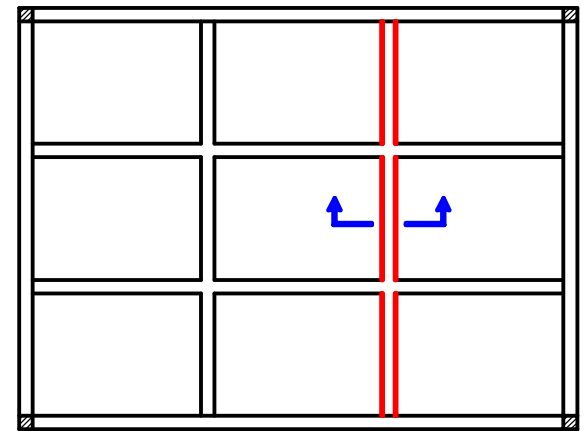
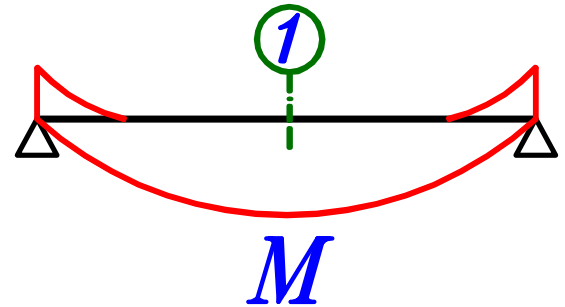
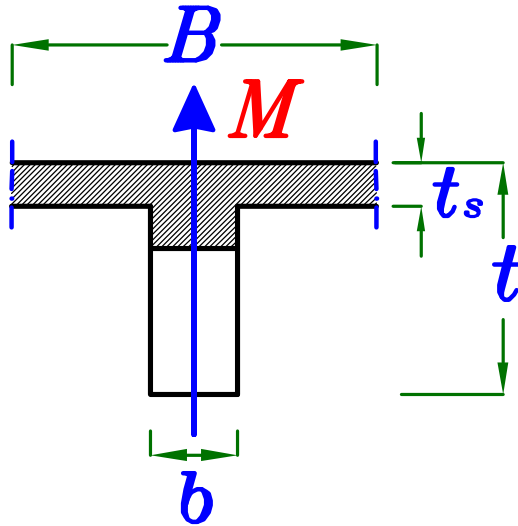
F – Design the Beam.

Take the cover = 50 mm

α Direction

Take the cover = 70 mm

β Direction



Design the Sec. as **T-Sec.**

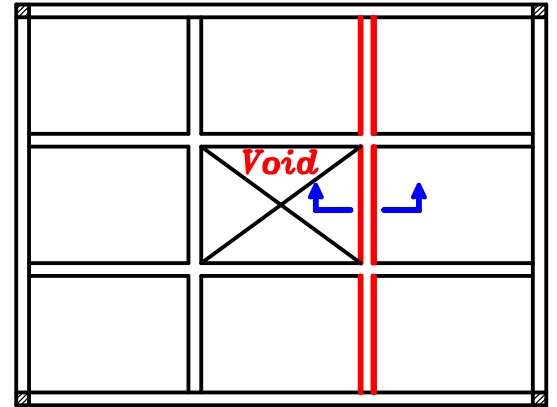
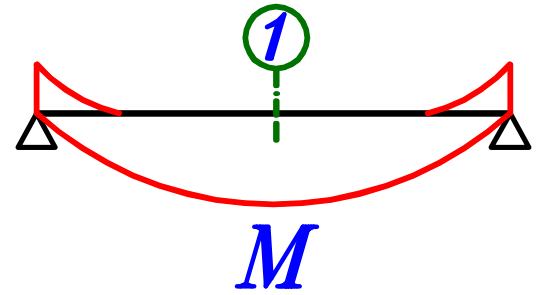
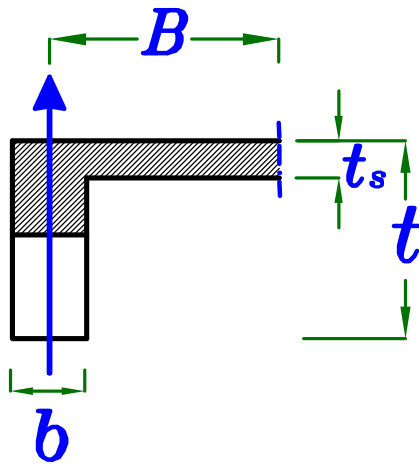
$$B = \begin{cases} C.L. \rightarrow C.L. (a \text{ or } b) \\ 16 t_s + b \\ K \frac{L}{5} + b \quad (K = 1.0) \end{cases}$$

$$d = t - \text{Cover} = \checkmark$$

$$d = C_1 \sqrt{\frac{M_{u.l.}}{F_{cu} * B}} \rightarrow C_1 = \checkmark \rightarrow J = \checkmark$$

$$A_s = \frac{M_{u.l.}}{J F_y d} = \checkmark \text{ mm}^2$$

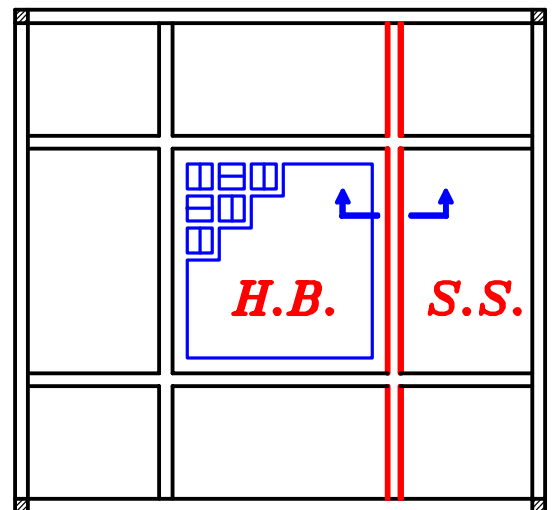
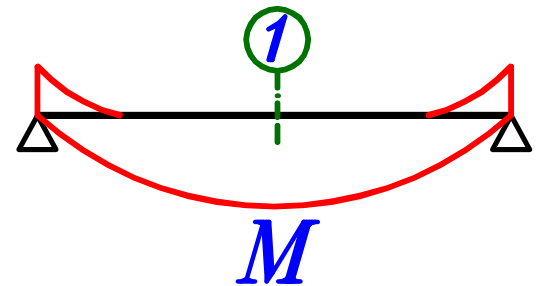
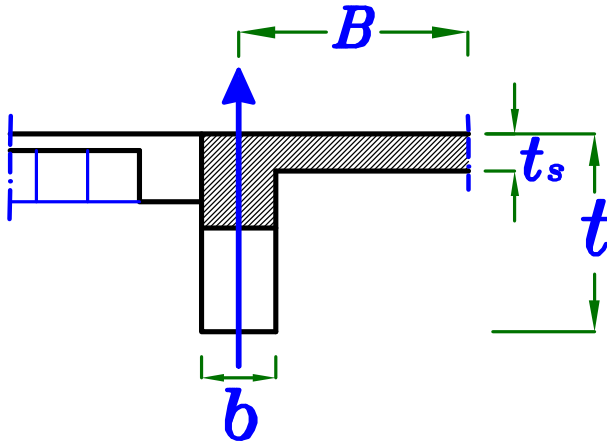
IF There is a Void.



Design the Sec. as **L-Sec.**

$$B = \begin{cases} C.L. \rightarrow C.L. \left(\frac{a}{2} \text{ or } \frac{b}{2} \right) \\ 6 t_s + b \\ K \frac{L}{10} + b \quad (K = 1.0) \end{cases}$$

IF There is a Solid & Hollow Blocks.

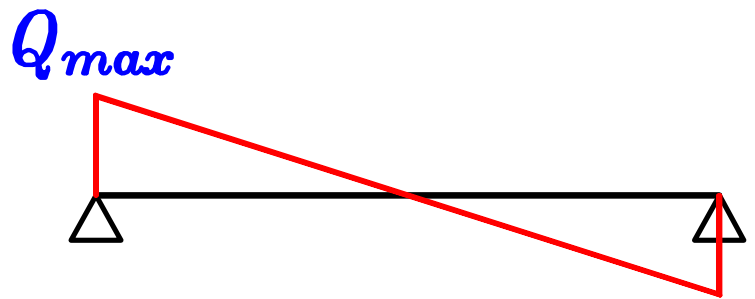


Design the Sec. as **L-Sec.**

$$B = \begin{cases} C.L. \rightarrow C.L. \left(\frac{a}{2} \text{ or } \frac{b}{2} \right) \\ 6 t_s + b \\ K \frac{L}{10} + b \quad (K = 1.0) \end{cases}$$

يفضل تصميم القطاع على انه **L-Sec.** من جهة ال **Solid Slab** فقط.

Check Shear.



* Allowable Shear Stresses.

$$q_{cu} = (0.24) \sqrt{\frac{F_{cu}}{\delta_c}} \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{F_{cu}}{\delta_c}} \text{ N/mm}^2$$

* Actual Shear Stress.

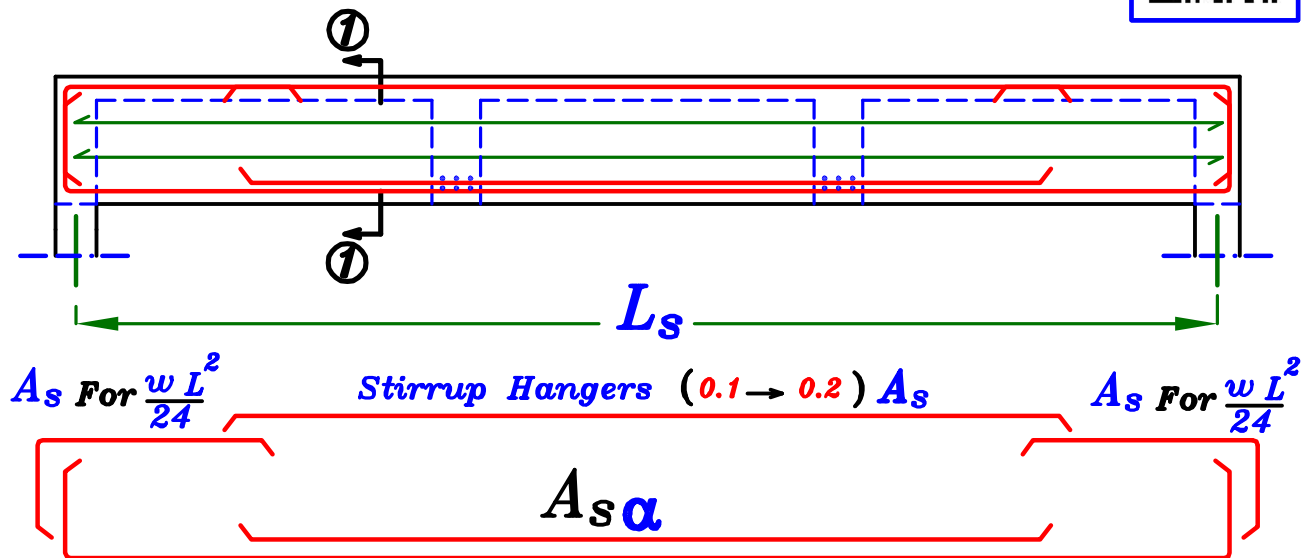
$$q_s = \frac{Q_{max}}{b d} \quad (\text{N/mm}^2)$$

1- IF $q_s < q_{cu}$ \longrightarrow Use min. Shear RFT. $5\phi 8 \text{ m}$

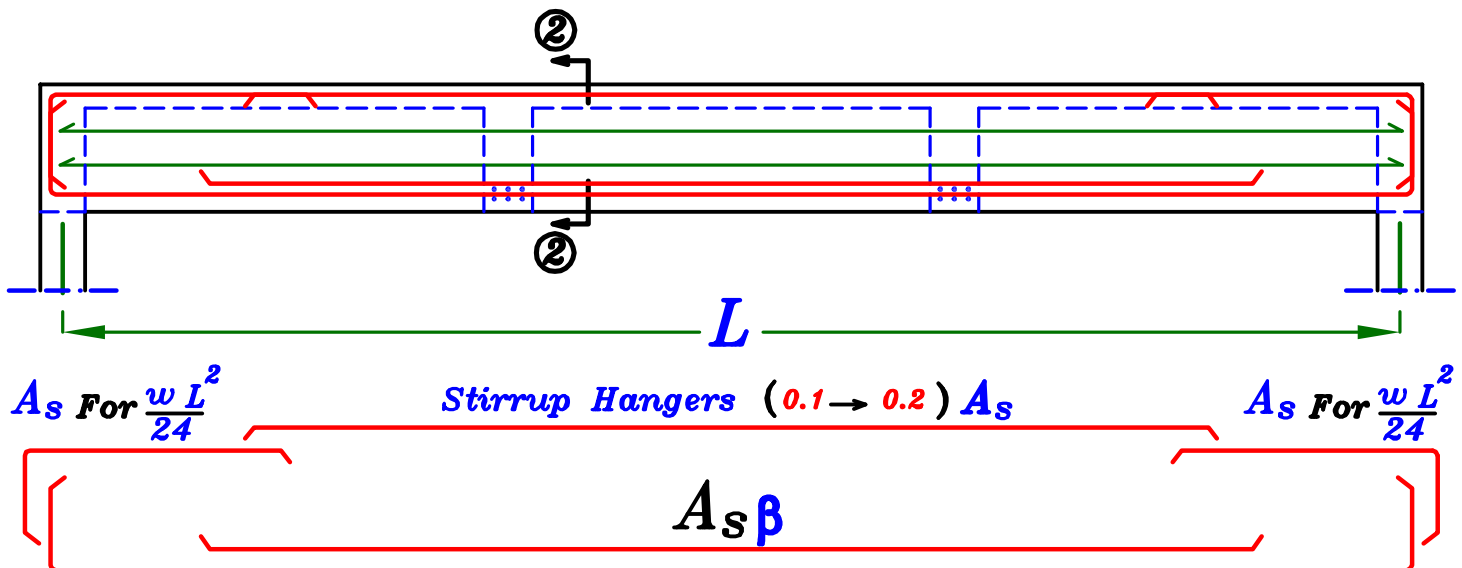
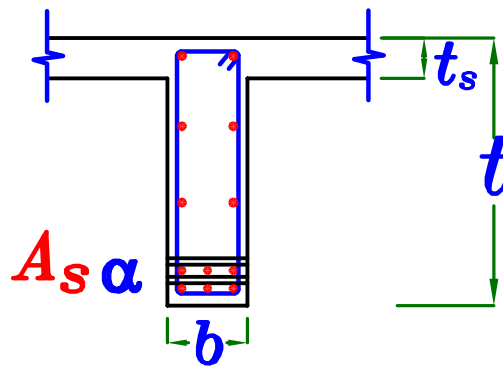
2- IF $q_s > q_{u_{max}}$ \longrightarrow Increase Dimensions (b or d)

3- IF $q_{cu} < q_s < q_{u_{max}}$ \longrightarrow
$$q_s - \frac{q_{cu}}{2} = \frac{n A_s (F_y \delta_s)}{b S}$$

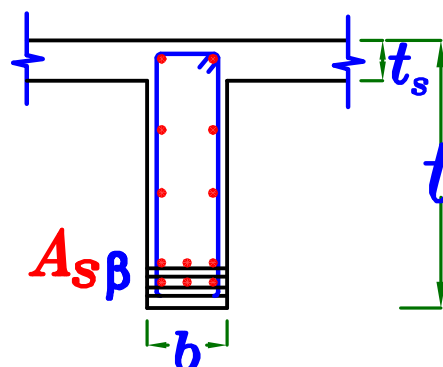
g – Draw Details of RFT. For the Beams.



Sec. (1-1)



Sec. (2-2)



③ Design of the Edge Beam. (Exterior Beam)

الكمرات الخارجيه محموله على أعمده أى انها محموله على **Rigid Support**

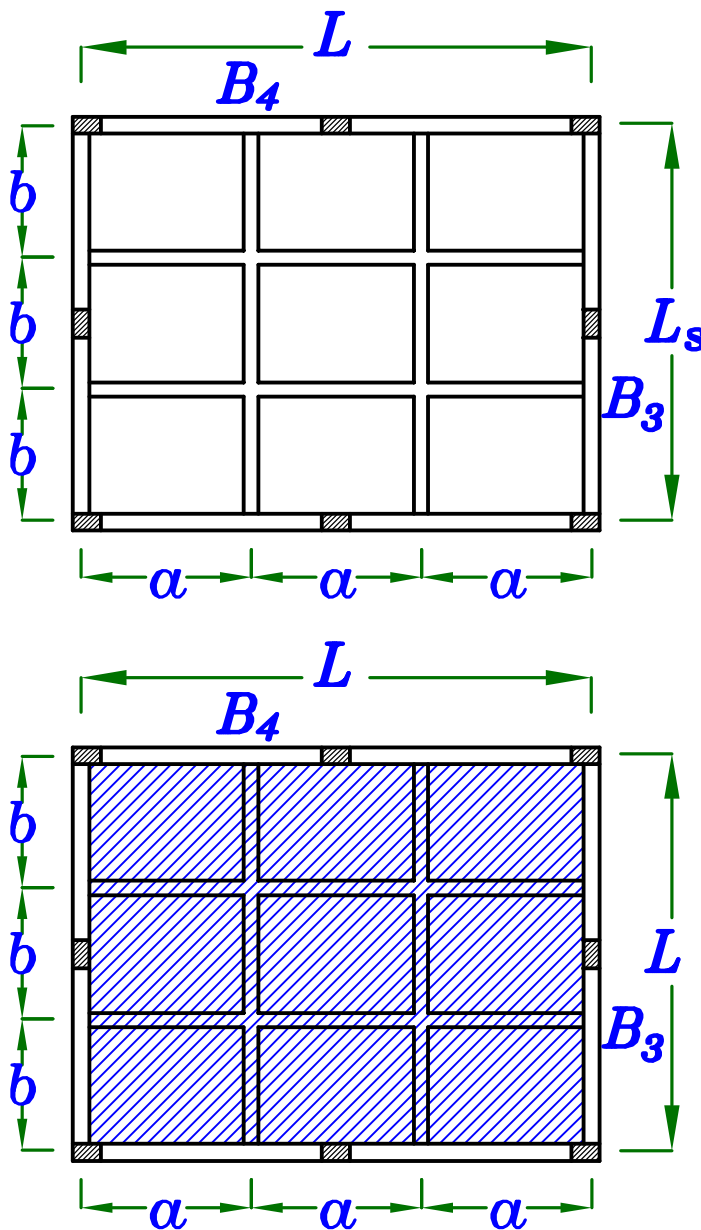
و ليست موجوده فى شبكه لذا لا يوجد بها **Reduction Factor**

و ممكن حساب الاحمال عليها عن طريق **Load Distribution**

و يتم تصميم الكمرات الخارجيه على ال **Shear & moment**

و لحساب الاحمال على الكمرات الخارجيه توجد حالتان :

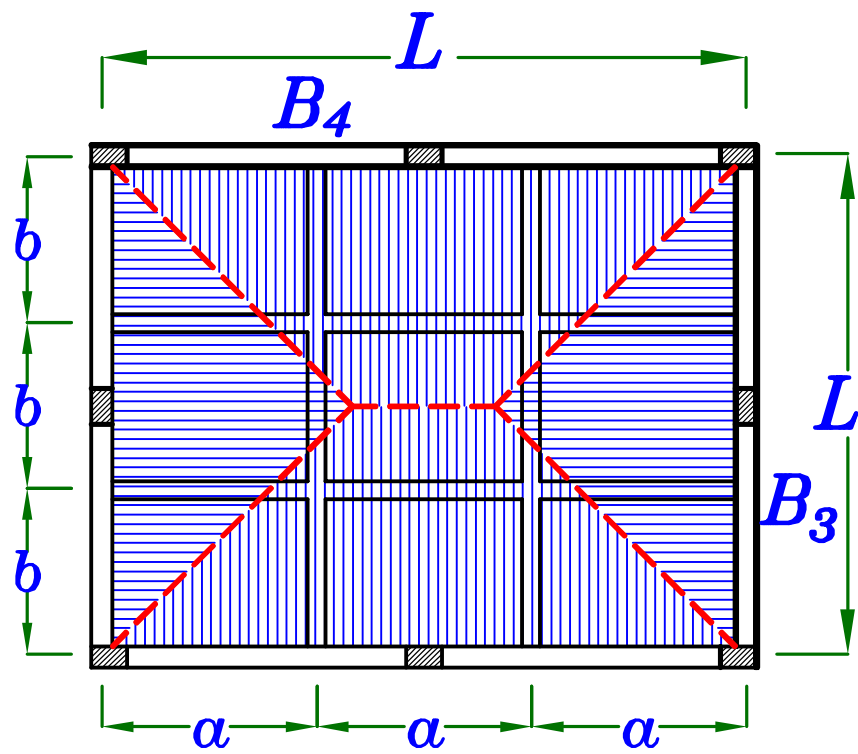
١- اذا كانت كل الكمرات ال **Panelled** محموله على الكمرات الخارجيه فقط.



ممكن استخدام حل **approximate**

و ذلك بأستخدام w_{av} لحساب الوزن

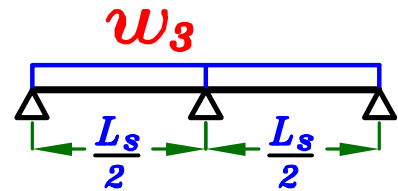
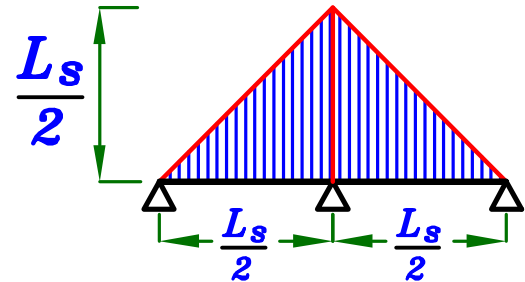
كأنها بلاطه كبيره أبعادها $(L * L_s)$



B₃

$$w_3 = (\text{o.w.})_{\text{beam}} + \frac{\sum \text{area}}{\text{span}} (w_{av.})$$

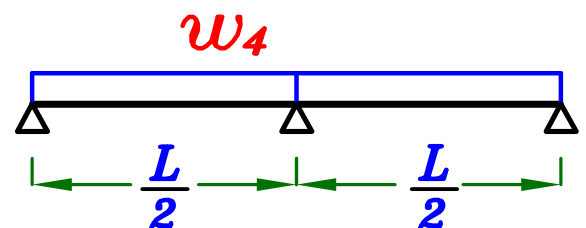
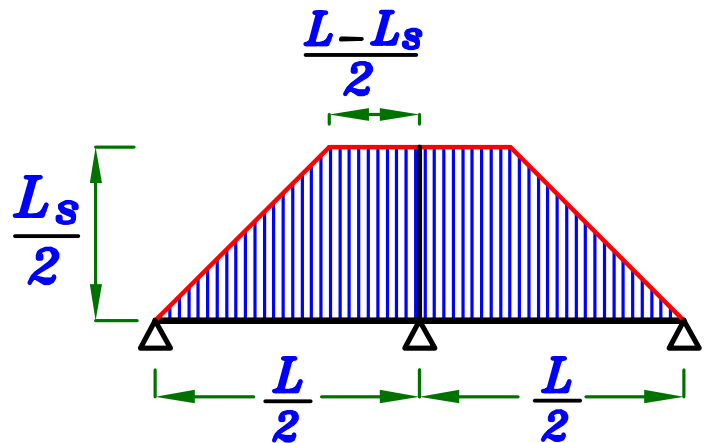
$$\frac{\sum \text{area}}{\text{span}} = \frac{\left(0.5 * \frac{L_s}{2} * \frac{L_s}{2}\right)}{L_s}$$



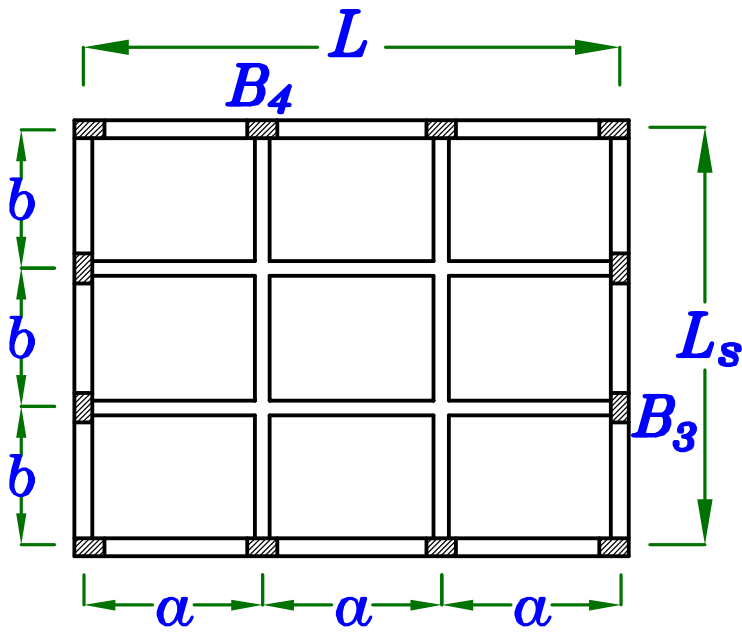
B₄

$$w_4 = (\text{o.w.})_{\text{beam}} + \frac{\sum \text{area}}{\text{span}} (w_{av.})$$

$$\frac{\sum \text{area}}{\text{span}} = \frac{\left[\left(\frac{L}{2} + \frac{L-L_s}{2} \right) * \frac{L_s}{2} \right]}{\left(\frac{L}{2} \right)}$$



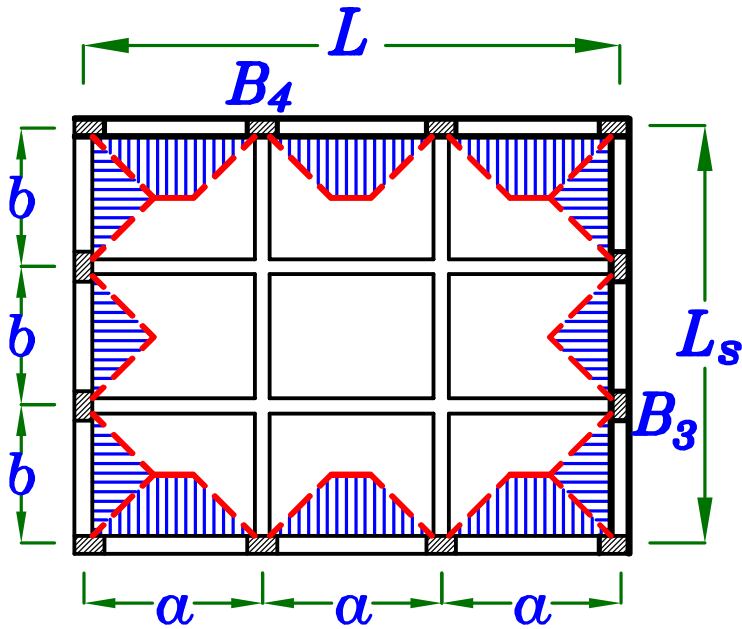
٢- اذا كانت كل الكمرات ال *Panelled* محمولة على الاعمده .



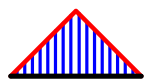
أى ان وزن الكمرات ال *Panelled* يذهب مباشرة على الاعمده و لن يحمل على الكمرات الخارجيه .

لذا لن نستطيع ان نحسب الاحمال على الكمرات الخارجيه عن طريق w_{av}

بل يجب ان نستخدم w_s

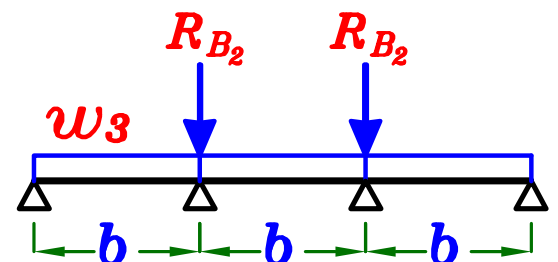
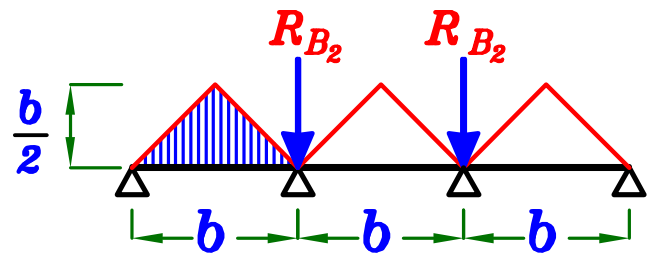


B_3



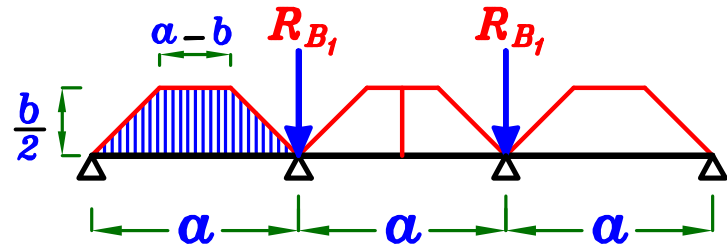
$$w_3 = (o.w.)_{beam} + \frac{C_a}{C_e} (w_s) \left(\frac{b}{2} \right)$$

Solve it using Empirical Values

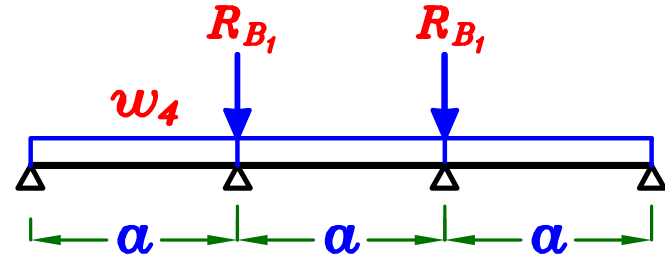


B_4

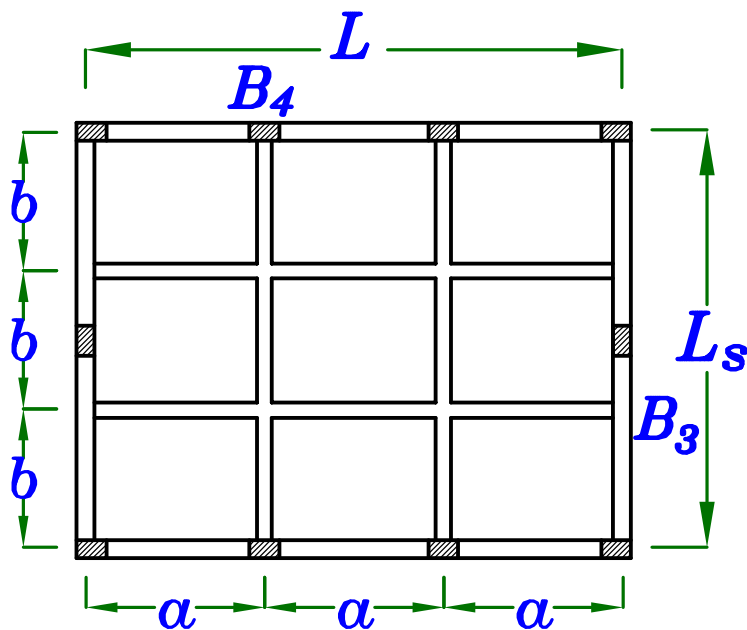
$$w_4 = (o.w.)_{beam} + \frac{C_a}{C_e} (w_s) \left(\frac{b}{2} \right)$$



Solve it using Empirical Values



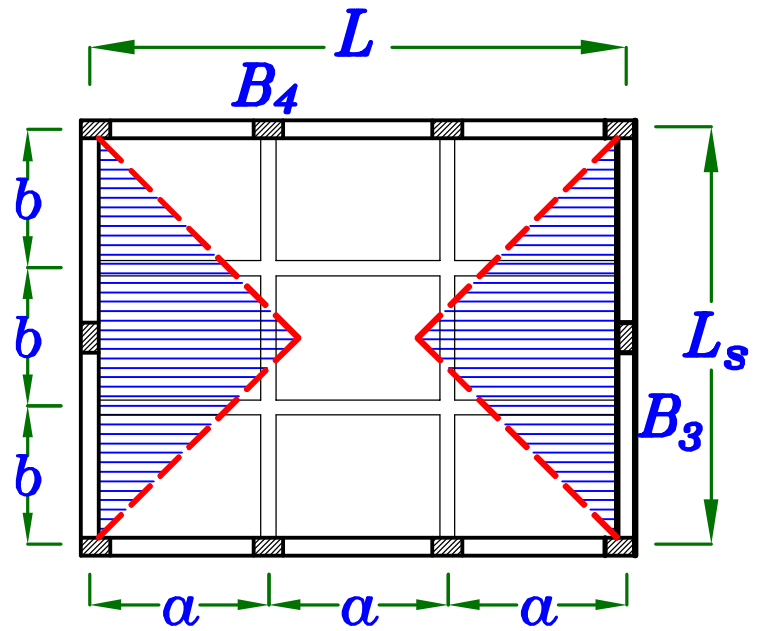
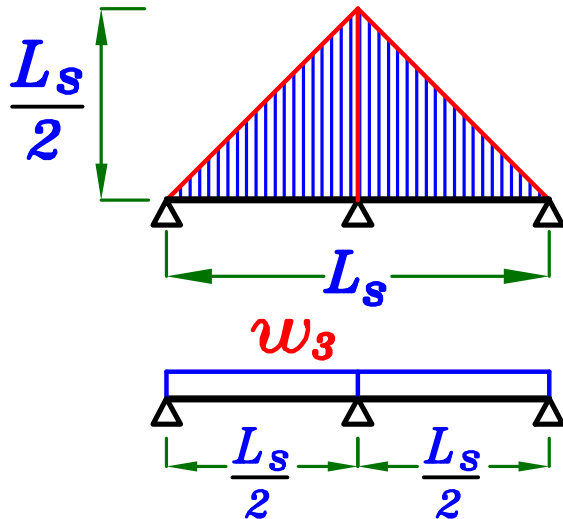
Special Case.



إذا وجد اتجاه الكمرات ال **panelled**
محمولة على الكمرات الخارجيه
و الاتجاه الاخر محموله على اعمده .

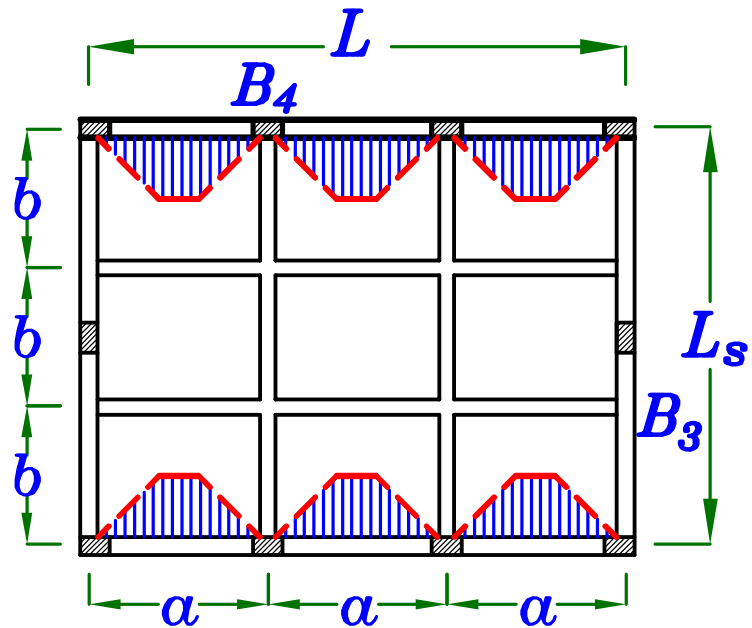
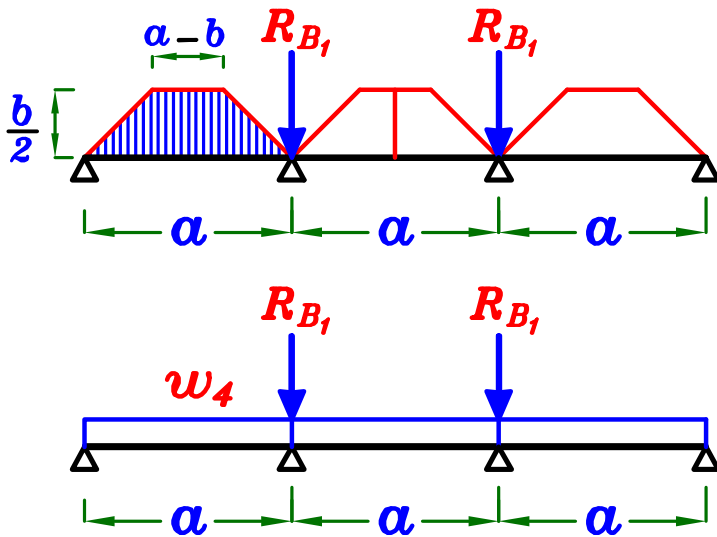
يمكن للتسهيل عند حساب الاحمال
اتجاه نحسبه بالطريقه ال **approximate**
أى بأستخدام w_{av} لحساب الوزن .
و الاتجاه الاخر بالطريقه ال **exact**
أى بأستخدام w_s لحساب الوزن .

B₃



$$w_3 = (\text{o.w.})_{\text{beam}} + \frac{\sum \text{area}}{\text{span}} (w_{av.})$$

B₄

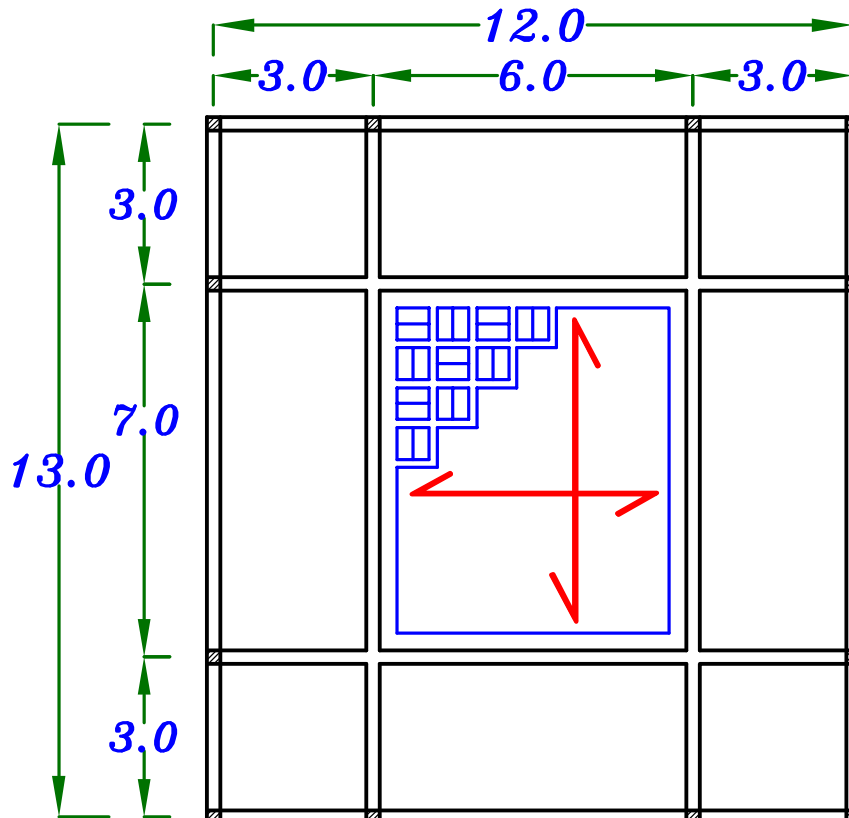
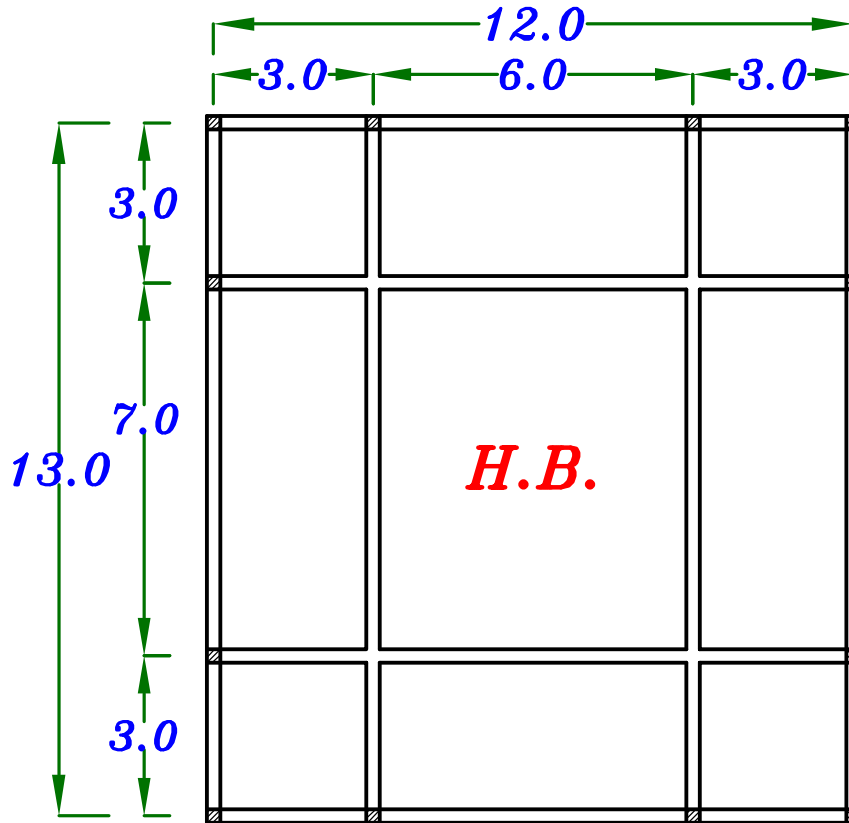


$$w_4 = (\text{o.w.})_{\text{beam}} + \frac{C_a}{C_e} (w_s) \left(\frac{b}{2} \right)$$

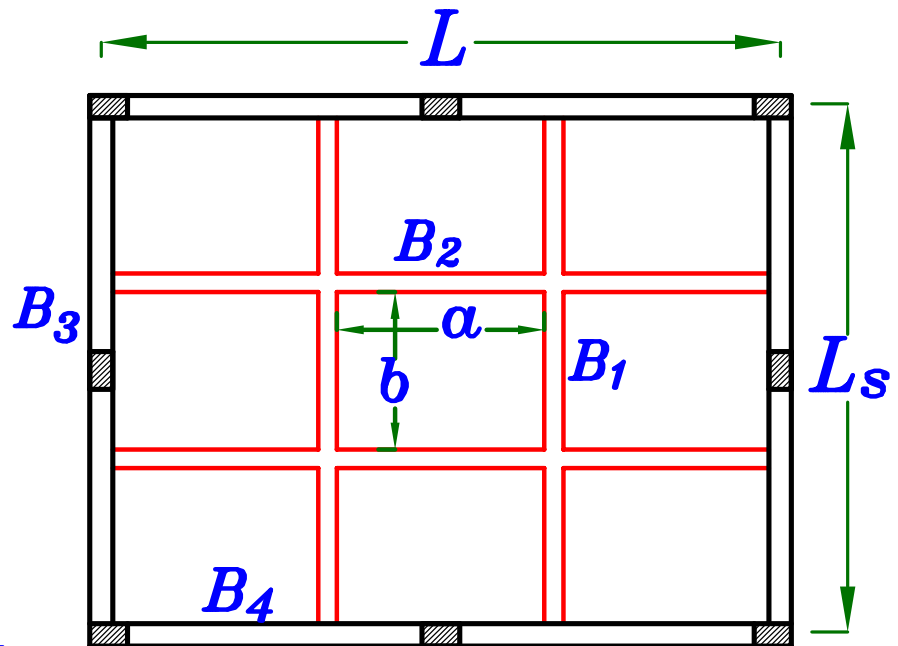
Solve it using Empirical Values

Note.

إذا وجدت بلاطات **Hollow Blocks** محمولة على **Panelled Beams** يجب أن تكون البلاطة الوسطى **Two way Hollow Blocks** حتى يتوزع الحمل على الكمرات الـ **Panelled** تقريبا بالتساوي



Panelled Beams General Examples.



Steps of Design.

- ① **Design the slabs.** (Two way slab يفضل أن تكون) (Solid or Hollow Blocks Slabs) ($a * b$)

a– Choose the Thickness of the Slab (t_s).

b– Get the Loads on the Slab (w_s).

c– Get the Load Factors α, β .

d– Take a strips in the slab (at the Load direction)

And then Get (B.M.) on the Slab & Design the slab.

e– Draw Details of RFT. of the slab in plan.

- ② **Design the Panelled Beams.** (B_1, B_2)

a– Get the Dimensions of the beam. (b, t).

b– Get the average Load on the Slab. (w_{av}).

c– Calculate α, β (For the hall area) By using Grashoff.

d– Get the Loads on the Panelled Beam & Calculate the B.M.

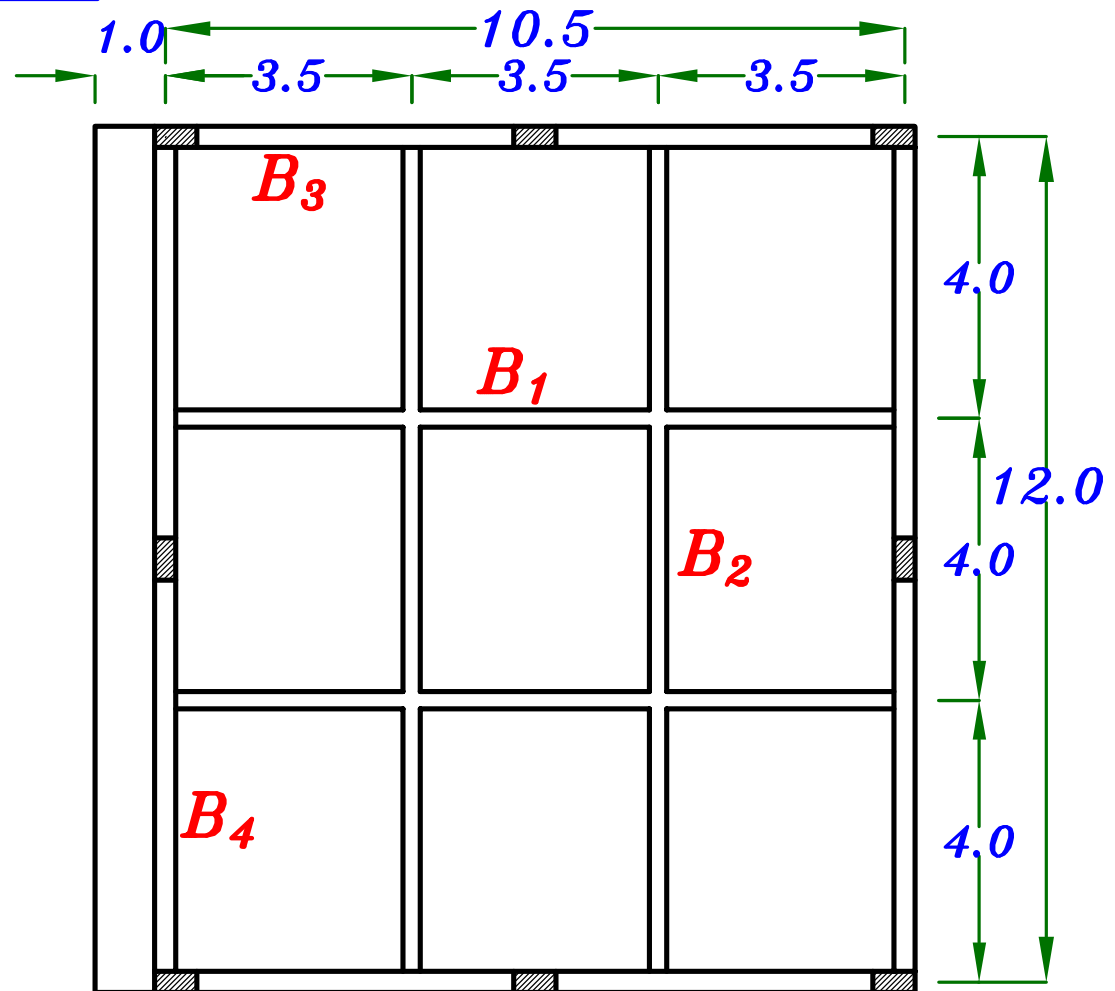
e– Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

f– Design the Panelled Beam.

g– Draw Details of RFT. For the Panelled Beams.

- ③ **Design the Edge Beams.**
(The Exterior Beam) (B_3, B_4)

Example.



Data.

$$F_{cu} = 25 \text{ N/mm}^2$$

$$F_y = 360 \text{ N/mm}^2$$

$$F.C. = 1.5 \text{ kN/m}^2$$

$$L.L. = 4.0 \text{ kN/m}^2$$

Req.

- ① Design the Slabs **as Solid Slabs.**
- ② Draw Details **of RFT.** of Slabs **in plan.**
- ③ Design Beams **B_1, B_2, B_3, B_4**
- ④ Draw Details **of RFT.** of the beams **in elevation & cross sections.**

① Design the Slabs as Solid Slabs.

a- Choose the Thickness of the Slab. (t_s).

S_1 two way $L_S = 3.5$ m

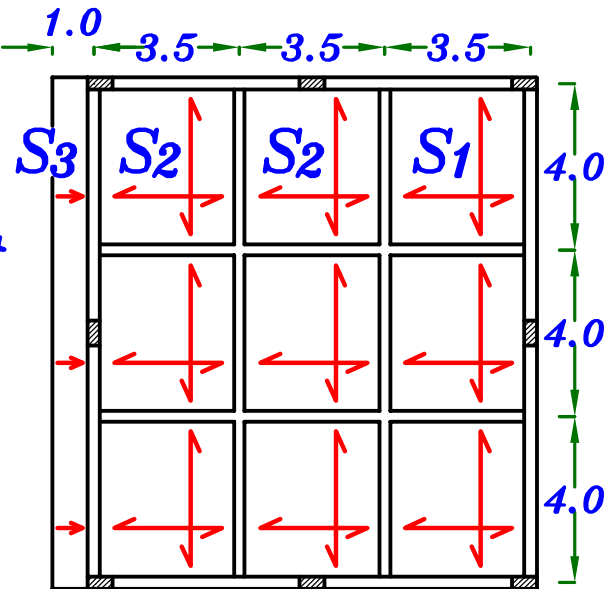
$$t_s = \frac{3500}{40} = 87.5 \text{ mm}$$

S_2 two way $L_S = 3.5$ m

$$t_s = \frac{3500}{45} = 77.7 \text{ mm}$$

S_3 Cantilever $L_C = 1.0$ m

$$t_s = \frac{1000}{10} = 100 \text{ mm}$$



Take (t_s) the bigger value

$$t_s = 100 \text{ mm}$$

b- Get the Loads on the Slab (w_s).

$$w_s = 1.4 (0.10 * 25 + 1.50) + 1.6 (4.0) = 12.0 \text{ kN/m}^2$$

c- Get the Load Factors α , β

$$\alpha = 0.5 r - 0.15$$

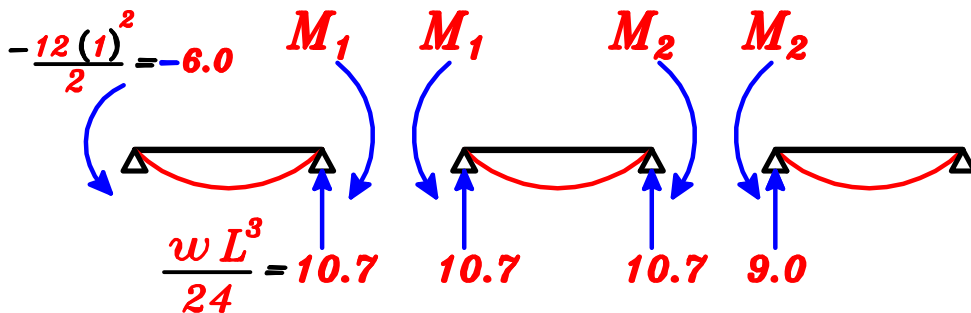
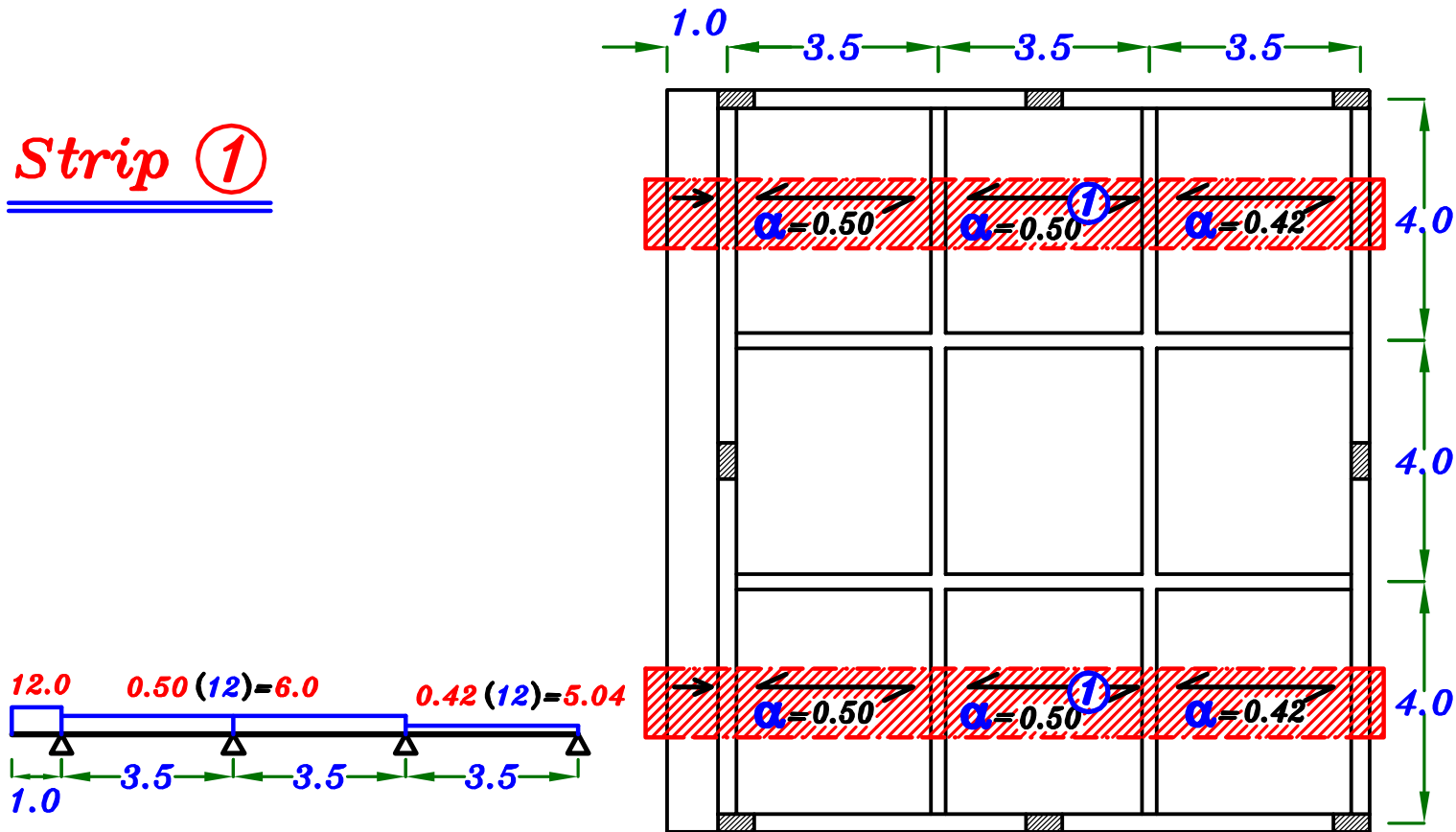
$$\beta = \frac{0.35}{r^2}$$

$r = \frac{0.87(4.0)}{0.76(3.5)}$ $r = 1.30$ $\alpha = 0.50 \rightarrow$ $\beta = 0.20 \uparrow$	$r = \frac{0.87(4.0)}{0.76(3.5)}$ $r = 1.30$ $\alpha = 0.50 \rightarrow$ $\beta = 0.20 \uparrow$	$r = \frac{0.87(4.0)}{0.87(3.5)}$ $r = 1.14$ $\alpha = 0.42 \rightarrow$ $\beta = 0.26 \uparrow$
$r = \frac{0.76(4.0)}{0.76(3.5)}$ $r = 1.14$ $\alpha = 0.42 \rightarrow$ $\beta = 0.26 \uparrow$	$r = \frac{0.76(4.0)}{0.76(3.5)}$ $r = 1.14$ $\alpha = 0.42 \rightarrow$ $\beta = 0.26 \uparrow$	$r = \frac{0.76(4.0)}{0.87(3.5)}$ $r = 1.0$ $\alpha = 0.35 \rightarrow$ $\beta = 0.35 \uparrow$
$r = \frac{0.87(4.0)}{0.76(3.5)}$ $r = 1.30$ $\alpha = 0.50 \rightarrow$ $\beta = 0.20 \uparrow$	$r = \frac{0.87(4.0)}{0.76(3.5)}$ $r = 1.30$ $\alpha = 0.50 \rightarrow$ $\beta = 0.20 \uparrow$	$r = \frac{0.76(4.0)}{0.76(3.5)}$ $r = 1.14$ $\alpha = 0.42 \rightarrow$ $\beta = 0.26 \uparrow$

d - Take a strips in the slab (at the Load direction)

And then Get (B.M.) on the Slab & Design the slab.

Strip ①



$$-6(3.5) + 2M_1(3.5 + 3.5) + M_2(3.5) = -6(10.7 + 10.7)$$

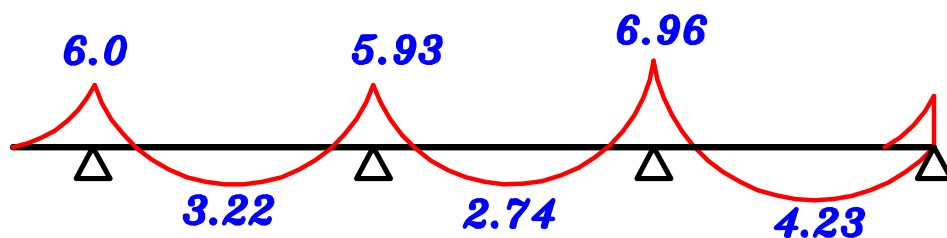
$$14M_1 + 3.5M_2 = -107.4 \quad \text{--- ①}$$

$$M_1(3.5) + 2M_2(3.5 + 3.5) + 0.0 = -6(10.7 + 9.0)$$

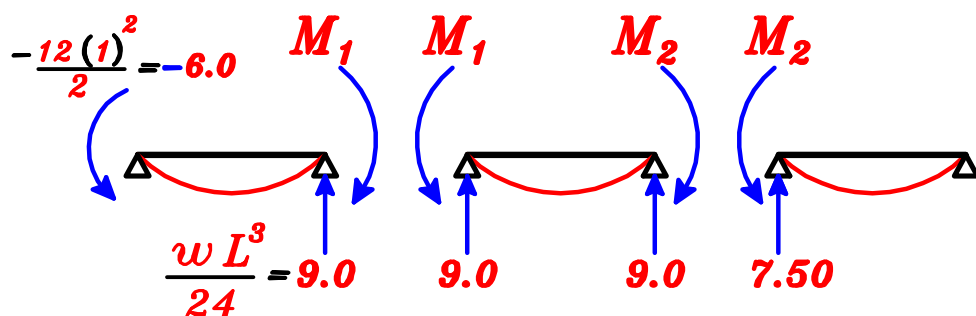
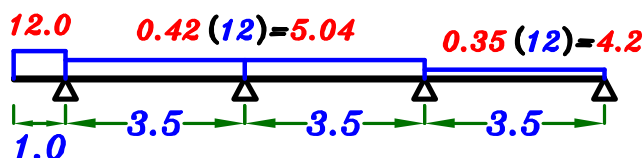
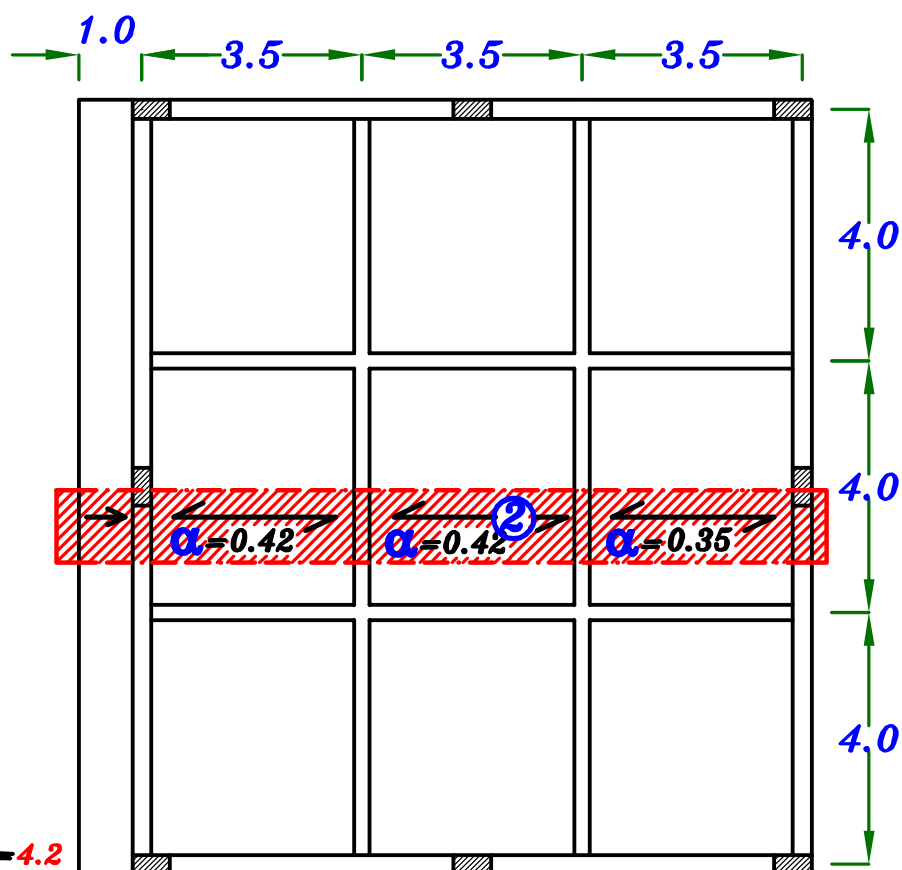
$$3.5M_1 + 14M_2 = -118.2 \quad \text{--- ②}$$

$$M_1 = -5.93 \text{ kN.m}$$

$$M_2 = -6.96 \text{ kN.m}$$



Strip ②



$$-6(3.5) + 2M_1(3.5 + 3.5) + M_2(3.5) = -6(9.0 + 9.0)$$

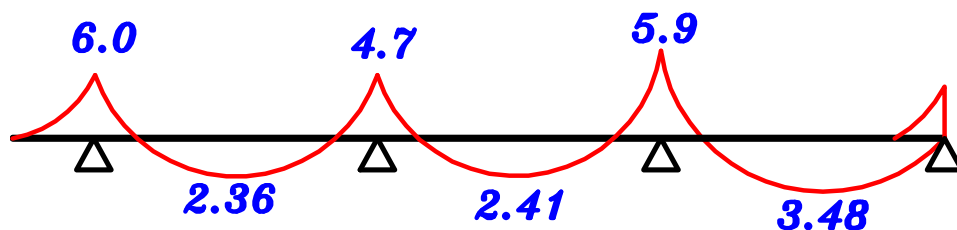
$$14M_1 + 3.5M_2 = -87.0 \quad \text{--- ①}$$

$$M_1(3.5) + 2M_2(3.5 + 3.5) + 0.0 = -6(9.0 + 7.5)$$

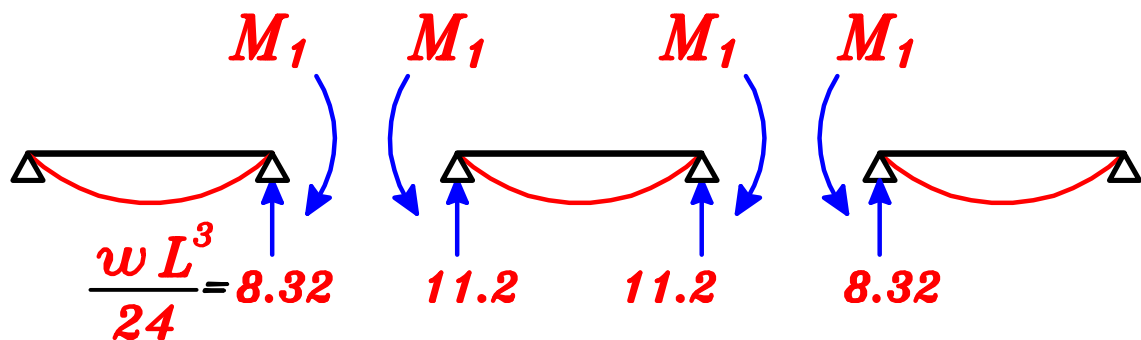
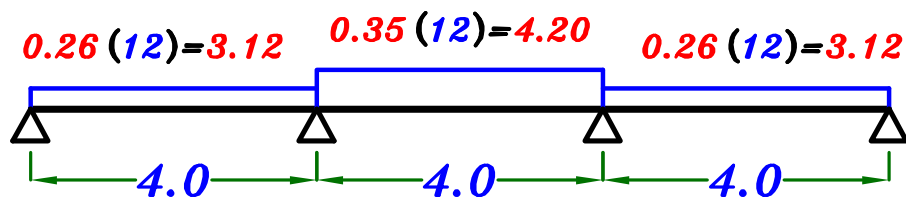
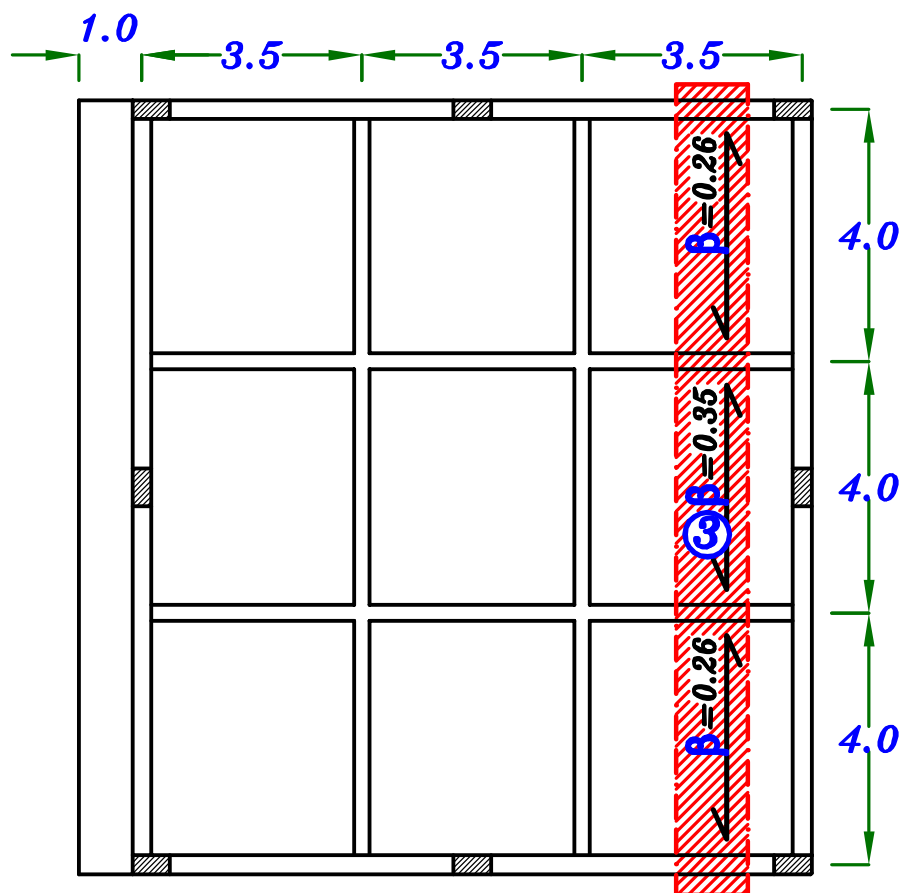
$$3.5M_1 + 14M_2 = -99.0 \quad \text{--- ②}$$

$$M_1 = -4.70 \text{ kN.m}$$

$$M_2 = -5.90 \text{ kN.m}$$

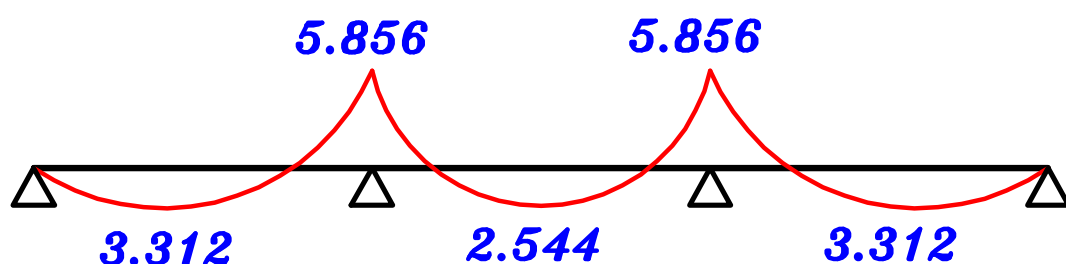


Strip ③

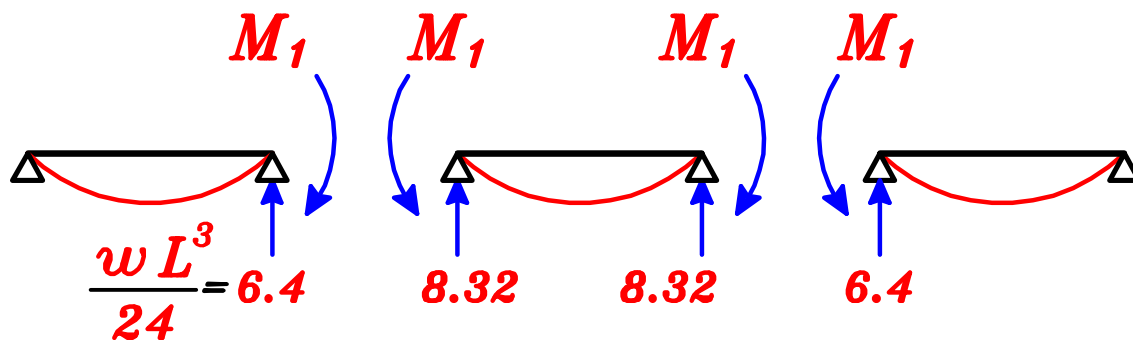
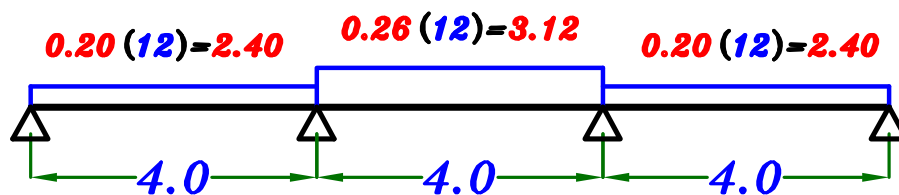
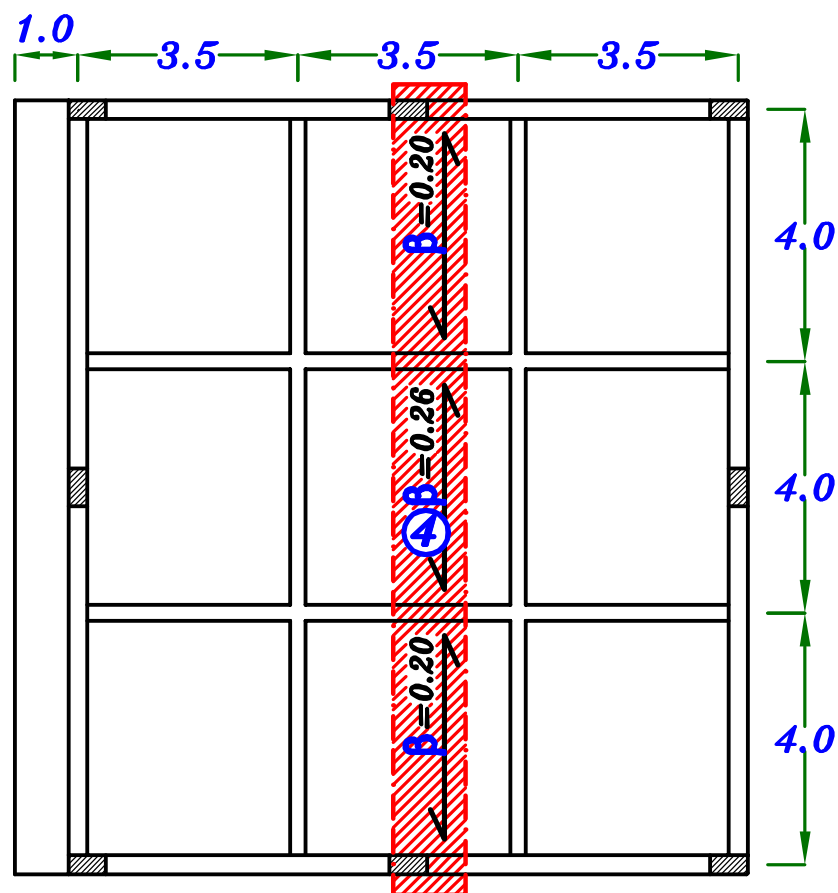


$$0.0 + 2M_1(4.0 + 4.0) + M_1(4.0) = -6(8.32 + 11.2)$$

$$M_1 = -5.856 \text{ kN.m}$$

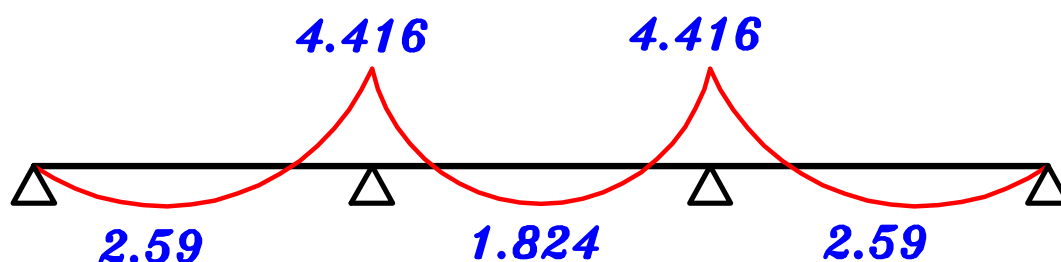


Strip ④

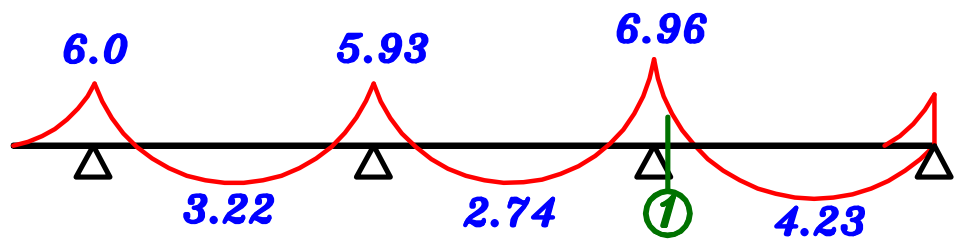


$$0.0 + 2 M_1 (4.0 + 4.0) + M_1 (4.0) = -6 (6.4 + 8.32)$$

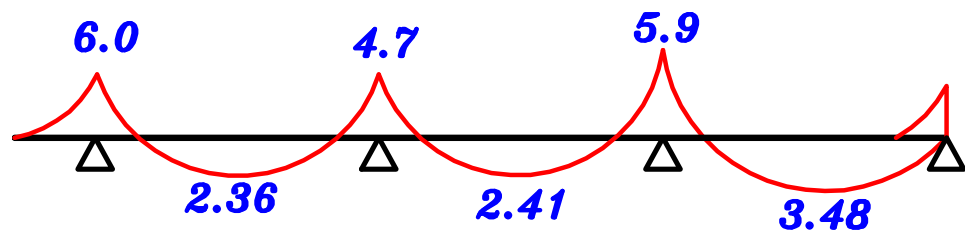
$$M_1 = -4.416 \text{ kN.m}$$



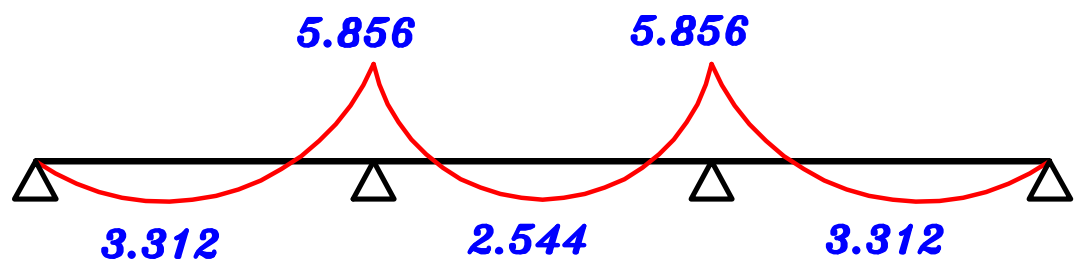
Strip ①



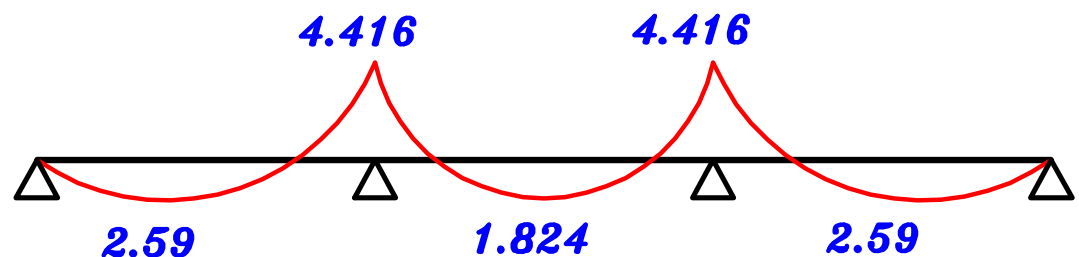
Strip ②



Strip ③



Strip ④



Sec. ① $M_{U.L.} = 6.96 \text{ kN.m/m}$

$t_s = 100 \text{ mm}$, $d = 100 - 20 = 80 \text{ mm}$, $B = 1000 \text{ mm}$ عرض الشريحة

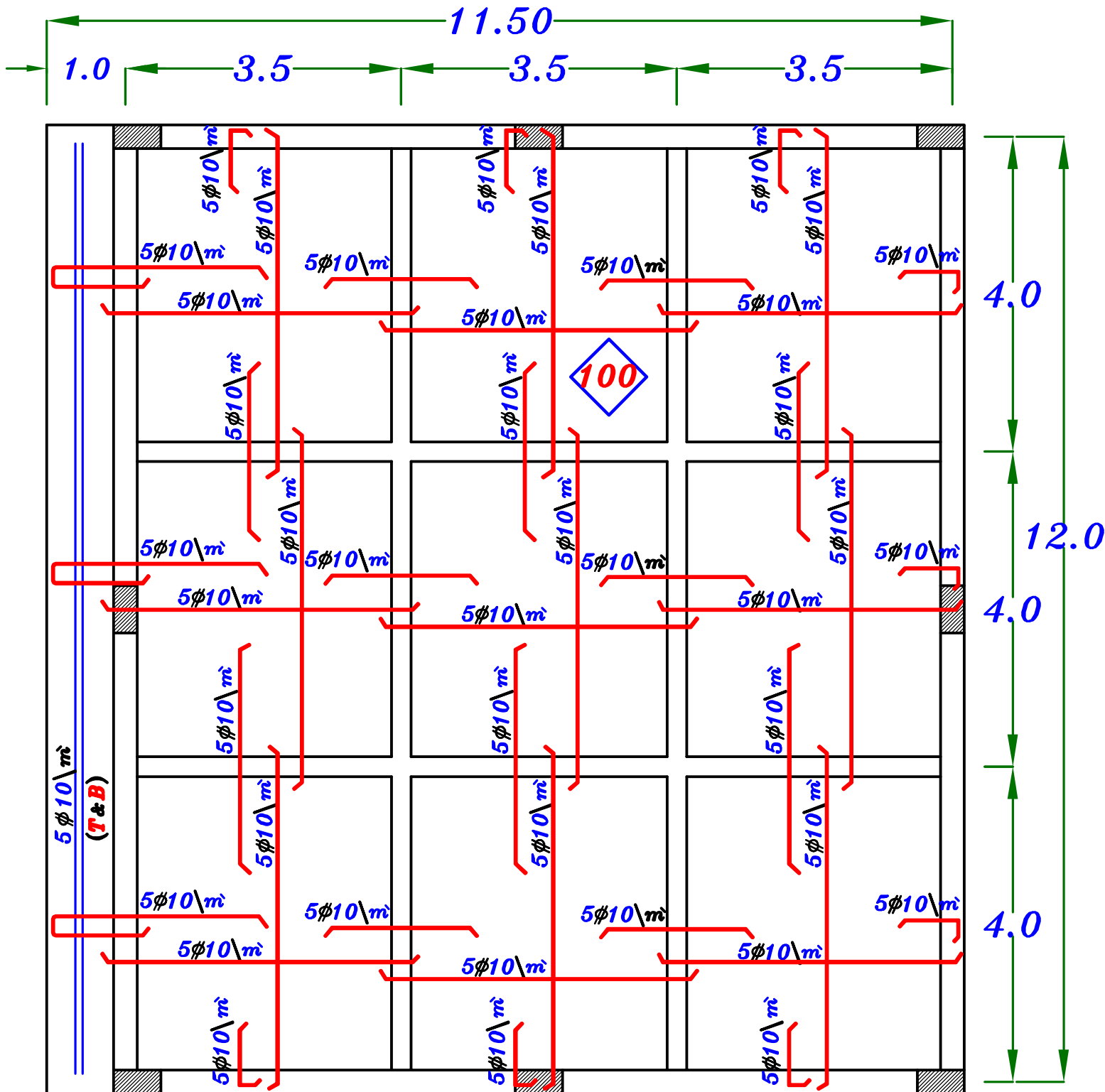
$$80 = C_1 \sqrt{\frac{6.96 * 10^6}{25 * 1000}} \longrightarrow C_1 = 4.79 \longrightarrow J = 0.825$$

$$A_s = \frac{6.96 * 10^6}{0.825 * 360 * 80} = 293 \text{ mm}^2/\text{m}$$

$$5 \phi 10 \setminus \text{m}$$

∴ سيؤخذ تسليح باقى القطاعات $5 \phi 10 \setminus \text{m}$

Details of RFT. For the Slab.



② Design of Panelled Beams.

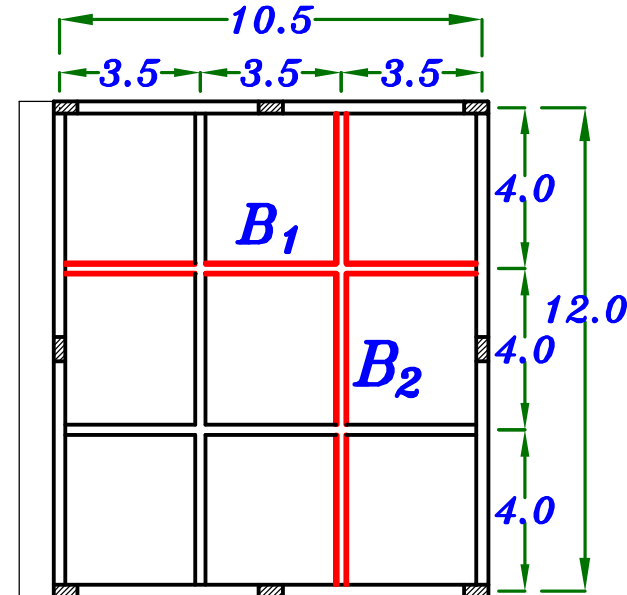
a – Get the Dimensions of the beam. (**b, t**)

Take **b** = 0.25 m

$$t = \frac{L_s}{16} = \frac{10.5}{16} = 0.656 \text{ m} \\ = 0.70 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$t = 0.70 \text{ m}$$



b – Get the Loads on the Slab. (**w_{av}**)

$$w_{av.} = w_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s}$$

$$w_{av.} = w_s + \frac{1.4 * b (t - t_s) [\text{مجموع أطوال الكمرات الداخلية}] * \delta_c}{L * L_s}$$

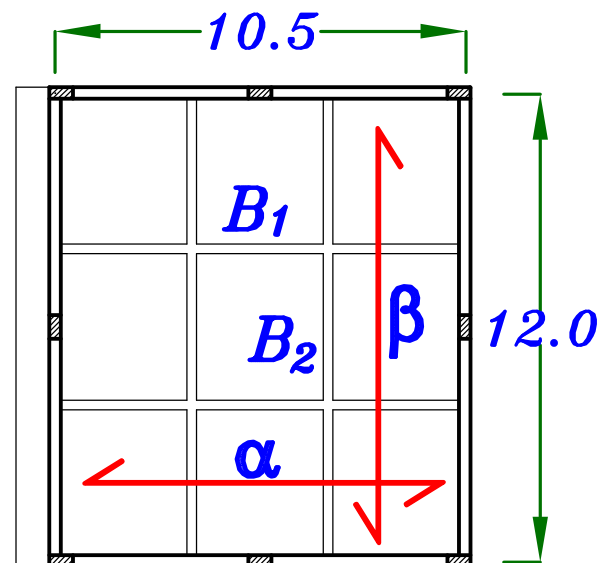
$$w_{av.} = 12.0 + \frac{1.4 * 0.25 (0.7 - 0.1) [2 * 12 + 2 * 10.5] * 25}{12 * 10.5} = 13.87 \text{ kN/m}^2$$

c – Calculate **α**, **β** By using Grashoff.

$$r = \frac{m L}{m' L_s} = \frac{(1.0) 12.0}{(1.0) 10.5} = 1.142$$

$$\alpha = \frac{r^4}{1 + r^4} = \frac{(1.142)^4}{1 + (1.142)^4} = 0.63$$

$$\beta = \frac{1}{1 + r^4} = \frac{1}{1 + (1.142)^4} = 0.37$$

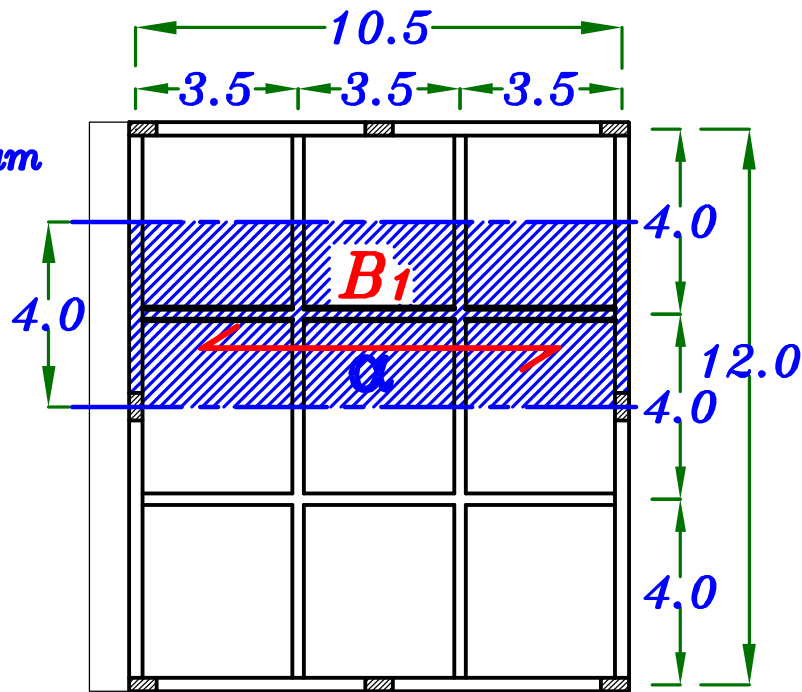


B_1 α Direction.

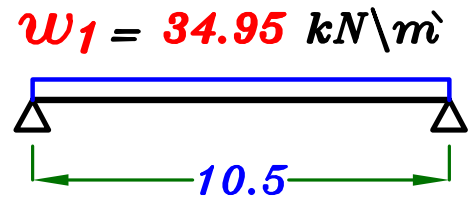
d – Get the Loads on the Panelled Beam & Calculate the B.M.

$$\alpha = 4.0 \text{ m}$$

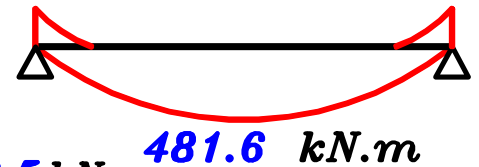
$$\begin{aligned} w_1 &= w_{av.} * \alpha * \alpha \\ &= 13.87 * 4.0 * 0.63 \\ &= 34.95 \text{ kN/m} \end{aligned}$$



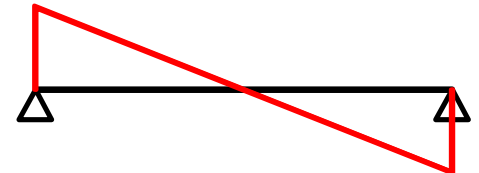
$$M = 34.95 * \frac{10.5^2}{8} = 481.6 \text{ kN.m}$$



B.M.D.



S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

$$X = 4.0 \text{ m} , \quad \frac{L}{2} = 6.0 \text{ m}$$

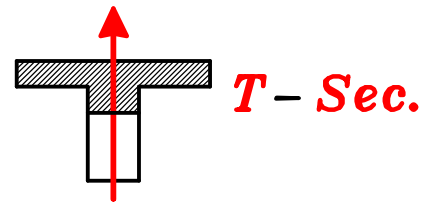
$$\theta_{B_1} = \frac{4.0}{6.0} * 90^\circ = 60^\circ$$

$$M_1 = 481.6 * \frac{\sin 60^\circ}{\sin 90^\circ} = 417.0 \text{ kN.m}$$

F- Design the Panelled Beam. B_1

α Direction. $\therefore \text{Cover} = 50 \text{ mm}$

$$t = 700 \text{ mm} \quad d = 700 - 50 = 650 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 4.0 \text{ m} = 4000 \text{ mm} \\ 16 t_s + b = 16 * 100 + 250 = 1850 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{10500}{5} + 250 = 2350 \text{ mm} \end{array} \right\} \quad \boxed{B = 1850 \text{ mm}}$$

$$650 = C_1 \sqrt{\frac{417.0 * 10^6}{25 * 1850}} \rightarrow C_1 = 6.84 \rightarrow J = 0.826$$

$$A_s = \frac{417.0 * 10^6}{0.826 * 360 * 650} = 2157 \text{ mm}^2$$

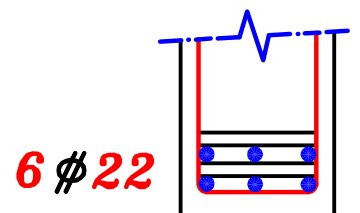
Check $A_{s_{min.}}$ $A_{s_{req.}} = 2157 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 650 = 507.8 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2157 \text{ mm}^2$$

6 ϕ 22

$$n = \frac{b - 25}{\phi + 25} = \frac{250 - 25}{22 + 25} = 4.78 = 4.0 \text{ bars}$$



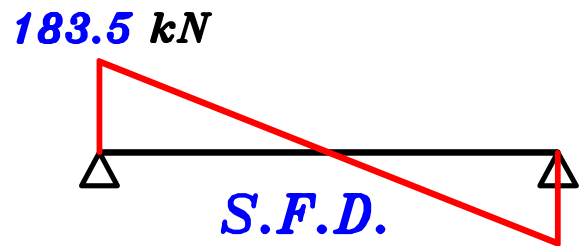
$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (215 \rightarrow 431 \text{ mm}^2)$$

3 ϕ 12

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$



$$q_s = \frac{Q_{max}}{b d} = \frac{183.5 * 10^3}{250 * 650} = 1.13 \text{ N/mm}^2 \quad \therefore q_{cu} < q_s < q_{u_{max}}$$

$$q_s - \frac{q_{cu}}{2} = \frac{n A_s (F_y / \delta_s)}{b S} \quad \text{Take } n = 2, \phi 8 = 50.3 \text{ mm}^2$$

$$1.13 - \frac{0.98}{2} = \frac{2 (50.3) (240 / 1.15)}{250 * S} \quad \longrightarrow S = 131.2 \text{ mm}$$

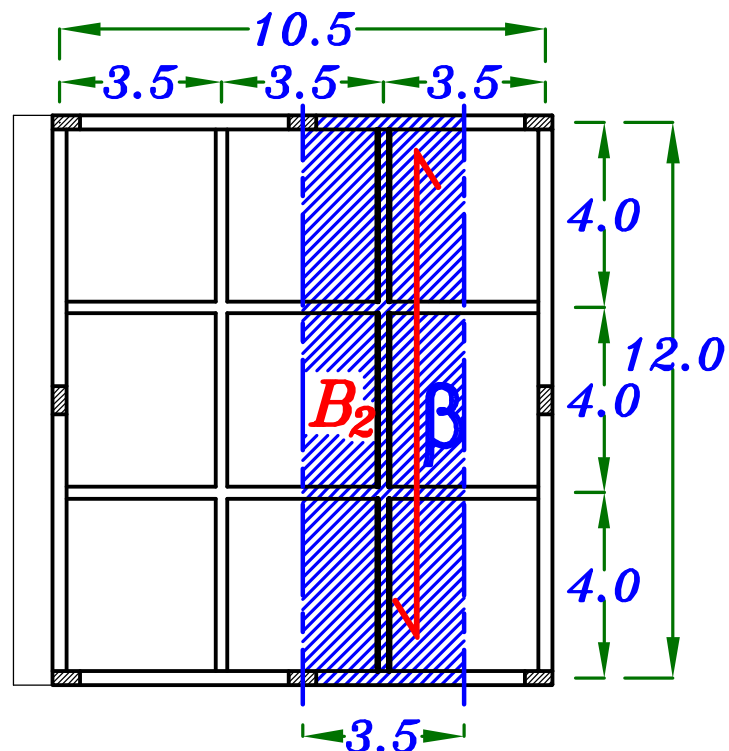
$$\text{No. of stirrups/m} = \frac{1000}{S} = \frac{1000}{131.2} = 7.62 \quad \text{Use } 8 \phi 8 \text{ m}$$

B₂ β Direction.

d- Get the Loads on the Panelled Beam & Calculate the B.M.

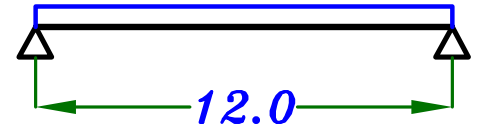
$$b = 3.5 \text{ m}$$

$$\begin{aligned} w_2 &= w_{av.} * b * \beta \\ &= 13.87 * 3.5 * 0.37 \\ &= 17.96 \text{ kN/m} \end{aligned}$$

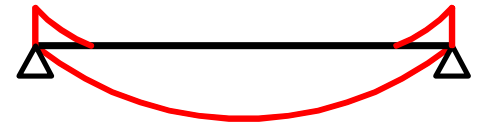


$$M = 17.96 * \frac{12.0^2}{8} = 323.3 \text{ kN.m}$$

$$w_2 = 17.96 \text{ kN/m}$$

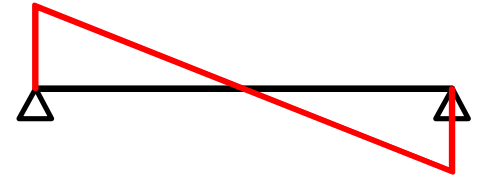


B.M.D.



$$107.76 \text{ kN} \quad 323.3 \text{ kN.m}$$

S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90}\right)$

$$X = 3.5 \text{ m} , \quad \frac{L}{2} = 5.25 \text{ m}$$

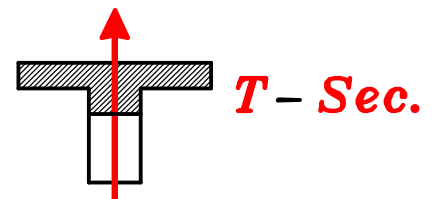
$$\theta_{B_1} = \frac{3.5}{5.25} * 90^\circ = 60^\circ$$

$$M_1 = 323.3 * \frac{\sin 60^\circ}{\sin 90^\circ} = 279.98 \text{ kN.m}$$

F– Design the Panelled Beam. B_1

β Direction. $\therefore \text{Cover} = 70 \text{ mm}$

$$t = 700 \text{ mm} \quad d = 700 - 70 = 630 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 3.5 \text{ m} = 3500 \text{ mm} \\ 16 t_s + b = 16 * 100 + 250 = 1850 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{12000}{5} + 250 = 2650 \text{ mm} \end{array} \right\} \quad \boxed{B = 1850 \text{ mm}}$$

$$630 = C_1 \sqrt{\frac{279.98 * 10^6}{25 * 1850}} \rightarrow C_1 = 9.55 \rightarrow J = 0.826$$

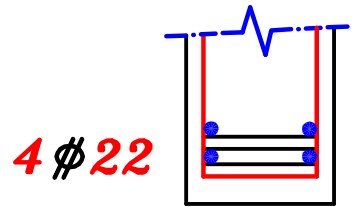
$$A_s = \frac{279.98 * 10^6}{0.826 * 360 * 630} = 1494.5 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1494.5 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 630 = 492.2 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1494.5 \text{ mm}^2$ **4 ϕ 22**

$$n = \frac{b - 25}{\phi + 25} = \frac{250 - 25}{22 + 25} = 4.78 = 4.0 \text{ bars}$$



Stirrup Hangers = $(0.1 \rightarrow 0.2) A_s = (107 \rightarrow 214 \text{ mm}^2)$ **2 ϕ 12**

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

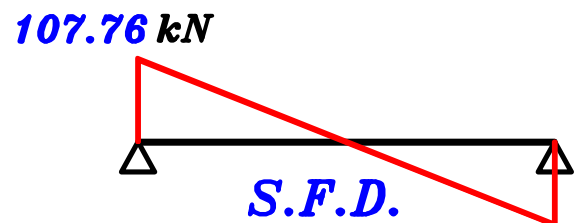
$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

$$q_s = \frac{Q_{max}}{b d} = \frac{107.76 * 10^3}{250 * 650} = 0.66 \text{ N/mm}^2$$

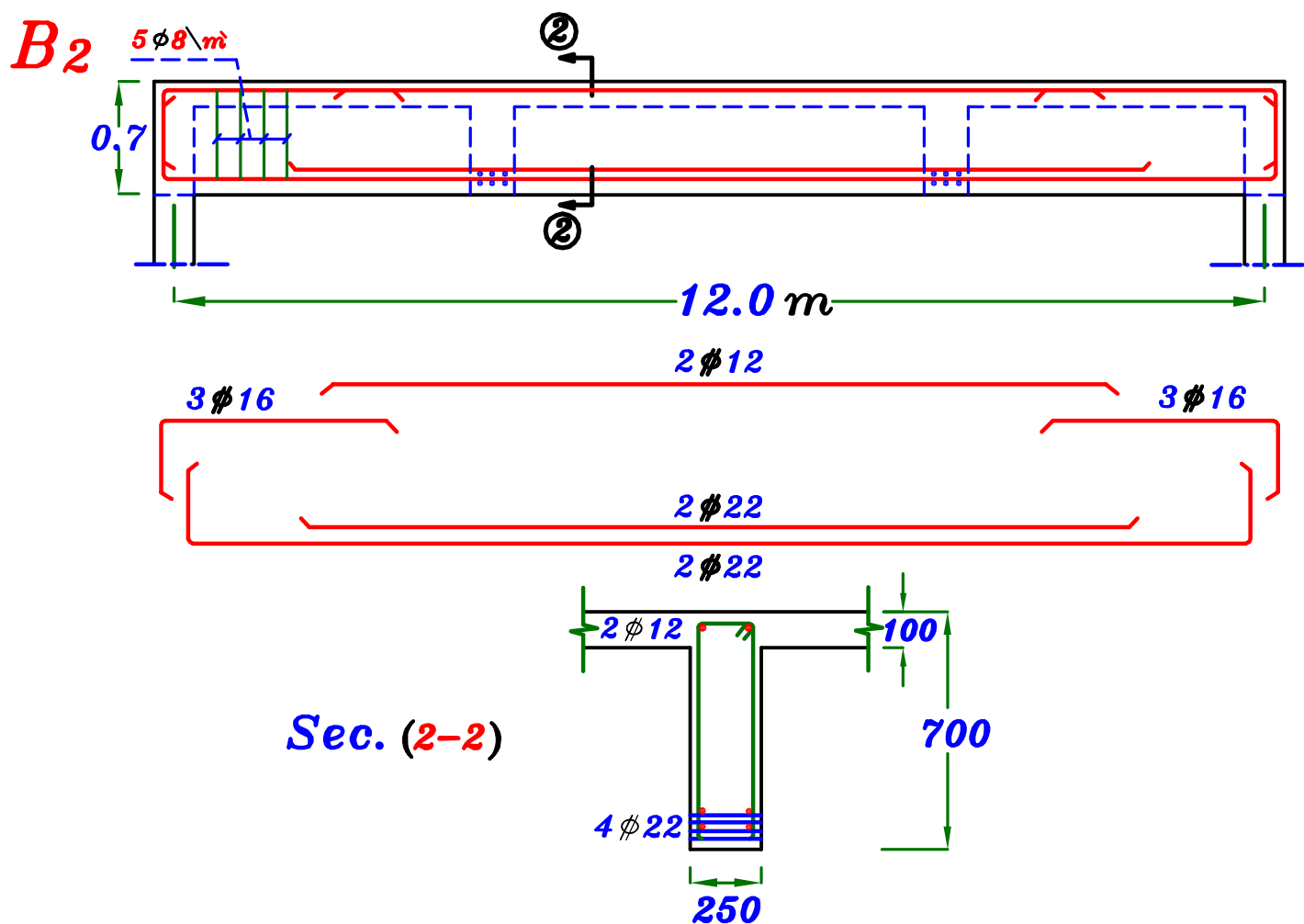
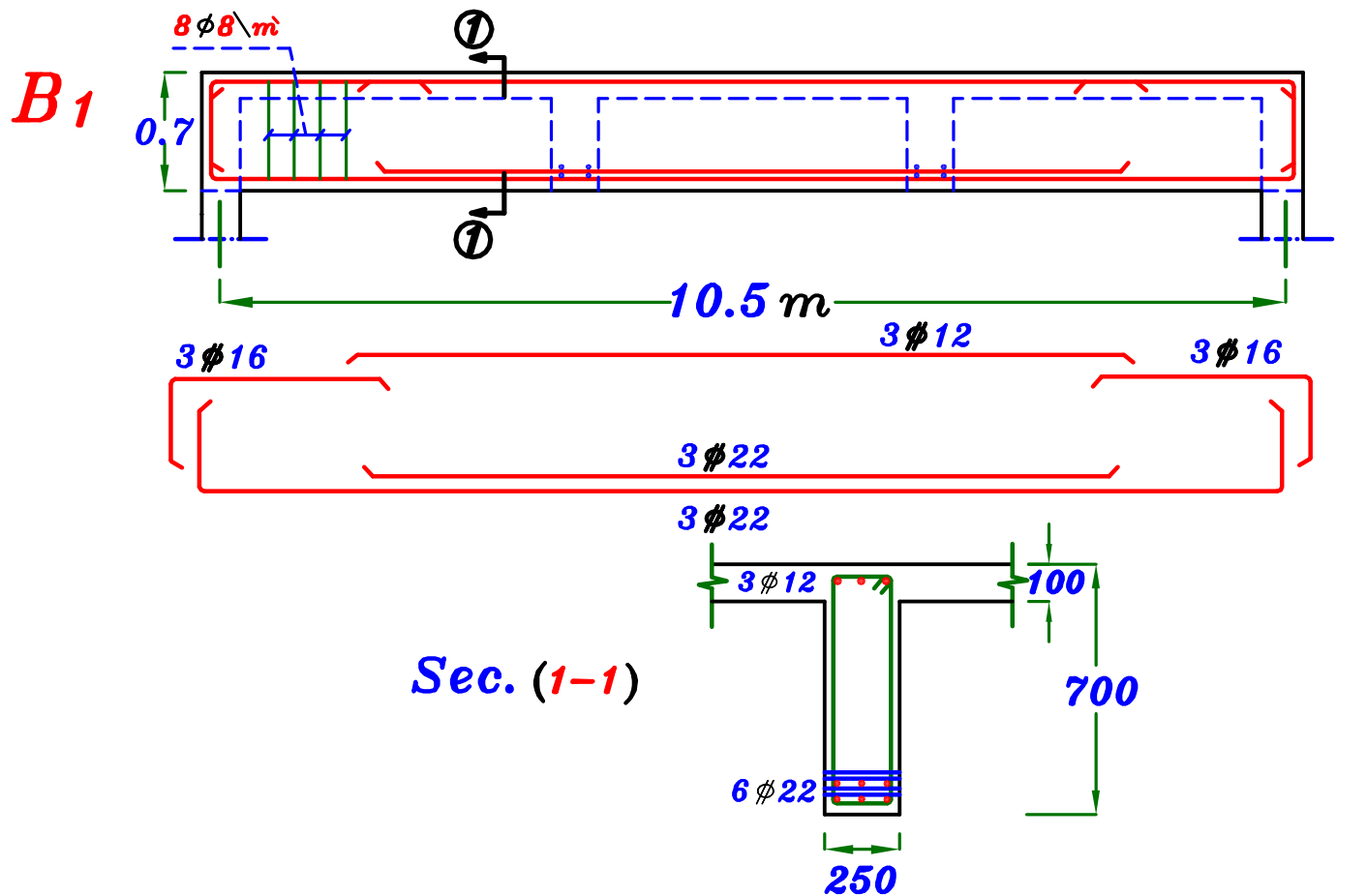
$$\therefore q_s < q_{cu}$$

\therefore Use min. Shear RFT.

5 ϕ 8 \text{ m}

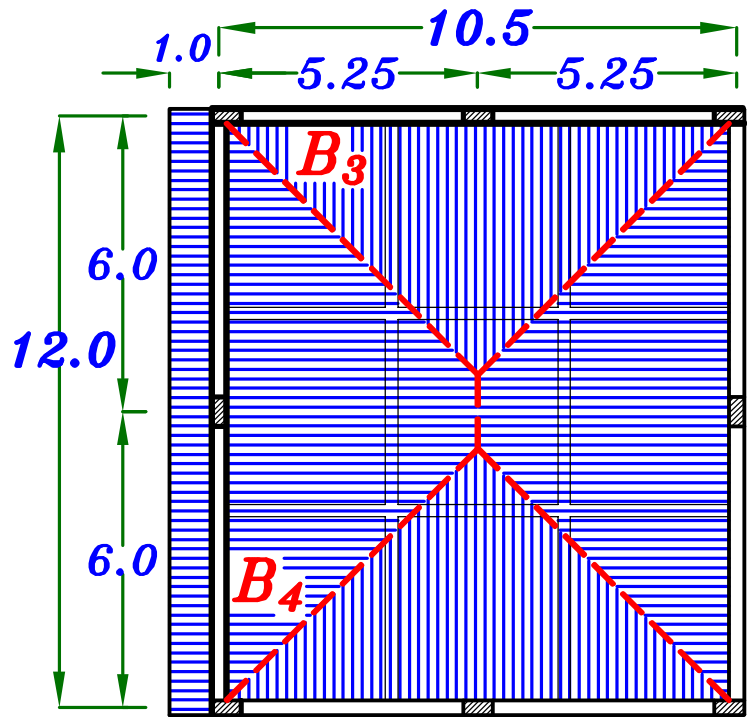


9 – Draw Details of RFT. For the Beams (B_1, B_2)



③ Design of Edge Beams. B_3, B_4

لان الكمرات ال **Panelled** محموله كلها
على الكمرات الخارجيه و ليس الاعمده .
اذا نستطيع حساب الاحمال على الكمرات الخارجيه
عن طريق **Approximate Method**

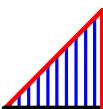


B_3

ال t للكمره الخارجيه يجب ان لا تقل عن ال t للكمره ال **Panelled** المحموله عليها

Take $b = 300 \text{ mm}$, $t = 700 \text{ mm}$

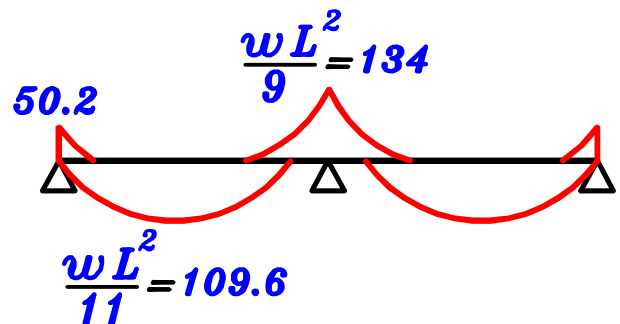
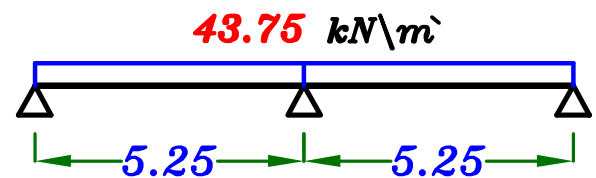
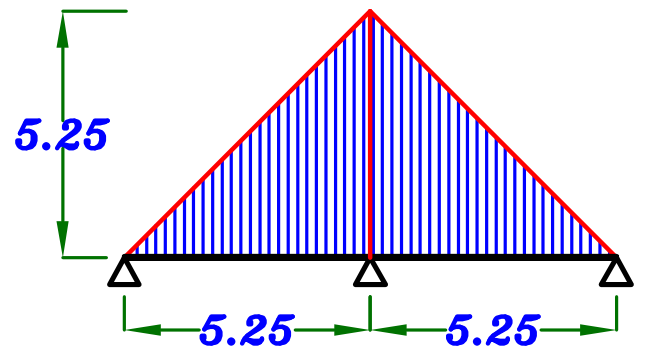
$$\begin{aligned} (o.w.)_{U.L.} &= 1.4 * b * t * \delta_c \\ &= 1.4 * 0.3 * 0.7 * 25 \\ &= 7.35 \text{ kN/m} \end{aligned}$$



$$\frac{\sum \text{area}}{\text{span}} = \frac{0.5 * 5.25 * 5.25}{5.25} = 2.625$$

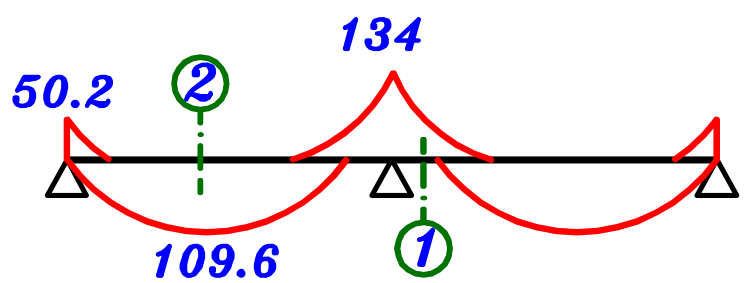
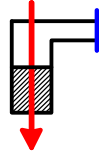
$$w_3 = (o.w.)_{\text{beam}} + \frac{\sum \text{area}}{\text{span}} (w_{av.})$$

$$w_3 = 7.35 + 2.625 * 13.87 = 43.75 \text{ kN/m}$$



Sec. ① $M_{U.L.} = 134.0 \text{ kN.m}$

R-Sec.



$$650 = C_1 \sqrt{\frac{134.0 * 10^6}{25 * 300}} \rightarrow C_1 = 4.85 \rightarrow J = 0.826$$

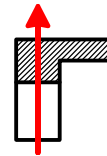
$$A_s = \frac{134.0 * 10^6}{0.826 * 360 * 650} = 693.3 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 693.3 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 650 = 507.8 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 693.3 \text{ mm}^2$ $4 \phi 16$

Sec. ② $M_{U.L.} = 109.6 \text{ kN.m}$ L-Sec.



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 6.0 \text{ m} = 6000 \text{ mm} \\ 6 t_s + b = 6 * 100 + 300 = 900 \text{ mm} \\ K \frac{L}{10} + b = 0.8 * \frac{5250}{10} + 300 = 720 \text{ mm} \end{array} \right\} \quad \boxed{B = 720 \text{ mm}}$$

$$650 = C_1 \sqrt{\frac{109.6 * 10^6}{25 * 720}} \rightarrow C_1 = 8.33 \rightarrow J = 0.826$$

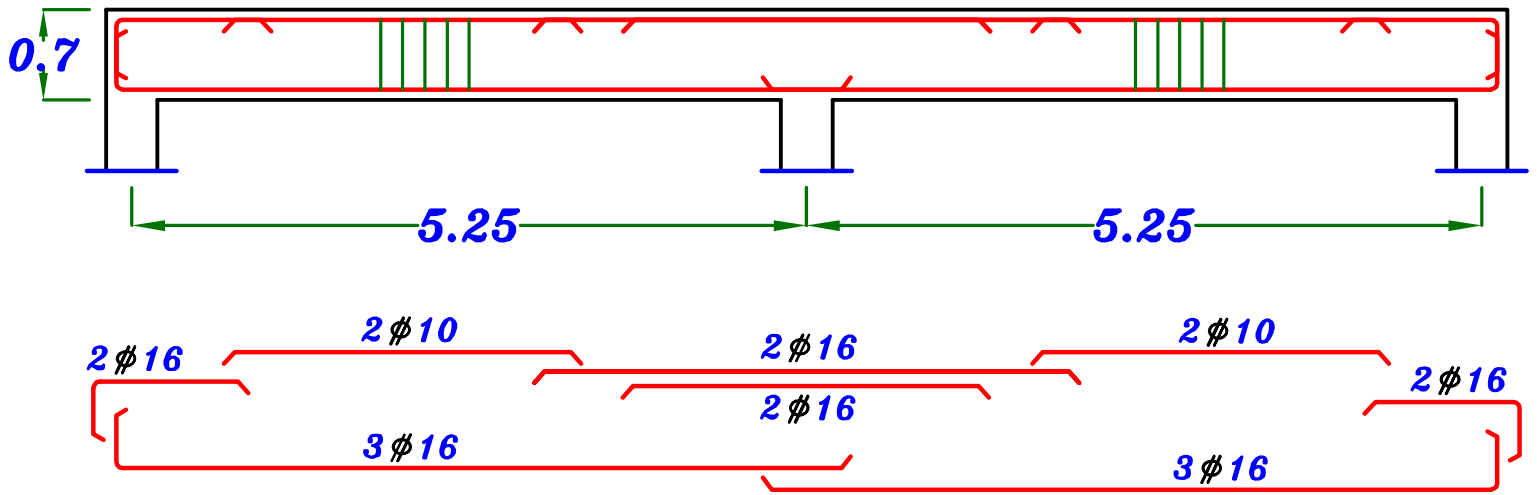
$$A_s = \frac{109.6 * 10^6}{0.826 * 360 * 650} = 567.0 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 567.0 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 650 = 507.8 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 567.0 \text{ mm}^2$ $3 \phi 16$

RFT. of Beam B_3

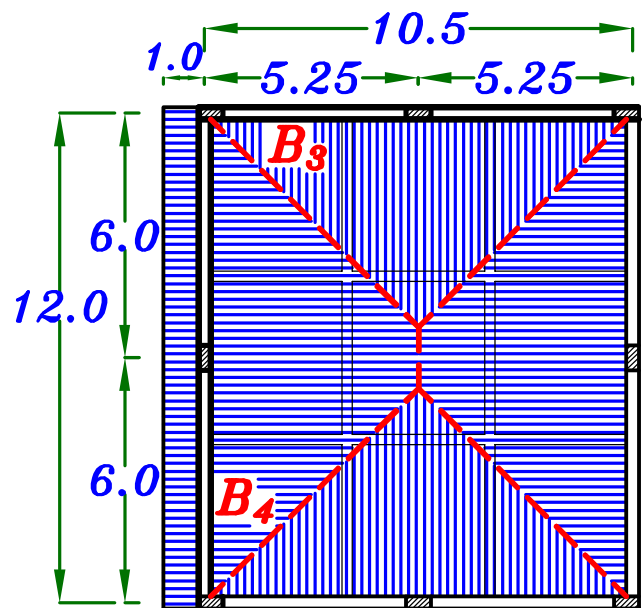
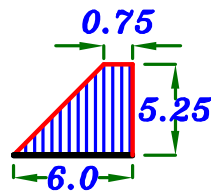


B_4

Take $b = 300 \text{ mm}$

$t = 700 \text{ mm}$

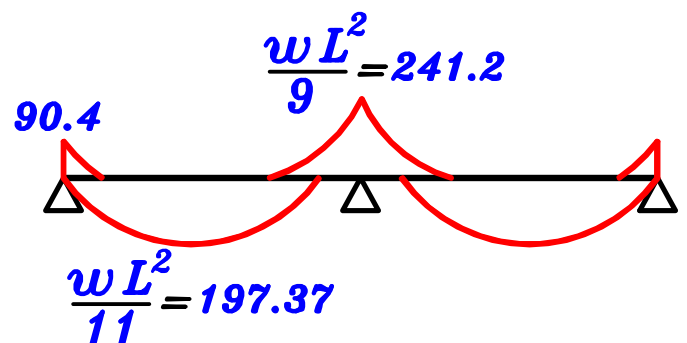
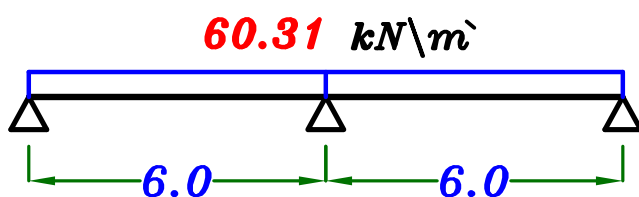
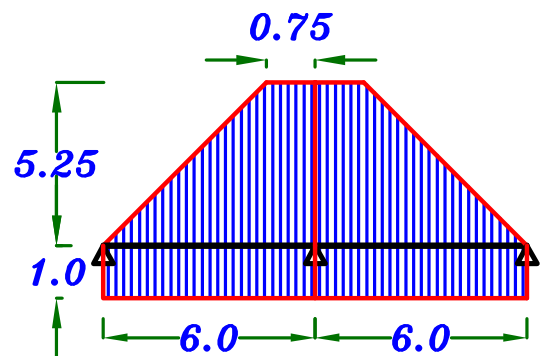
$(o.w.)_{U.L.} = 7.35 \text{ kN/m}$



$$\frac{\sum \text{area}}{\text{span}} = \frac{5.25 \left(\frac{6.0 + 0.75}{2} \right)}{6.0} = 2.953$$

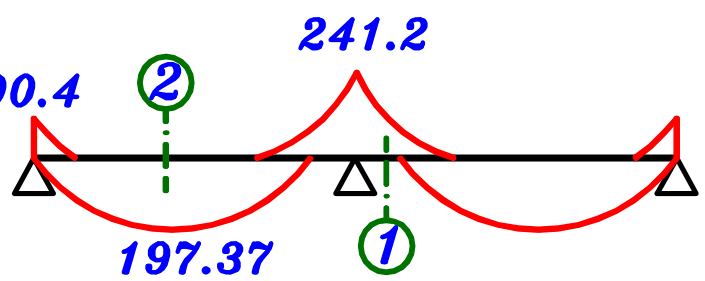
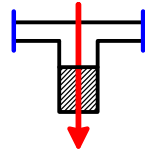
$$w_3 = (o.w.)_{\text{beam}} + \frac{\sum \text{area}}{\text{span}} (w_{\text{av.}}) + w_s L_c$$

$$w_3 = 7.35 + 2.953 * 13.87 + 12.0 * 1.0 = 60.31 \text{ kN/m}$$



Sec. ① $M_{U.L.} = 241.2 \text{ kN.m}$

R-Sec.



$$650 = C_1 \sqrt{\frac{241.2 * 10^6}{25 * 300}} \rightarrow C_1 = 3.62 \rightarrow J = 0.786$$

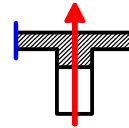
$$A_s = \frac{241.2 * 10^6}{0.786 * 360 * 650} = 1311 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1311 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 300 * 650 = 609.3 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1311 \text{ mm}^2$ 4 ϕ 22

Sec. ② $M_{U.L.} = 197.37 \text{ kN.m}$ T-Sec.



$$B = \left\{ \begin{array}{l} C.L.-C.L. = 1.0 + 5.25 = 6.25 = 6250 \text{ mm} \\ 16 t_s + b = 16 * 100 + 300 = 1900 \text{ mm} \\ K \frac{L}{5} + b = 0.8 * \frac{6000}{5} + 300 = 1260 \text{ mm} \end{array} \right\} \quad B = 1260 \text{ mm}$$

$$650 = C_1 \sqrt{\frac{197.37 * 10^6}{25 * 1260}} \rightarrow C_1 = 8.22 \rightarrow J = 0.826$$

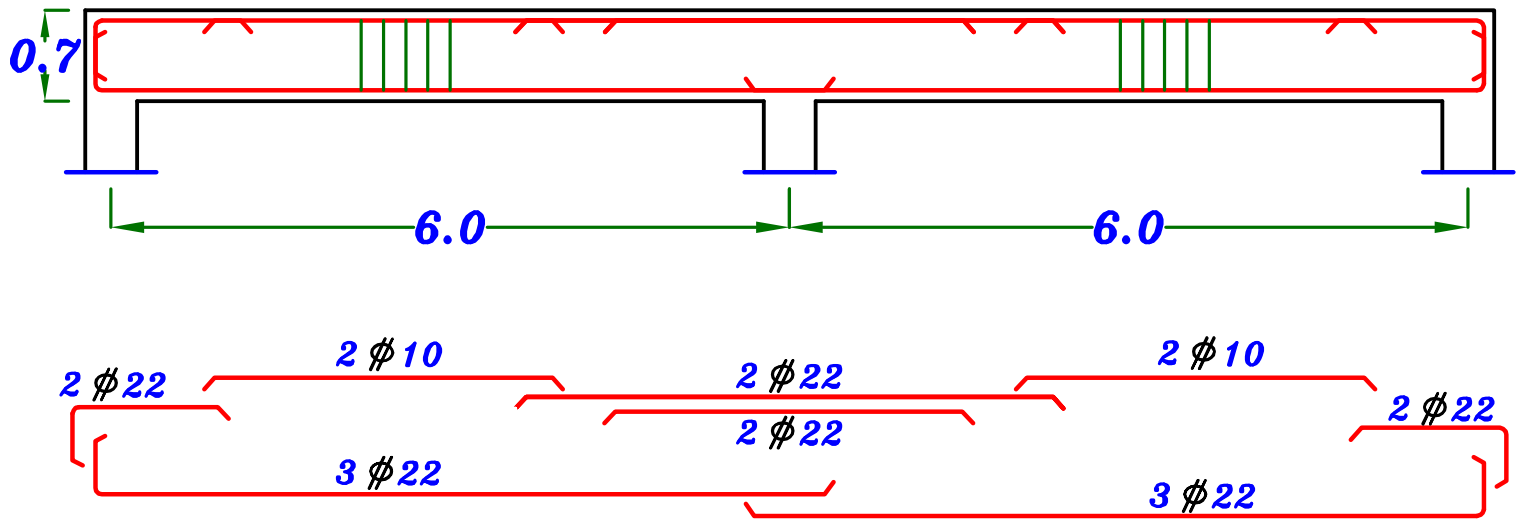
$$A_s = \frac{197.37 * 10^6}{0.826 * 360 * 650} = 1021 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1021 \text{ mm}^2$

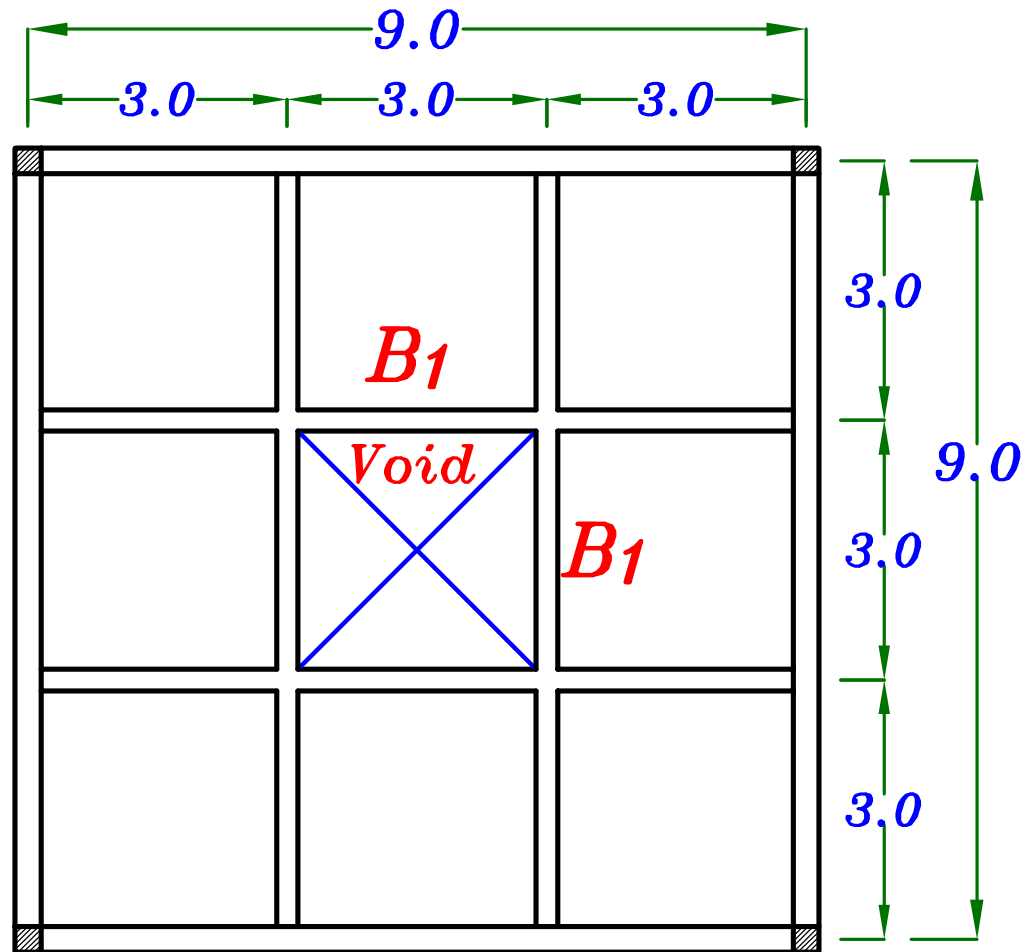
$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 300 * 650 = 609.3 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1021 \text{ mm}^2$ 3 ϕ 22

RFT. of Beam B_4



Example.



Data.

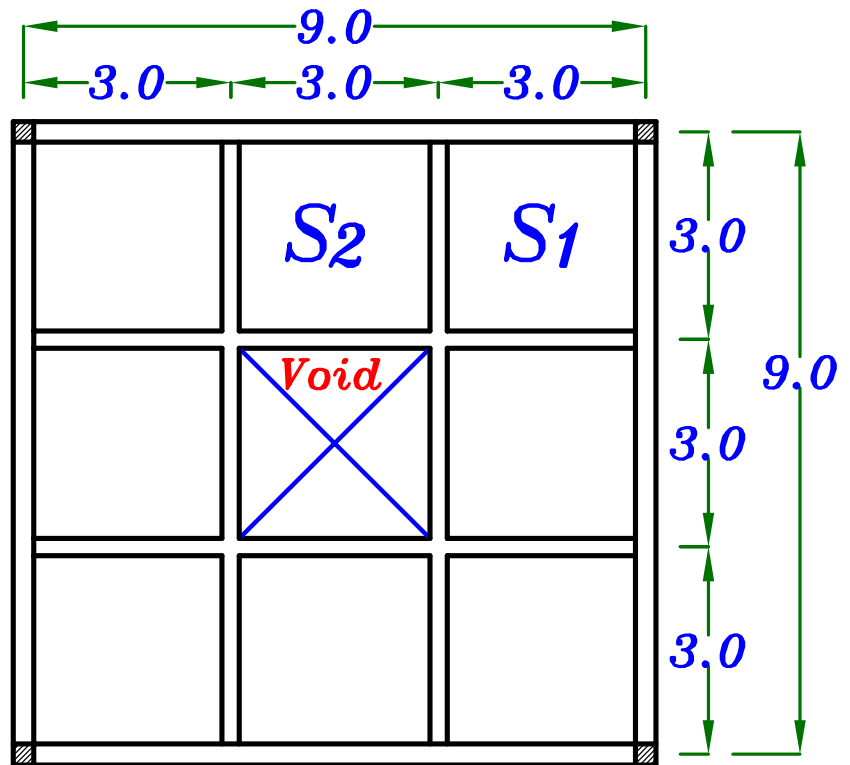
$$F_{cu} = 25 \text{ N/mm}^2 \quad F_y = 360 \text{ N/mm}^2$$

$$F.C. = 1.5 \text{ kN/m}^2 \quad L.L. = 3.0 \text{ kN/m}^2$$

Req.

- ① Design The Panelled Beam B_1
- ② Draw Details of RFT. of the beams in elevation & cross sections.

Design of Panelled Beams.



Choose the Thickness of the Slab. (t_s)

S_1 two way $L_s = 3.0\text{ m}$ \longleftarrow

$$t_s = \frac{3000}{40} = 75\text{ mm}$$

S_2 two way $L_s = 3.0\text{ m}$ \longleftarrow

$$t_s = \frac{3000}{35} = 85.7\text{ mm}$$

Take (t_s) the bigger value

$$t_s = 100\text{ mm}$$

b - Get the Loads on the Slab (w_s).

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 (L.L.) \quad \text{kN/m}^2$$

$$w_s = 1.4 (0.10 * 25 + 1.50) + 1.6 (3.0) = 10.4 \text{ kN/m}^2$$

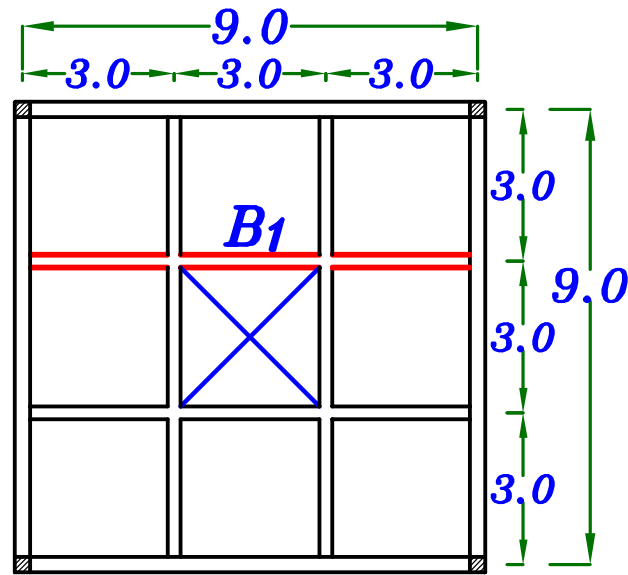
a – Get the Dimensions of the beam. (**b, t**)

Take **b = 0.25 m**

$$t = \frac{L_s}{16} = \frac{9.0}{16} = 0.56 \text{ m}$$

$$= 0.60 \text{ m}$$

$$\boxed{b = 0.25 \text{ m}} \quad \boxed{t = 0.60 \text{ m}}$$



b – Get the Loads on the Slab. (**w_{av}**)

$$w_{av.} = w_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s - \text{Void}}$$

$$w_{av.} = w_s + \frac{1.4 * b (t - t_s) [\text{مجموع أطوال الكمرات الداخلية}] * \delta_c}{L * L_s - \text{Void}}$$

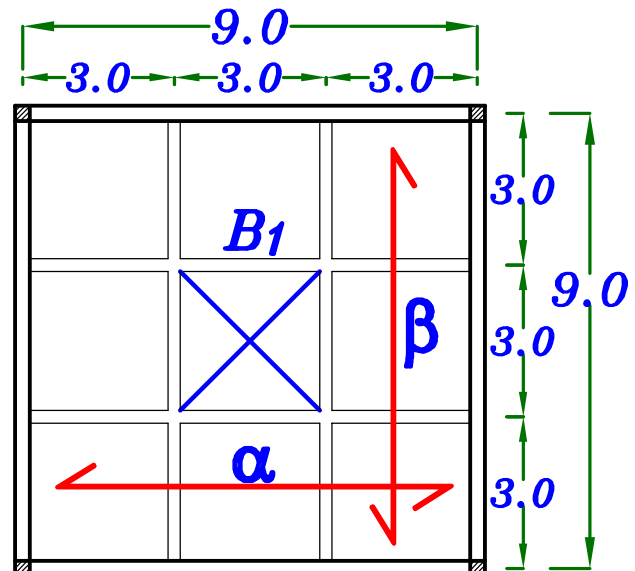
$$w_{av.} = 10.4 + \frac{1.4 * 0.25 (0.6 - 0.1) [2 * 9.0 + 2 * 9.0] * 25}{9.0 * 9.0 - 3.0 * 3.0} = 12.58 \text{ kN/m}^2$$

c – Calculate **α**, **β** By using Grashoff.

$$r = \frac{m L}{m L_s} = \frac{(1.0) 9.0}{(1.0) 9.0} = 1.0$$

$$\alpha = \frac{r^4}{1 + r^4} = \frac{(1.0)^4}{1 + (1.0)^4} = 0.50$$

$$\beta = \frac{1}{1 + r^4} = \frac{1}{1 + (1.0)^4} = 0.5$$



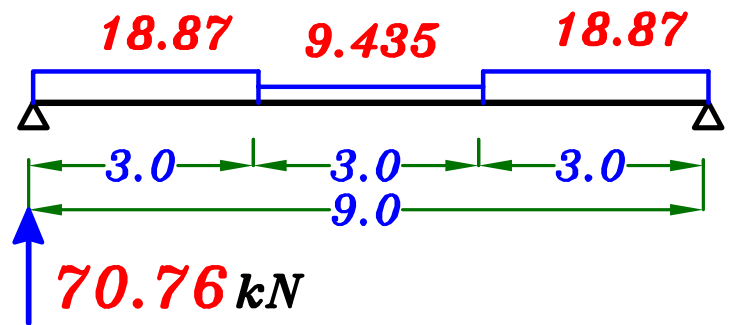
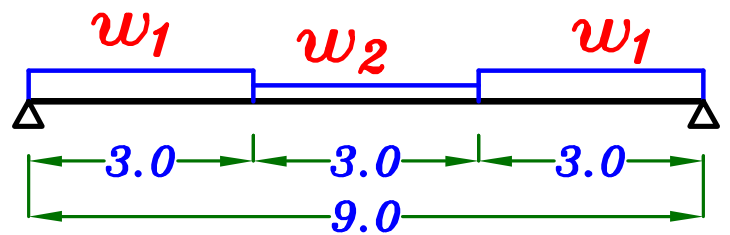
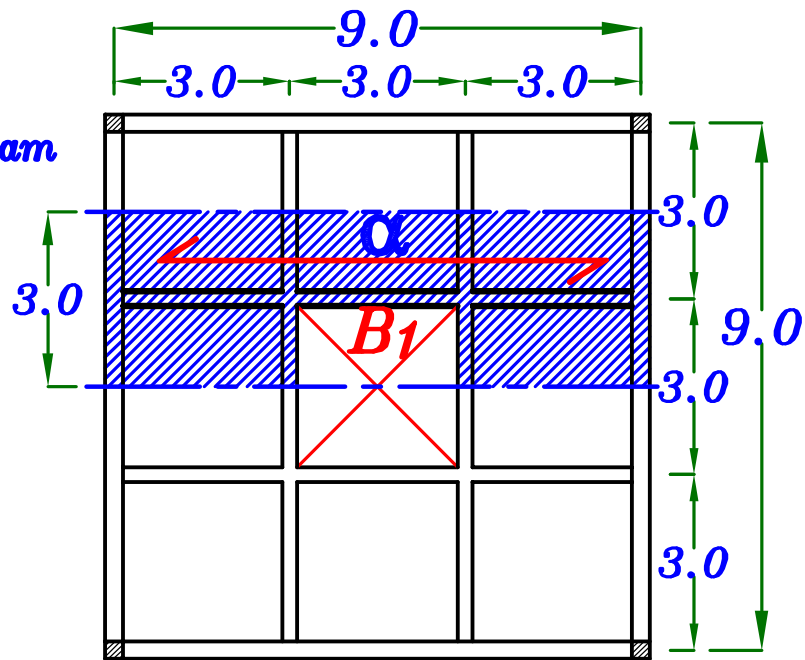
B_1 α Direction.

d– Get the Loads on the Panelled Beam
& Calculate the B.M.

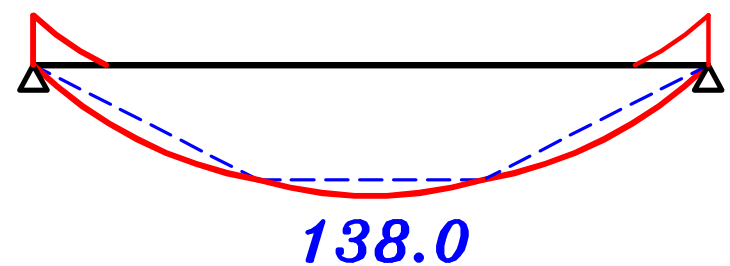
$$\alpha_1 = 3.0 \text{ m} , \quad \alpha_2 = 1.5 \text{ m}$$

$$\begin{aligned} w_1 &= w_{av.} * \alpha_1 * \alpha \\ &= 12.58 * 3.0 * 0.50 \\ &= 18.87 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} w_2 &= w_{av.} * \alpha_2 * \alpha \\ &= 12.58 * 1.5 * 0.50 \\ &= 9.435 \text{ kN/m} \end{aligned}$$

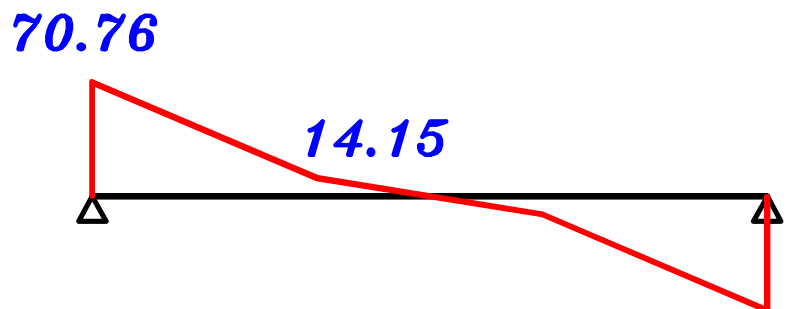


B.M.D.



$$M = 138.0 \text{ kN.m}$$

S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

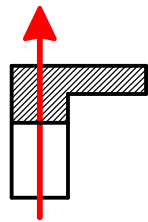
$$X = 3.0 \text{ m} , \quad \frac{L}{2} = 4.5 \text{ m}$$

$$\theta_{B_1} = \frac{3.0}{4.5} * 90^\circ = 60^\circ$$

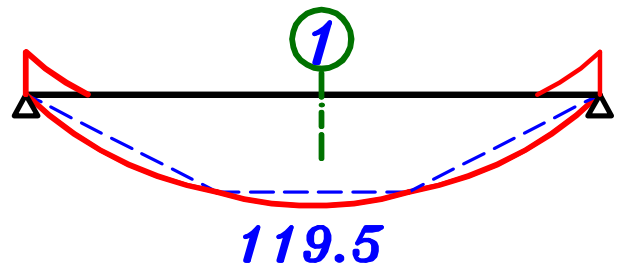
$$M_1 = 138.0 * \frac{\sin 60^\circ}{\sin 90^\circ} = 119.5 \text{ kN.m}$$

F – Design the Panelled Beam. B_1

فى الكمرات ال **symmetric** نصمم كمره واحده فقط و نضع تسليح الكمرتين مثل بعض
و يفضل ان نأخذ **cover** كمره β لانه الاكبر لانه فى التصميم كلما فرضنا ان ال **cover** اكبر
تقل قيمه **d** فى التصميم فتزيد كميته الحديد .



L – Sec.



β Direction. $\therefore \text{Cover} = 70 \text{ mm}$

$$t = 600 \text{ mm} \quad d = 600 - 70 = 530 \text{ mm}$$

$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = 1.5 \text{ m} = 1500 \text{ mm} \\ 6 t_s + b = 6 * 100 + 250 = 850 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{9000}{10} + 250 = 1150 \text{ mm} \end{array} \right\} \quad \boxed{B = 850 \text{ mm}}$$

$$530 = C_1 \sqrt{\frac{119.5 * 10^6}{25 * 850}} \rightarrow C_1 = 7.04 \rightarrow J = 0.826$$

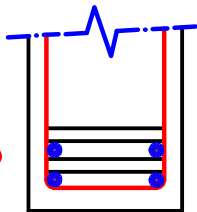
$$A_s = \frac{119.5 * 10^6}{0.826 * 360 * 530} = 758.2 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 758.2 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 530 = 414.06 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 758.2 \text{ mm}^2$ $4 \phi 22$

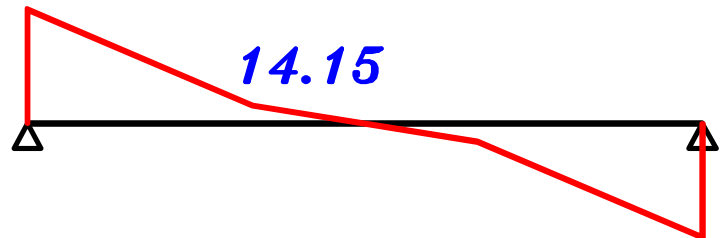
$$n = \frac{b - 25}{\phi + 25} = \frac{250 - 25}{16 + 25} = 5.48 = 5.0 \text{ bars}$$



Stirrup Hangers = $(0.1 \rightarrow 0.2) A_s = (75 \rightarrow 150 \text{ mm}^2)$ $2 \phi 10$

Check Shear.

S.F.D. 70.76



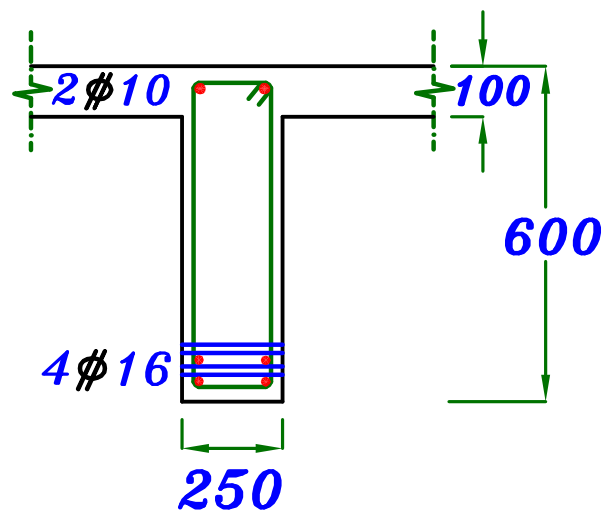
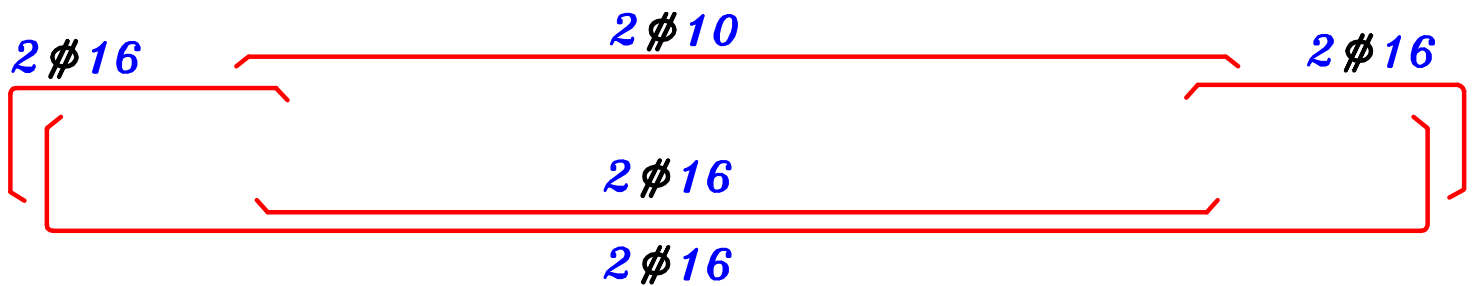
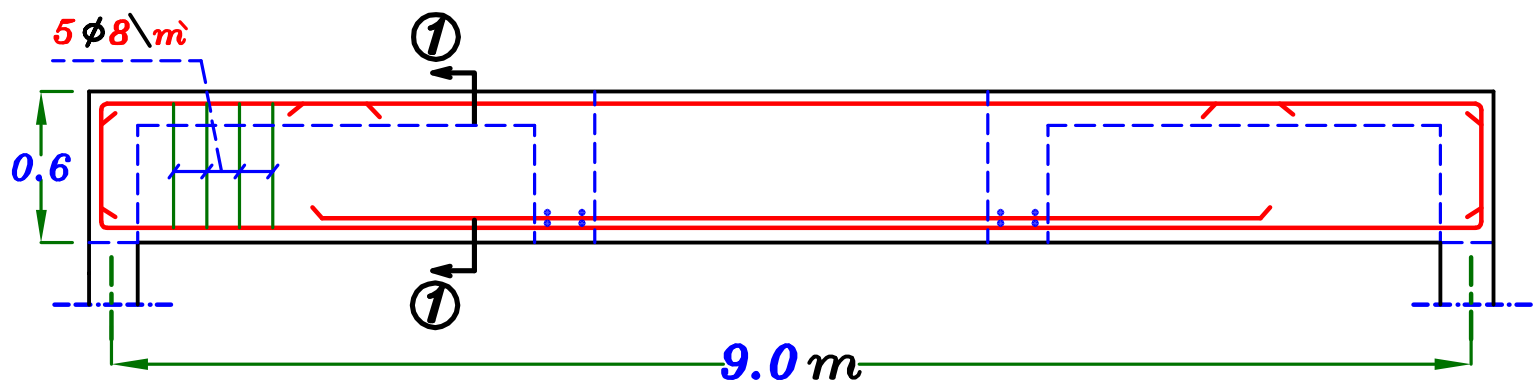
$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

$$q_s = \frac{Q_{max}}{b d} = \frac{70.76 * 10^3}{250 * 530} = 0.53 \text{ N/mm}^2$$

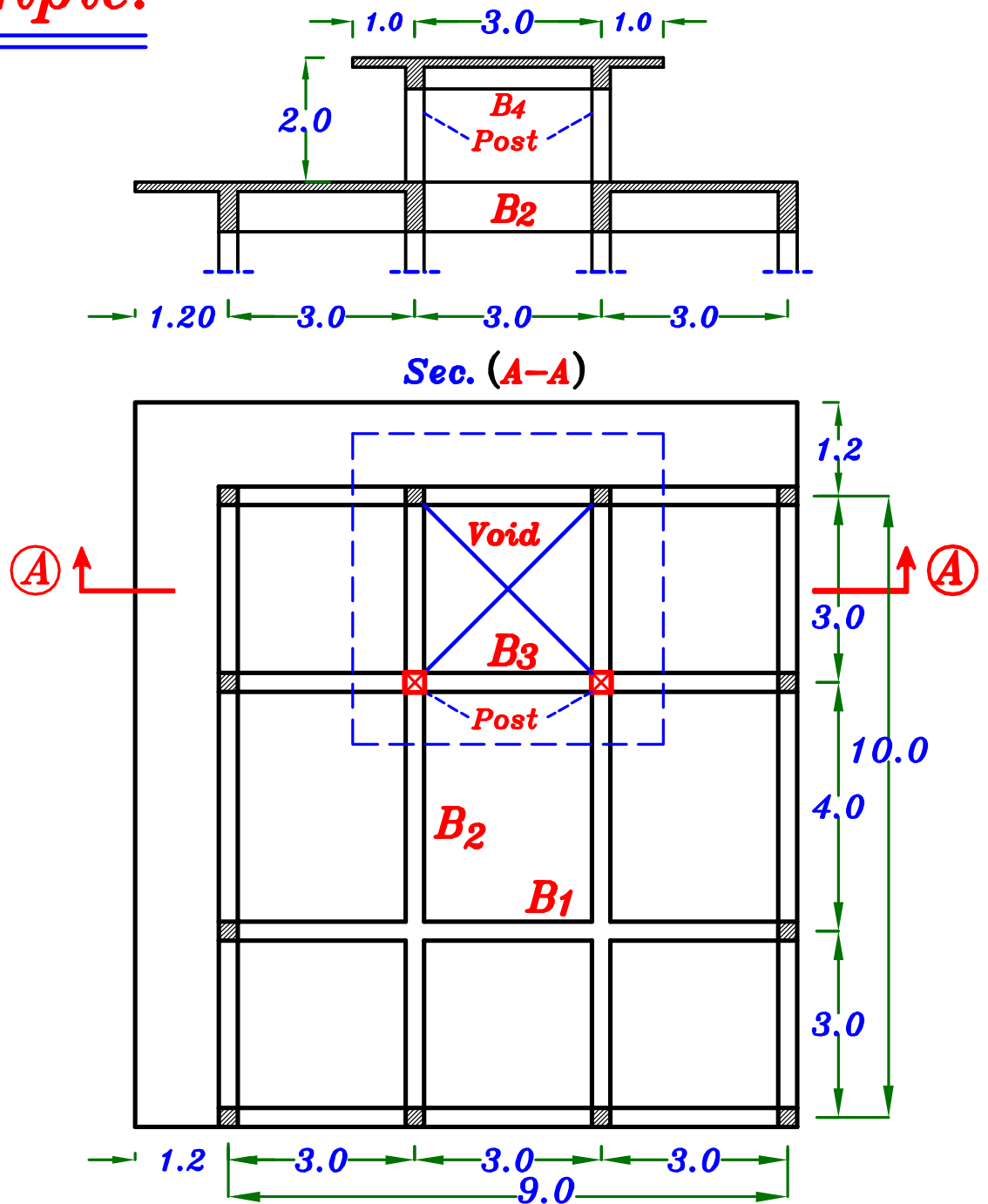
$\therefore q_s < q_{cu} \therefore \text{Use min. Shear RFT.}$ $5 \phi 8 \backslash m$

9 – Draw Details of RFT. For the Beam B_1



Sec. (1-1)

Example.



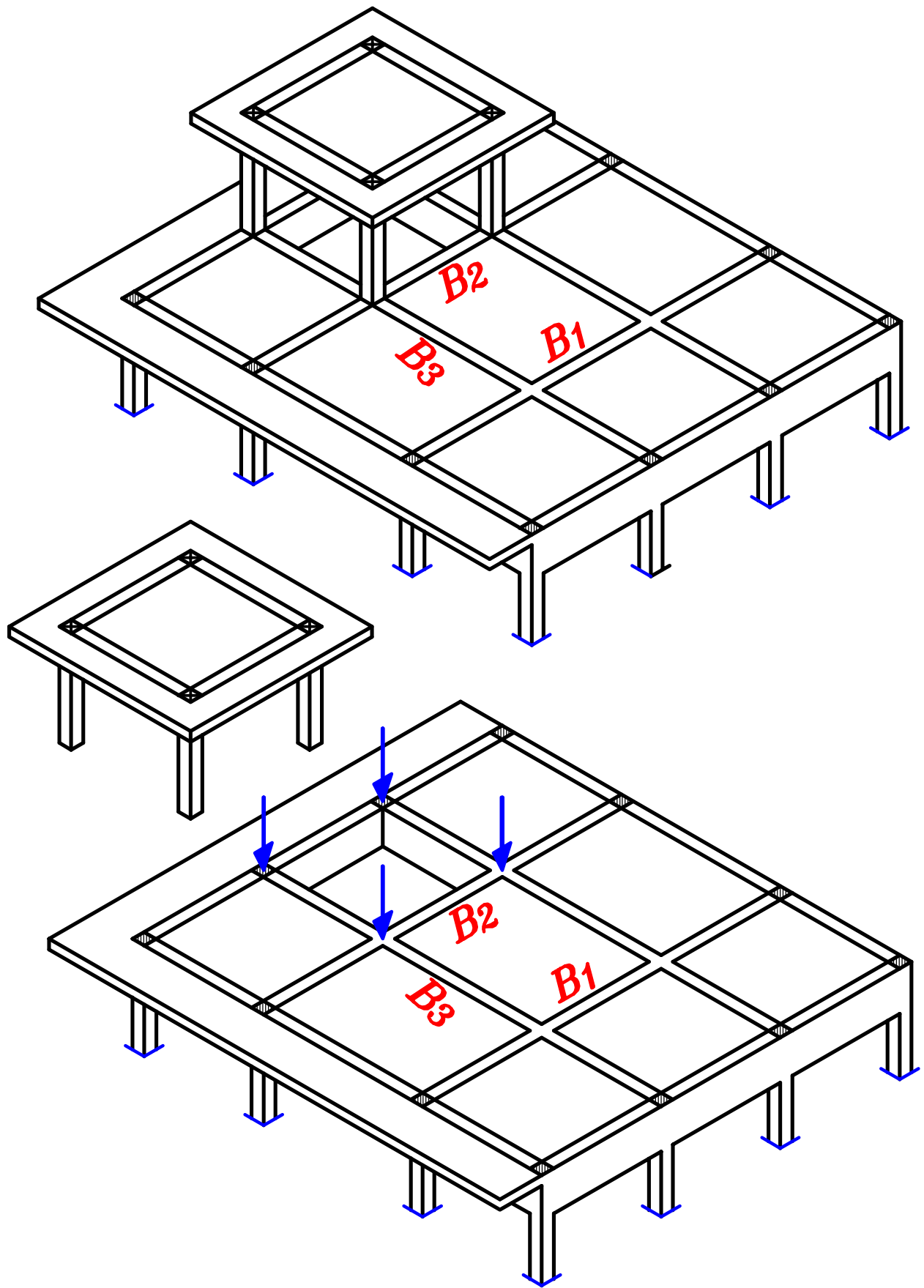
Data.

$$F_{cu} = 25 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

$$F.C. = 1.50 \text{ kN/m}^2, \quad L.L. = 2.0 \text{ kN/m}^2$$

Req.

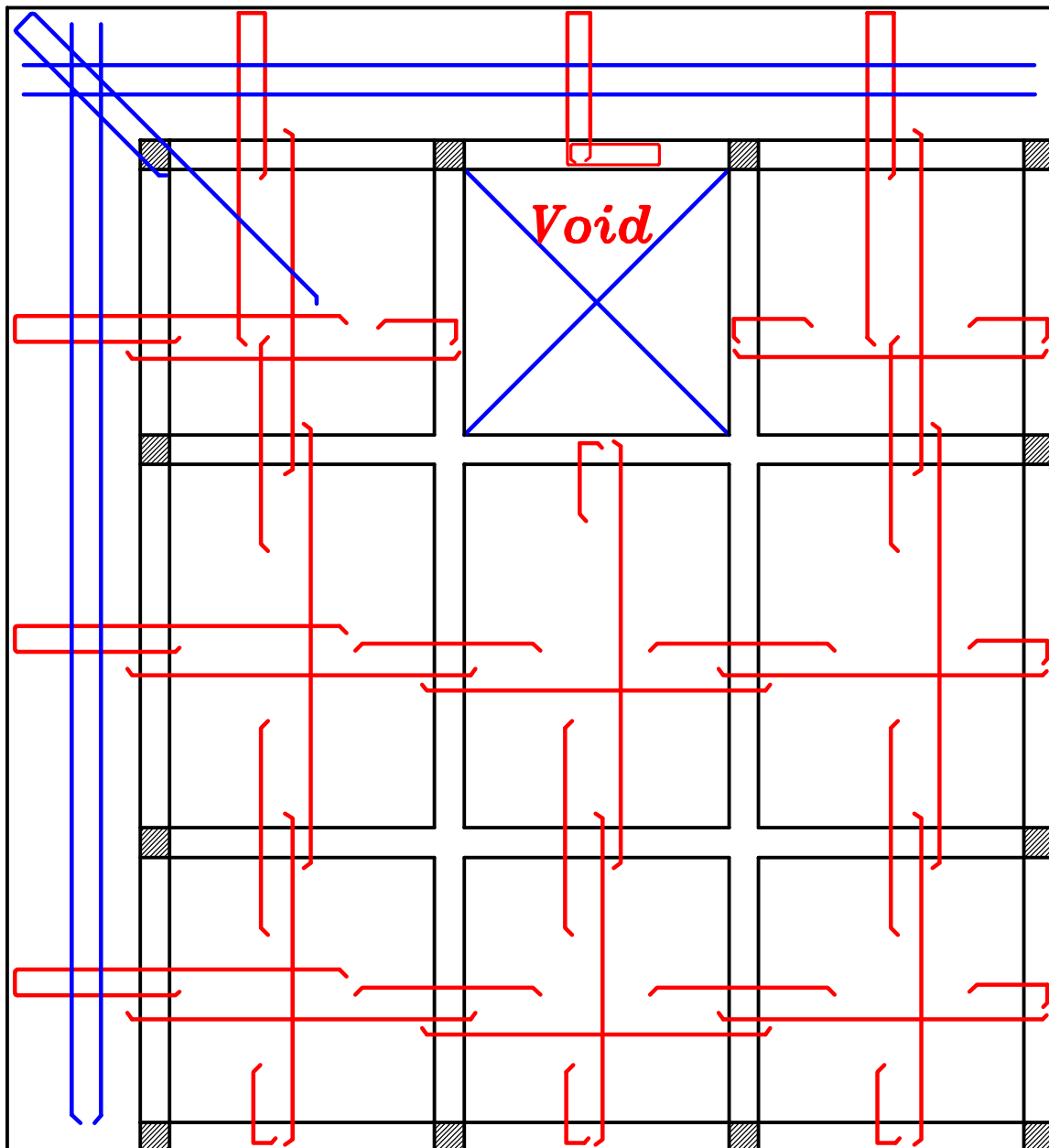
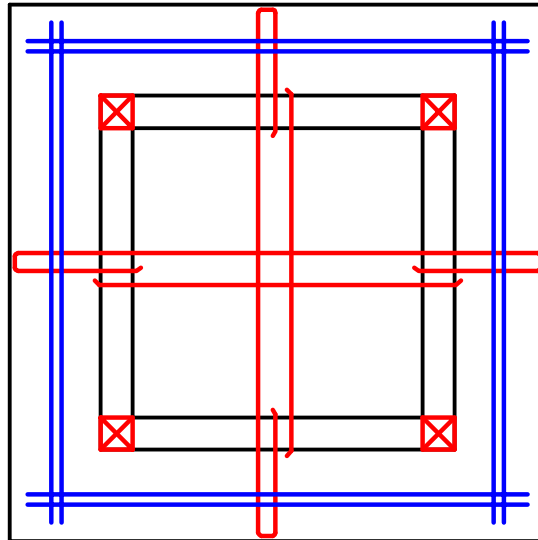
- ① Draw a sketch show the **RFT** of the slabs. **without Calculations.**
- ② Design the panelled beams B_1, B_2, B_3
- ③ Draw Details of **RFT** of the beams in elevation & cross sections.



فكره المسأله

الوزن الكلى للشخشيخه يتوزع على **4 Posts** و يكون حمل ال **Post** الواحد حمل مركز اثنان منهم يحملوا مباشره على الاعمده و الاثنان الاخران يعتبروا حمل مركز محمول على الكمرات ال **Panelled B₂ & B₃** و يتوزع الحمل المركز على الكمرات بنسبتي α و β

① RFT. of the Slabs.



Design of Panelled Beams.

a- Choose the Thickness of the Slab. (t_s).

S_1 two way $L_s = 3.0$ m

$$t_s = \frac{3000}{45} = 66.6 \text{ mm}$$

S_2 two way $L_s = 3.0$ m

$$t_s = \frac{3000}{40} = 75.0 \text{ mm}$$

S_3 two way $L_s = 3.0$ m

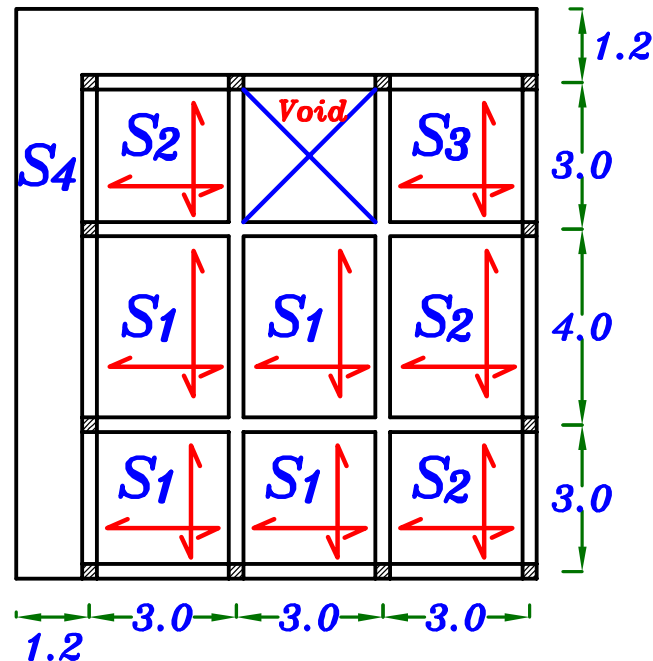
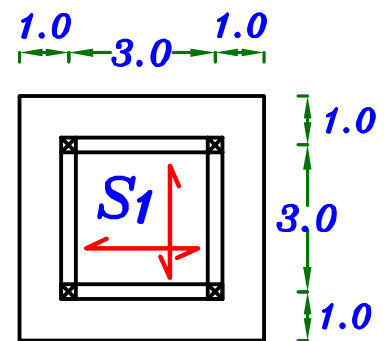
$$t_s = \frac{3000}{35} = 85.7 \text{ mm}$$

S_4 Cantilever $L_c = 1.2$ m

$$t_s = \frac{1200}{10} = 120 \text{ mm}$$

Take (t_s) the bigger value

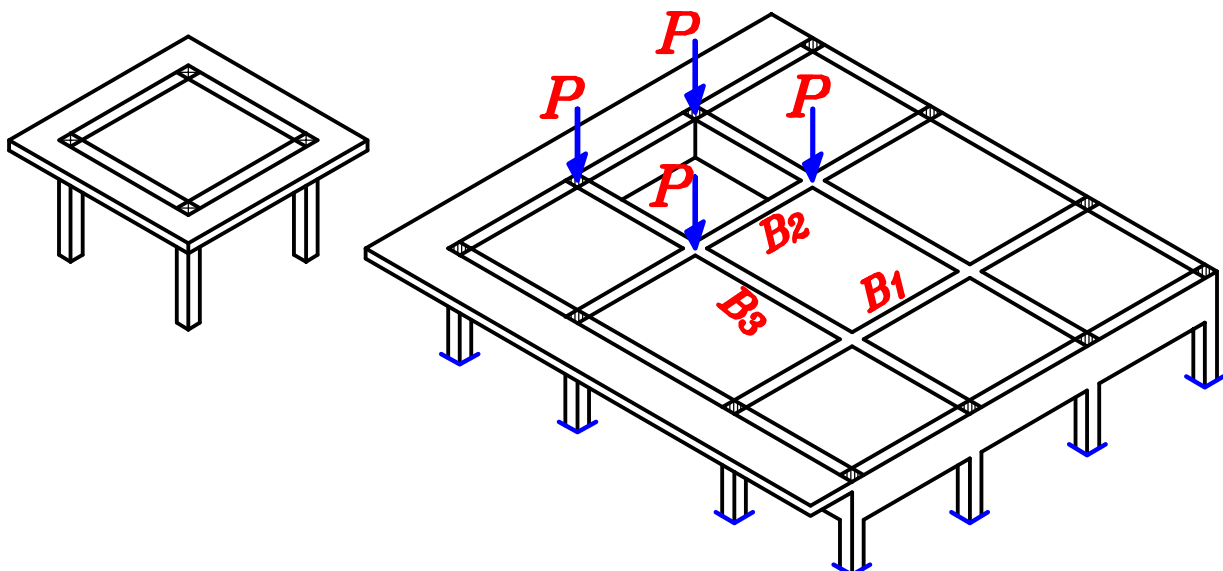
$$t_s = 120 \text{ mm}$$



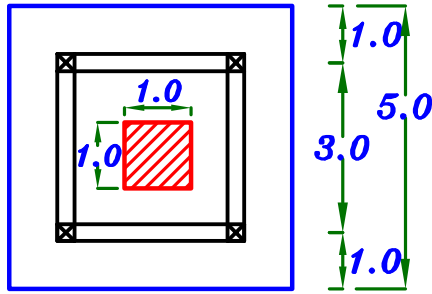
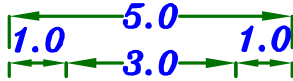
b- Get the Loads on the Slab (w_s).

$$w_s = 1.4 (0.12 * 25 + 1.50) + 1.6 (2.0) = 9.50 \text{ kN/m}^2$$

الوزن الكلى للشخشيخة يتوزع على **4 Posts** و يكون حمل ال **Post** الواحد حمل مركز اثنان منهم يحملوا مباشرة على الاعمده و الاثنان الاخران يعتبروا حمل مركز محمول على الكمرات ال **Panelled B_2 & B_3** و يتوزع الحمل المركز على الكمرات بنسبتي α , β



لحساب قيمه P لل $Post$ الواحد نحسب الوزن الكلى للشخشيخه (وزن البلاطه + وزن الكمرات + وزن ال $Posts$)
ثم نقسم الحمل الكلى على ϵ فيكون هذا هو حمل ال $Post$ الواحد

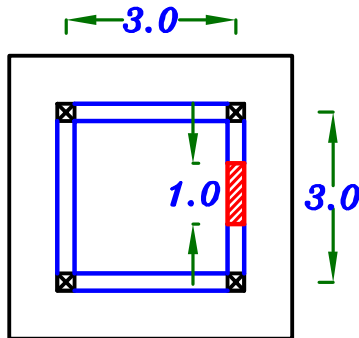


١- وزن البلاطه = وزن متر مربع \times مساحه البلاطه

Total weight of Slab

$$W_s * area = 9.50 * (5.0 * 5.0) = 237.5 \text{ kN}$$

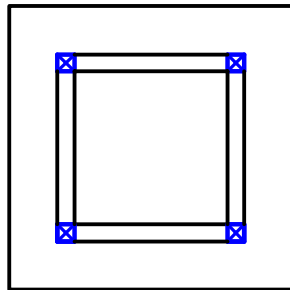
٢- وزن الكمرات = وزن متر طولى من الكمره \times الطول الكلى لا ϵ كمرات



$$\text{Take } o.w.(beam) = 3.0 * 1.4 = 4.20 \text{ kN/m} \quad (U.L.)$$

Total weight of Beams

$$o.w.(beam) * length = 4.20 * (4 * 3.0) = 50.4 \text{ kN}$$



٣- وزن ال $Posts$

$$\text{Take } o.w.(Post) = 3.50 \text{ kN}$$

$$\text{Total weight of Posts} = 3.50 * 4 = 14 \text{ kN}$$

يتوزع الحمل الكلى للشخشيخه على 4 $Posts$

$$\text{Loads on one Post} = \frac{\sum \text{Weight}}{4.0} = \frac{50.4 + 237.5 + 14}{4.0}$$

$$\text{Loads on one Post} = P = 75.5 \text{ kN}$$

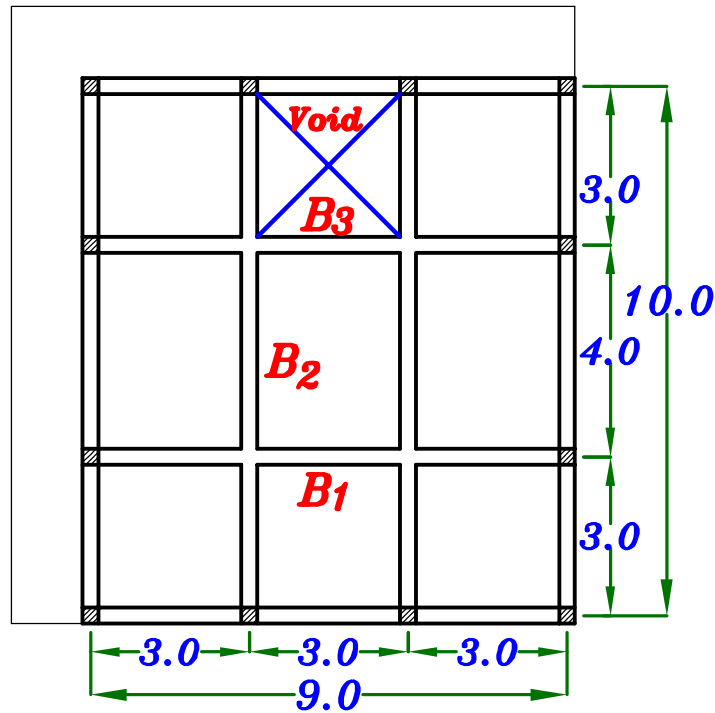
a – Get the Dimensions of the beam. (**b, t**)

Take **b** = 0.25 m

$$t = \frac{L_s}{16} = \frac{9.0}{16} = 0.56 \text{ m} \\ = 0.60 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$t = 0.60 \text{ m}$$



b – Get the Loads on the Slab. (**w_{av}**)

$$w_{av.} = w_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s - \text{Void}}$$

$$w_{av.} = w_s + \frac{1.4 * b (t - t_s) [\text{مجموع أطوال الكمرات الداخلية}] * \delta_c}{L * L_s - \text{Void}}$$

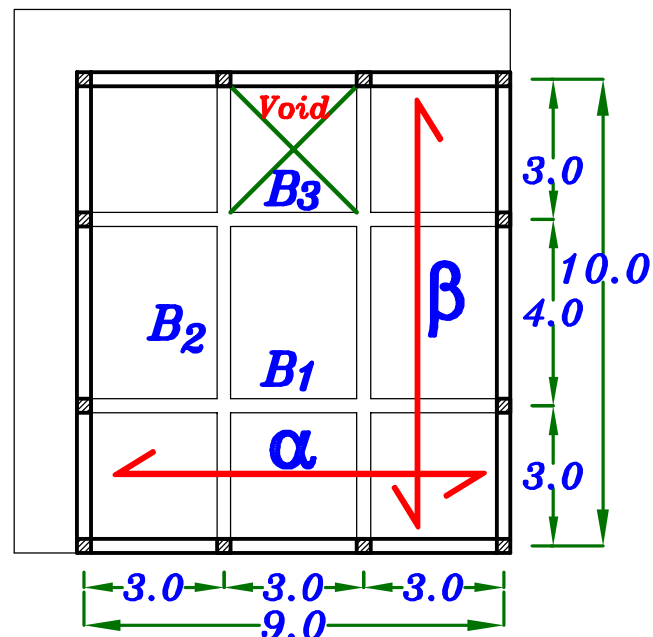
$$w_{av.} = 9.50 + \frac{1.4 * 0.25 (0.6 - 0.12) [2 * 9.0 + 2 * 10.0] * 25}{9.0 * 10.0 - 3.0 * 3.0} = 11.47 \text{ kN/m}^2$$

c – Calculate **α**, **β** By using Grashoff.

$$r = \frac{m L}{m L_s} = \frac{(1.0) 10.0}{(1.0) 9.0} = 1.11$$

$$\alpha = \frac{r^4}{1 + r^4} = \frac{(1.11)^4}{1 + (1.11)^4} = 0.603$$

$$\beta = \frac{1}{1 + r^4} = \frac{1}{1 + (1.11)^4} = 0.397$$

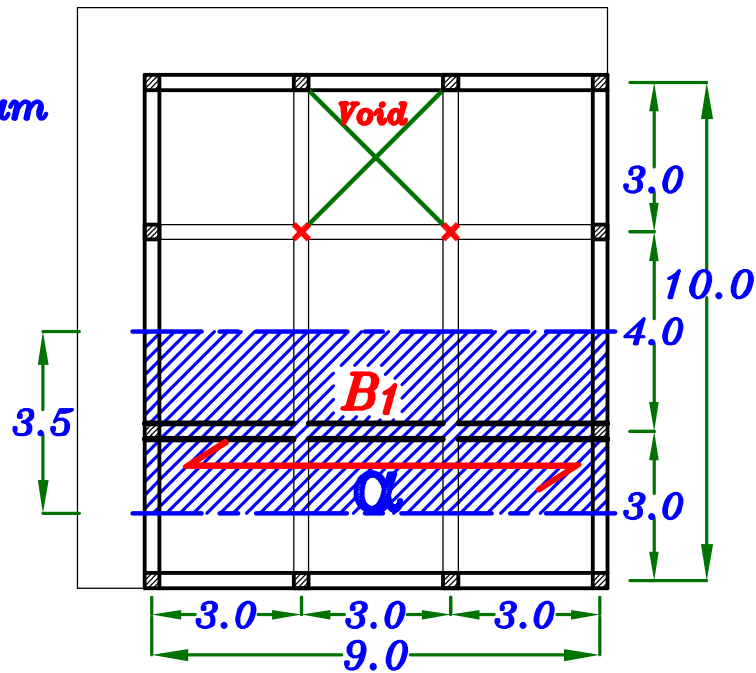


B_1 α Direction.

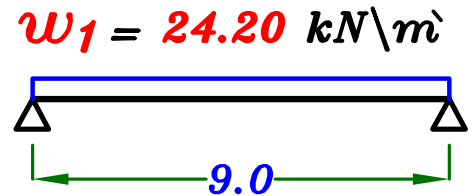
d – Get the Loads on the Panelled Beam & Calculate the B.M.

$$\alpha = 3.5 \text{ m}$$

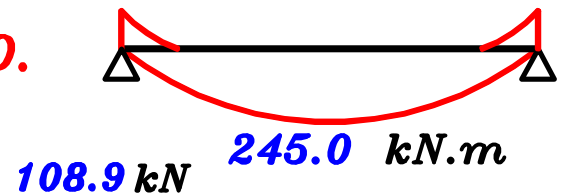
$$\begin{aligned} w_1 &= w_{av.} * \alpha * \alpha \\ &= 11.47 * 3.5 * 0.603 \\ &= 24.20 \text{ kN/m} \end{aligned}$$



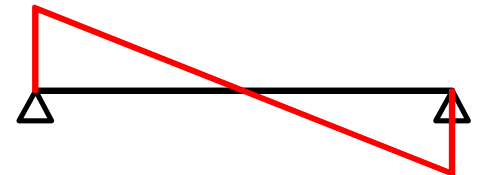
$$M = 24.20 * \frac{9.0^2}{8} = 245.0 \text{ kN.m}$$



B.M.D.



S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

$$X = 3.0 \text{ m} , \quad \frac{L}{2} = 5.0 \text{ m}$$

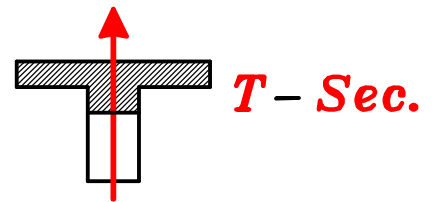
$$\theta_{B_1} = \frac{3.0}{5.0} * 90^\circ = 54^\circ$$

$$M_1 = 245.0 * \frac{\sin 54^\circ}{\sin 90^\circ} = 198.2 \text{ kN.m}$$

F – Design the Panelled Beam. *B*₁

α Direction. ∴ Cover = 50 mm

$$t = 600 \text{ mm} \quad d = 600 - 50 = 550 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = 3.5 \text{ m} = 3500 \text{ mm} \\ 16 t_s + b = 16 * 120 + 250 = 2170 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{9000}{5} + 250 = 2050 \text{ mm} \end{array} \right\} \quad \boxed{B = 2050 \text{ mm}}$$

$$550 = C_1 \sqrt{\frac{198.2 * 10^6}{25 * 2050}} \rightarrow C_1 = 8.91 \rightarrow J = 0.826$$

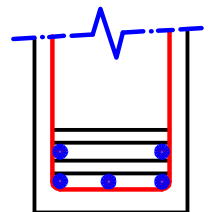
$$A_s = \frac{198.2 * 10^6}{0.826 * 360 * 550} = 1211 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1211 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 550 = 429.7 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1211 \text{ mm}^2 \quad \boxed{5 \phi 18}$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{250 - 25}{18 + 25} = 5.23 = 5.0 \text{ bars}$$



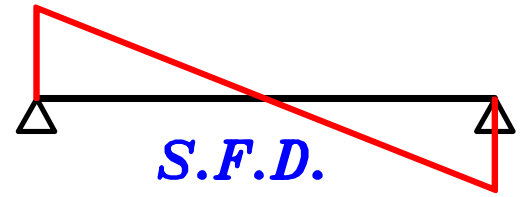
$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (121 \rightarrow 242 \text{ mm}^2) \quad \boxed{2 \phi 10}$$

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

108.9 kN



$$q_s = \frac{Q_{max}}{b d} = \frac{108.9 * 10^3}{250 * 550} = 0.792 \text{ N/mm}^2 \therefore q_s < q_{cu}$$

\therefore Use min. Shear RFT.

5 ϕ 8 m

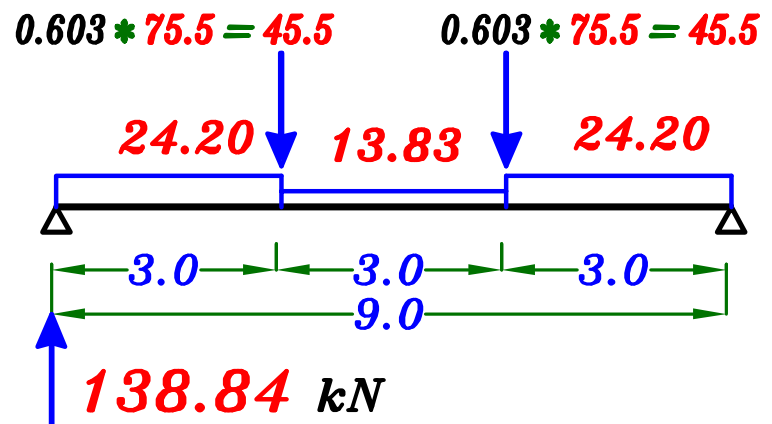
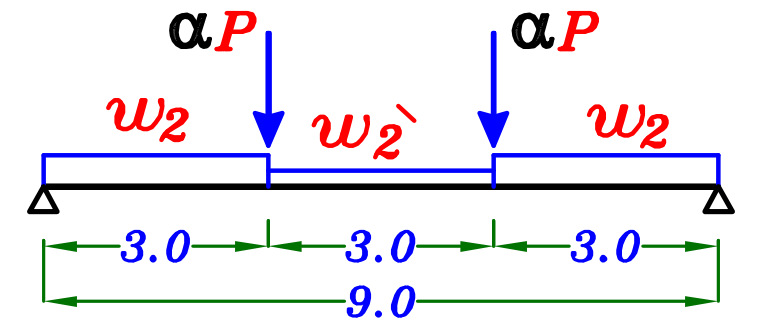
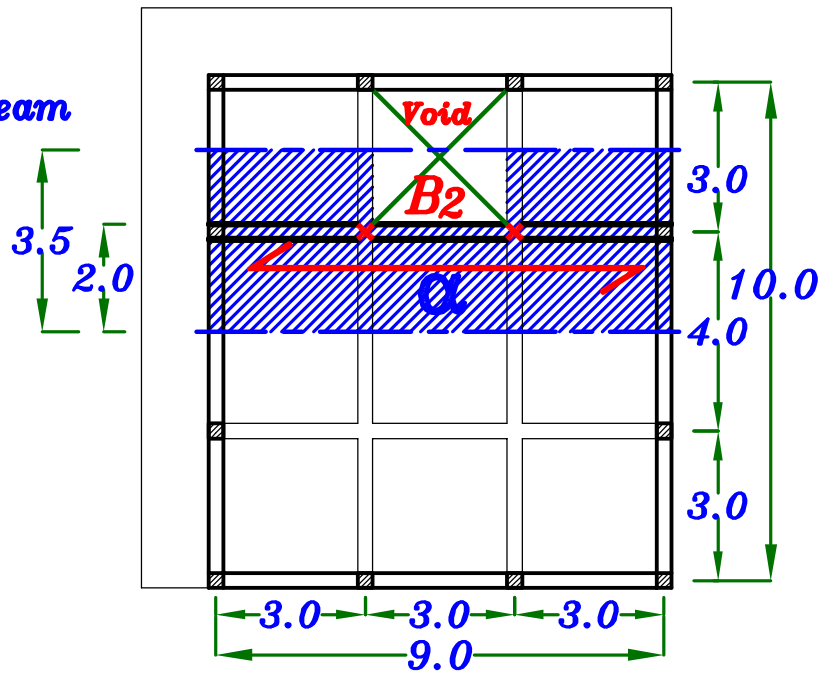
B₂ α Direction.

d– Get the Loads on the Panelled Beam
& Calculate the B.M.

$$\alpha_1 = 3.5 \text{ m} , \quad \alpha_2 = 2.0 \text{ m}$$

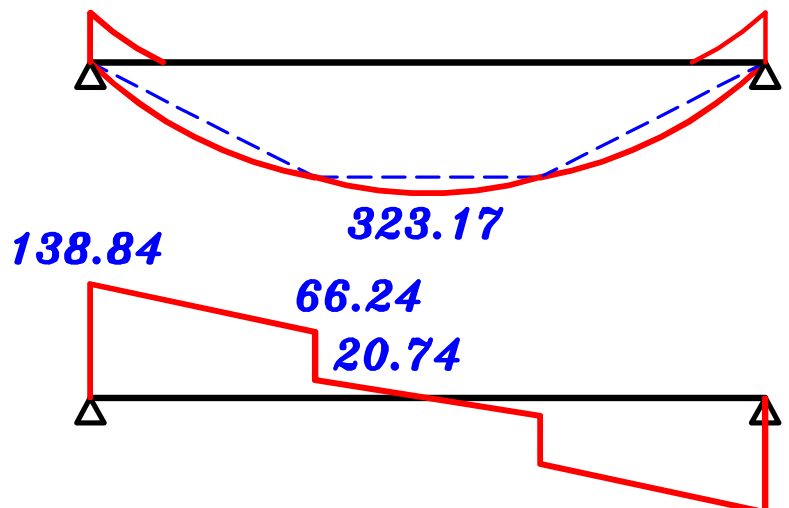
$$\begin{aligned} w_2 &= w_{av.} * \alpha_1 * \alpha \\ &= 11.47 * 3.5 * 0.603 \\ &= 24.20 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} w_2' &= w_{av.} * \alpha_2 * \alpha \\ &= 11.47 * 2.0 * 0.603 \\ &= 13.83 \text{ kN/m} \end{aligned}$$



B.M.D.

$$M = 323.17 \text{ kN.m}$$



S.F.D.

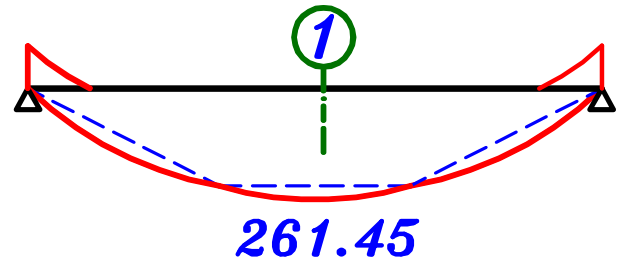
e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

$$X = 3.0 \text{ m} , \quad \frac{L}{2} = 5.0 \text{ m}$$

$$\theta_{B_2} = \frac{3.0}{5.0} * 90^\circ = 54^\circ$$

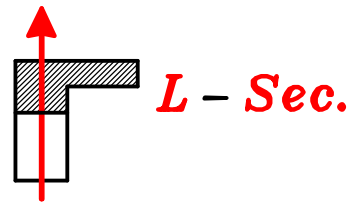
$$M_2 = 323.17 * \frac{\sin 54^\circ}{\sin 90^\circ} = 261.45 \text{ kN.m}$$

F– Design the Panelled Beam. B_2



α Direction. $\therefore \text{Cover} = 50 \text{ mm}$

$$t = 600 \text{ mm} \quad d = 600 - 50 = 550 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 2.0 \text{ m} = 2000 \text{ mm} \\ 6 t_s + b = 6 * 120 + 250 = 970 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{9000}{10} + 250 = 1150 \text{ mm} \end{array} \right\} \quad \boxed{B = 970 \text{ mm}}$$

$$550 = C_1 \sqrt{\frac{261.45 * 10^6}{25 * 970}} \rightarrow C_1 = 5.29 \rightarrow J = 0.826$$

$$A_s = \frac{261.45 * 10^6}{0.826 * 360 * 550} = 1598 \text{ mm}^2$$

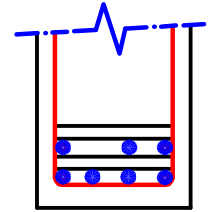
Check $A_{s_{min}}$

$$A_{s_{req.}} = 1598 \text{ mm}^2$$

$$\mu_{min} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 550 = 429.7 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1598 \text{ mm}^2 \quad \textcircled{7 \phi 18}$$

$$n = \frac{b - 25}{\phi + 25} = \frac{250 - 25}{18 + 25} = 5.23 = 5.0 \text{ bars}$$



$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (159 \rightarrow 318 \text{ mm}^2)$$

$$\textcircled{3 \phi 10}$$

Check Shear.

138.84

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

S.F.D.

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

$$q_s = \frac{Q_{max}}{b d} = \frac{138.84 * 10^3}{250 * 530} = 1.0 \text{ N/mm}^2 \therefore q_{cu} < q_s < q_{u_{max}}$$

$$q_s - \frac{q_{cu}}{2} = \frac{n A_s (F_y \delta_s)}{b S} \xrightarrow{\text{Take}} n = 2, \phi 8 = 50.3 \text{ mm}^2$$

$$1.0 - \frac{0.98}{2} = \frac{2 (50.3) (240 \delta 1.15)}{250 * S} \longrightarrow S = 164.6 \text{ mm}$$

$$\text{No. of stirrups/m} = \frac{1000}{S} = \frac{1000}{164.6} = 6.07 \text{ Use } \textcircled{7 \phi 8/m}$$

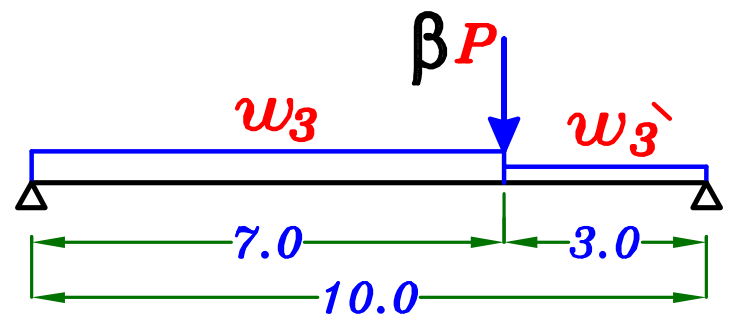
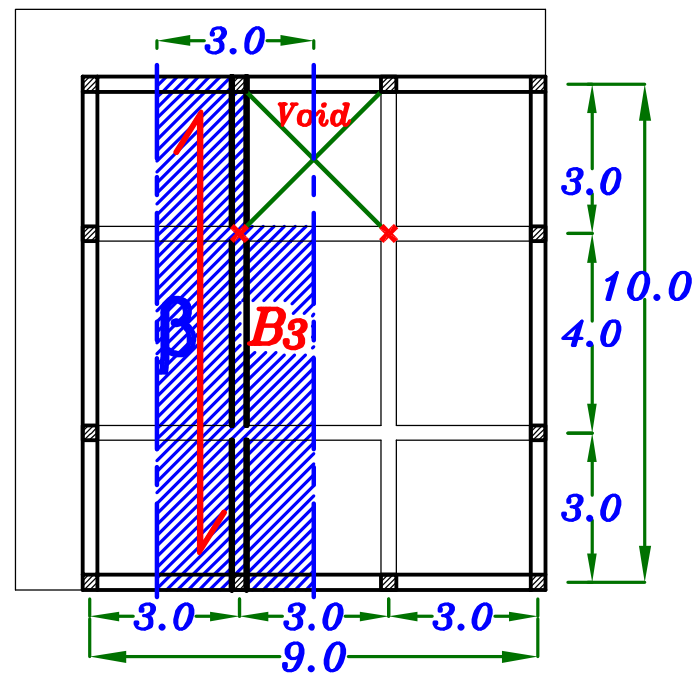
B_3 β Direction.

d– Get the Loads on the Panelled Beam & Calculate the B.M.

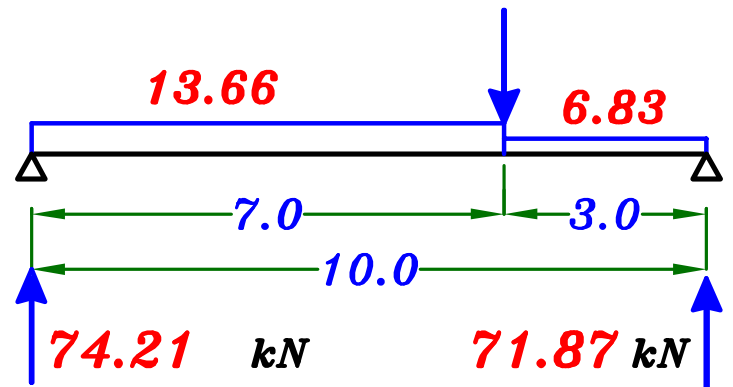
$$b_1 = 3.0 \text{ m} , b_2 = 1.5 \text{ m}$$

$$\begin{aligned} w_3 &= w_{av.} * b_1 * \beta \\ &= 11.47 * 3.0 * 0.397 \\ &= 13.66 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} w_3' &= w_{av.} * b_2 * \beta \\ &= 11.47 * 1.5 * 0.397 \\ &= 6.83 \text{ kN/m} \end{aligned}$$

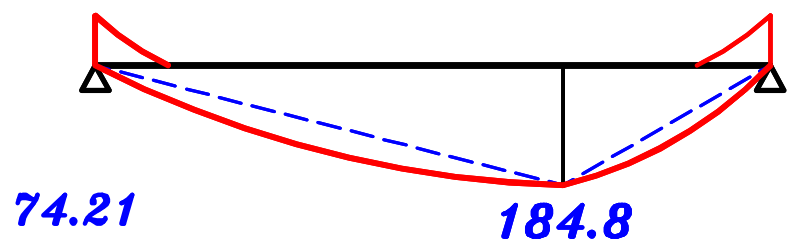


$$0.397 * 75.5 = 29.97$$

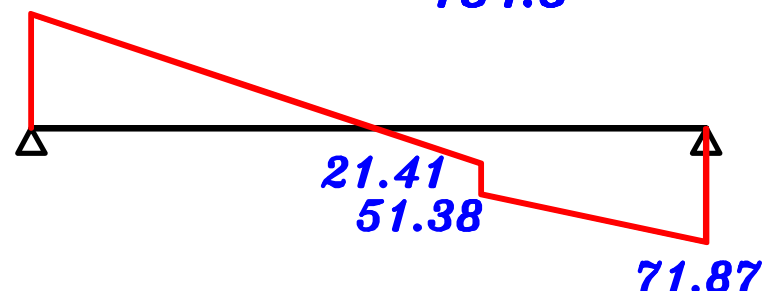


B.M.D.

$M = 184.8 \text{ kN.m}$



S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90}\right)$

$$X = 3.0 \text{ m} , \quad \frac{L}{2} = 4.5 \text{ m}$$

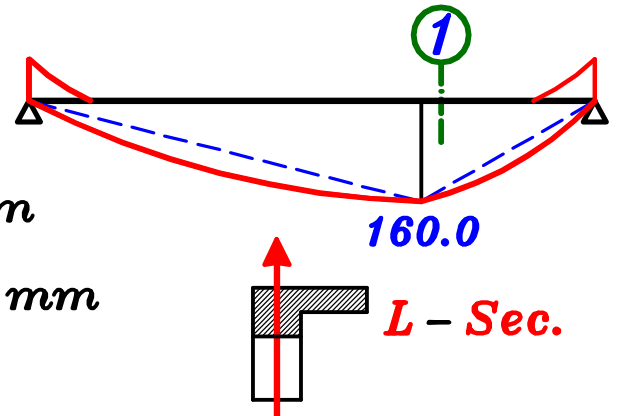
$$\theta_{B_2} = \frac{3.0}{4.5} * 90^\circ = 60^\circ$$

$$M_2 = 184.8 * \frac{\sin 60^\circ}{\sin 90^\circ} = 160.0 \text{ kN.m}$$

F– Design the Panelled Beam B_2

β Direction. $\therefore \text{Cover} = 70 \text{ mm}$

$$t = 600 \text{ mm} \quad d = 600 - 70 = 530 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = 1.5 \text{ m} = 1500 \text{ mm} \\ 6 t_s + b = 6 * 120 + 250 = 970 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{10000}{10} + 250 = 1250 \text{ mm} \end{array} \right\}$$

$$B = 970 \text{ mm}$$

$$530 = C_1 \sqrt{\frac{160.0 * 10^6}{25 * 970}} \rightarrow C_1 = 6.52 \rightarrow J = 0.826$$

$$A_s = \frac{160.0 * 10^6}{0.826 * 360 * 530} = 1015 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1015 \text{ mm}^2$

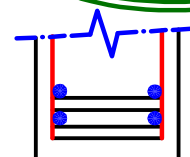
$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y}\right) b d = \left(0.225 * \frac{\sqrt{25}}{360}\right) 250 * 530 = 414.06 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1015 \text{ mm}^2$$

$$4 \phi 18$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (101 \rightarrow 202 \text{ mm}^2)$$

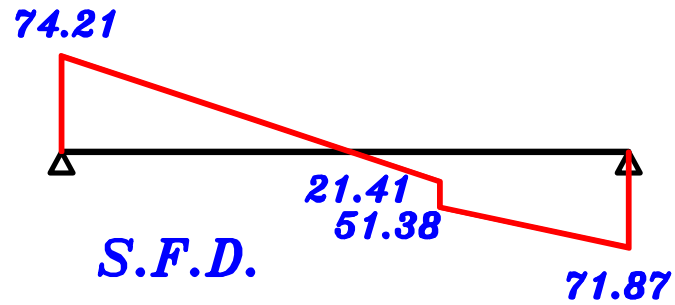
$$2 \phi 10$$



Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

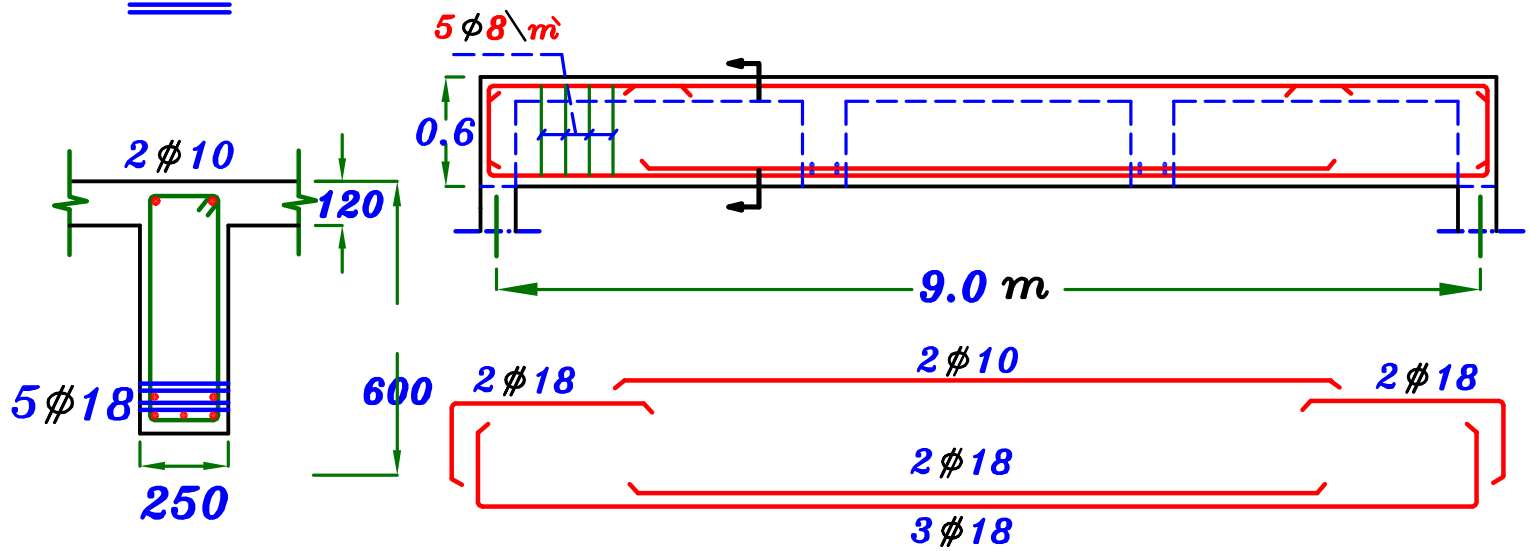


$$q_s = \frac{Q_{max}}{b d} = \frac{74.21 * 10^3}{250 * 530} = 0.56 \text{ N/mm}^2 \quad \therefore q_s < q_{cu}$$

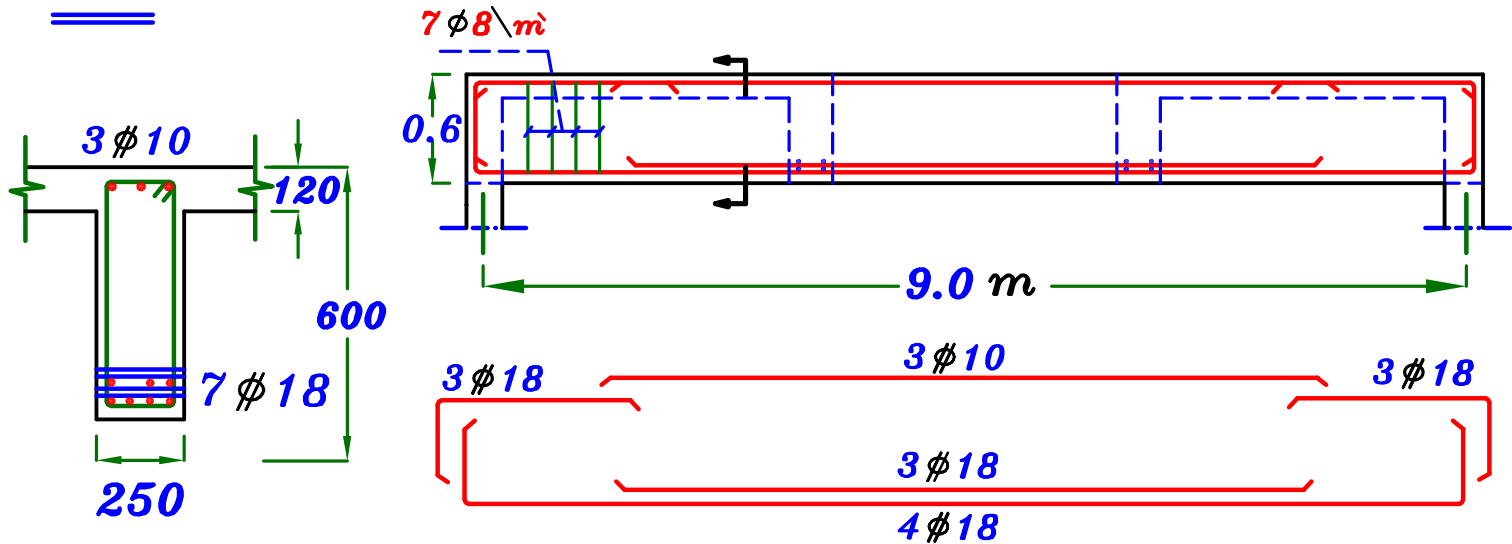
\therefore Use min. Shear RFT.

$5 \phi 8 \text{ m}$

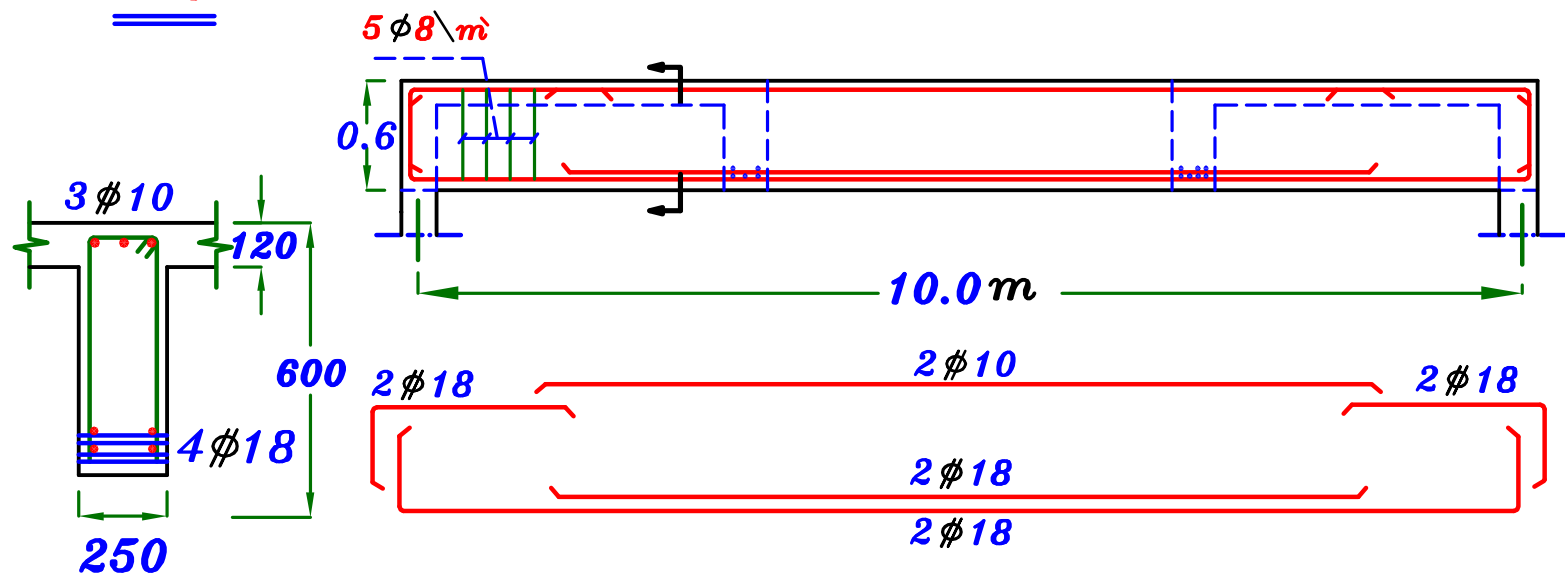
B₁



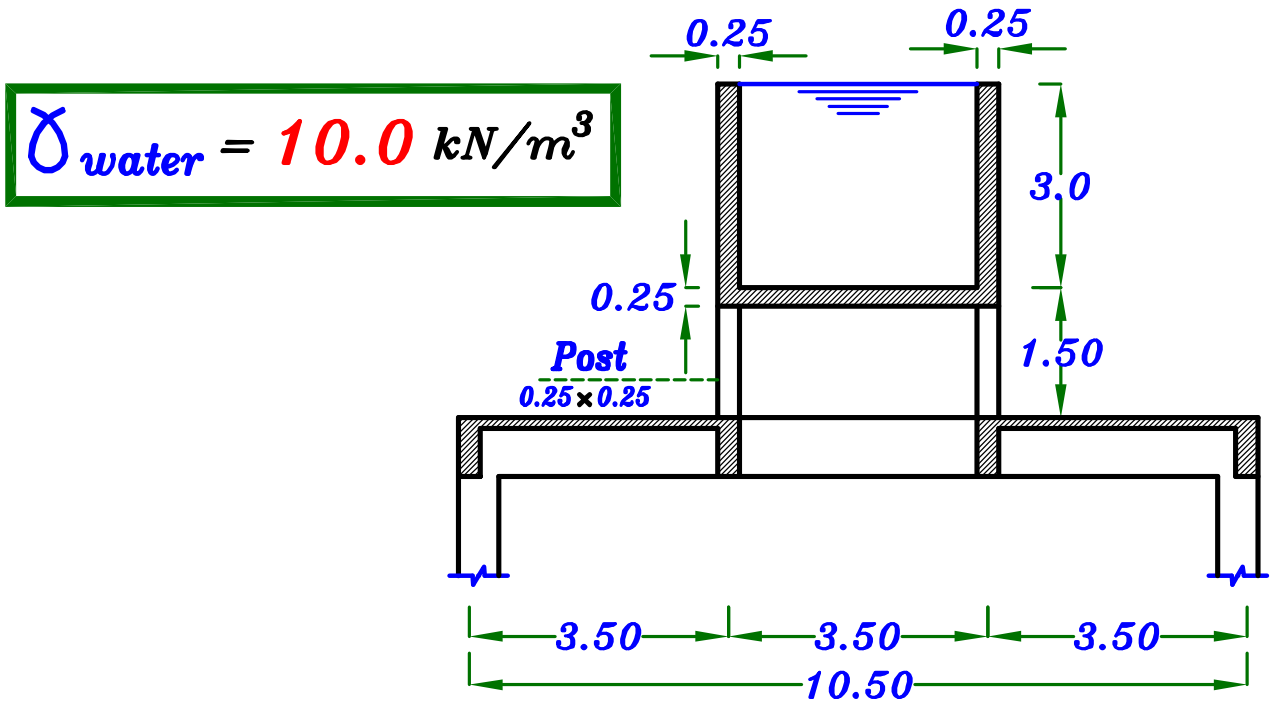
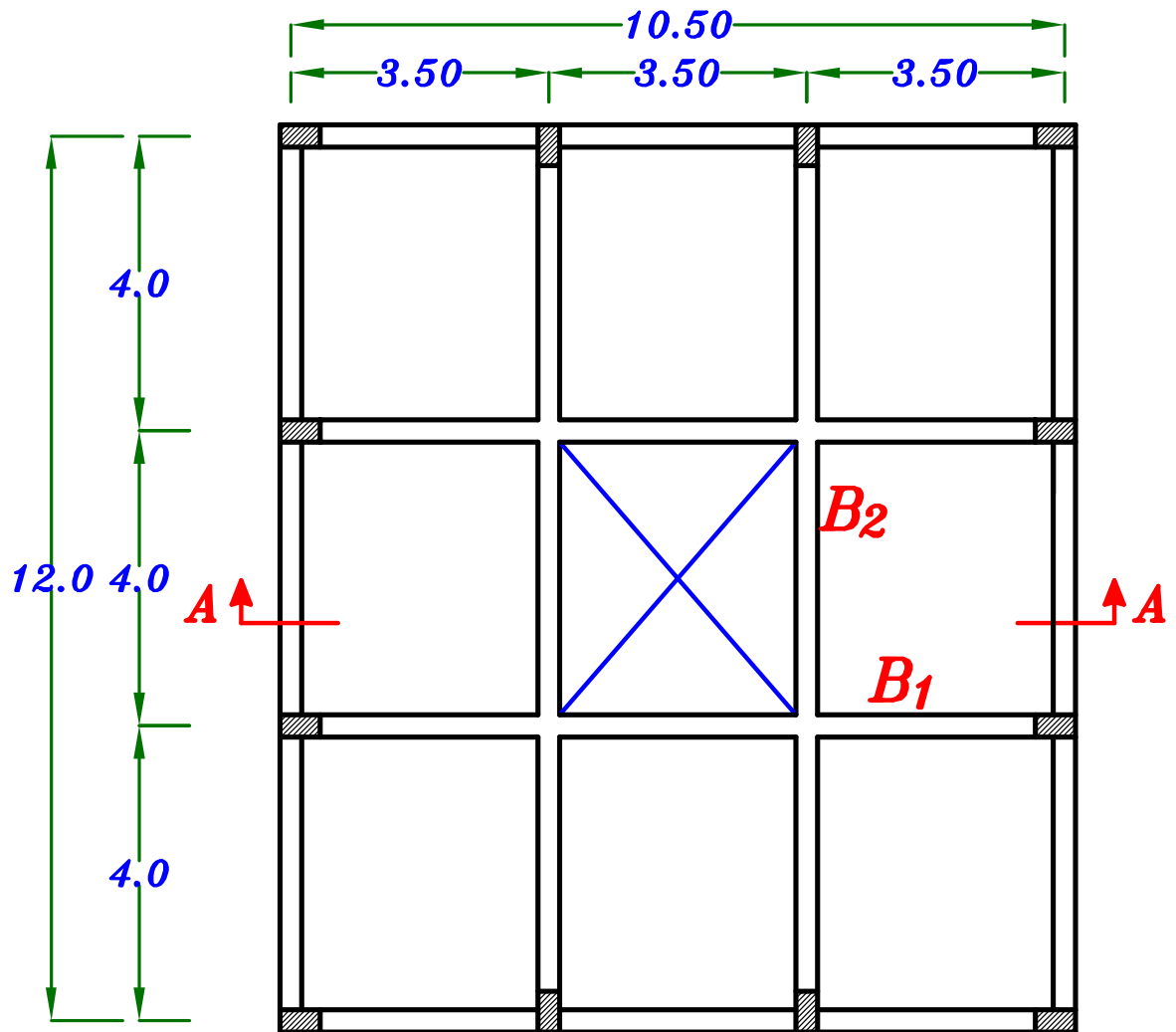
B₂



B₃



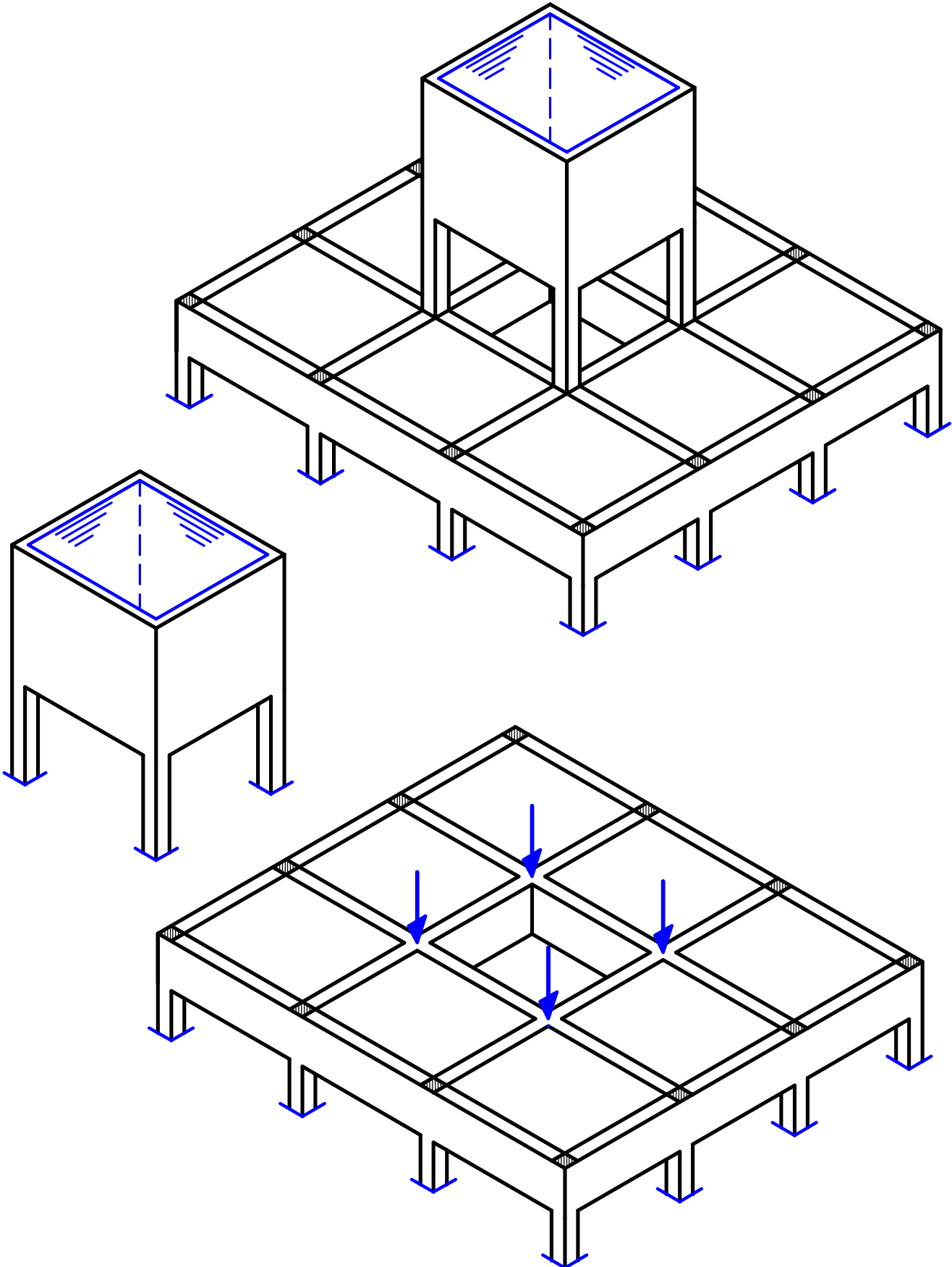
Example.

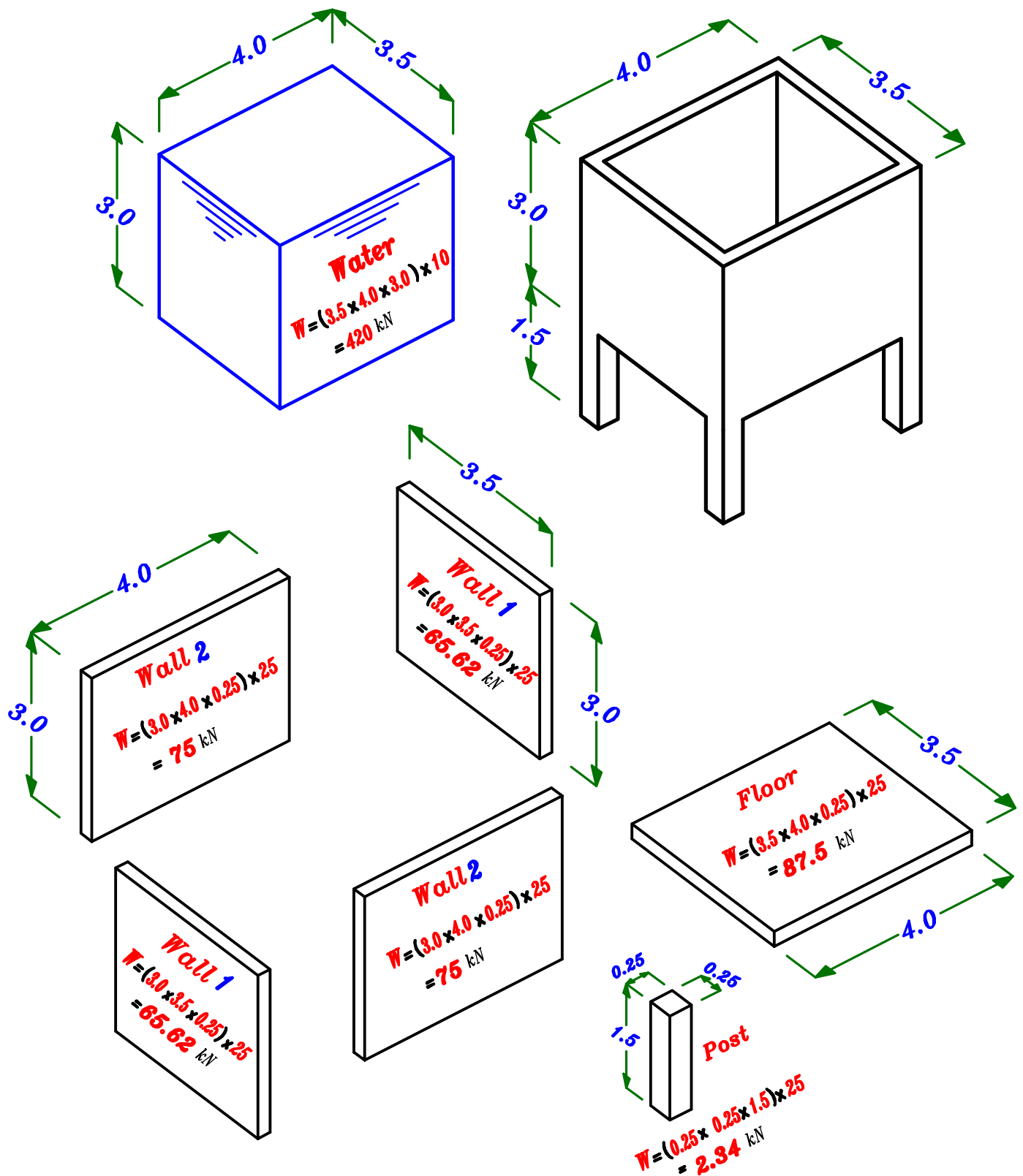


Design the Panelled Beams B_1, B_2

فكره المسأله

الوزن الكلى للخزان الماء و وزن الماء يتوزع على **4 Posts** بالتساوى
و يكون حمل ال **Post** الواحد حمل مركز محمول على الكمرات ال **Panelled B_1 & B_2**
و يتوزع الحمل المركز على الكمرات بنسبتى α , β





Total weight of the tank

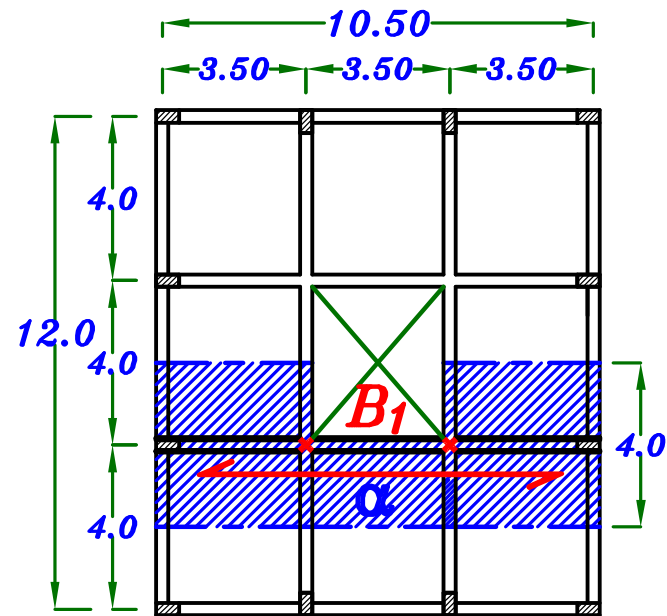
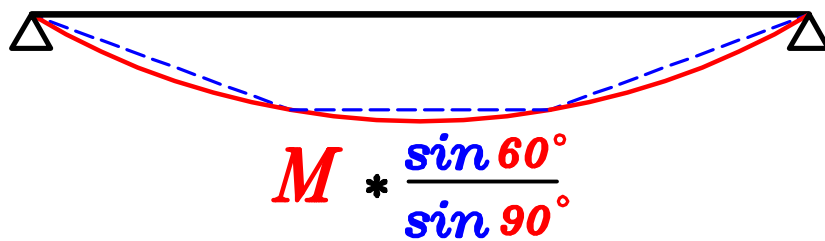
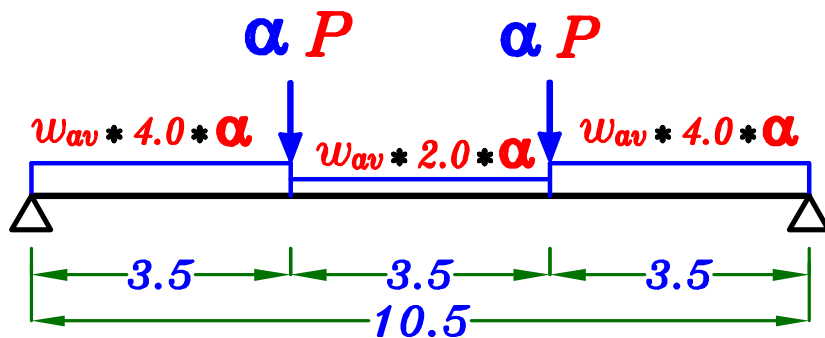
$$\begin{aligned}
 & \text{U.L. Water} \quad \text{Walls 1} \quad \text{Walls 2} \quad \text{Floor} \quad \text{posts} \\
 & = 1.5 \left[420 + (2 \times 65.62) + (2 \times 75.0) + 87.5 + (4 \times 2.34) \right] = 1197.15 \text{ kN}
 \end{aligned}$$

Load on one post.

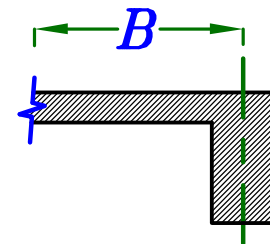
$$P = \frac{1197.15}{4.0} = 299.28 \text{ kN}$$

B_1

$$\Theta_{B1} = \frac{4.0}{6.0} * 90^\circ = 60^\circ$$



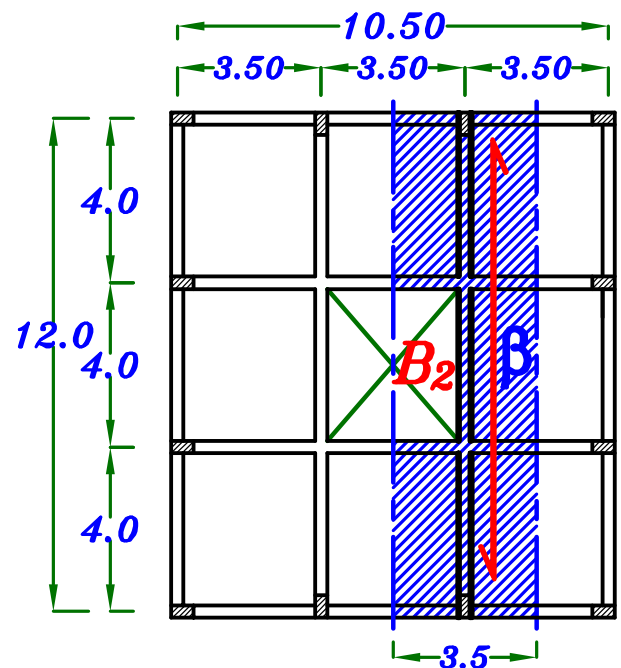
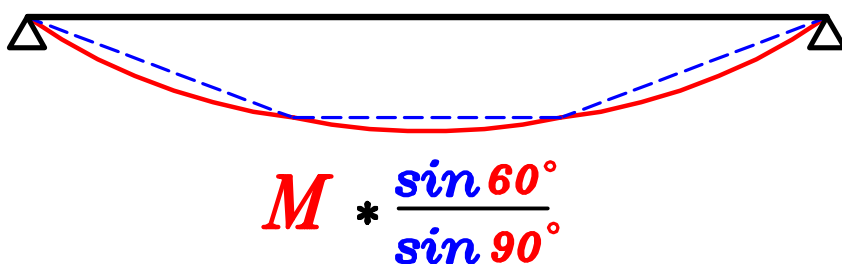
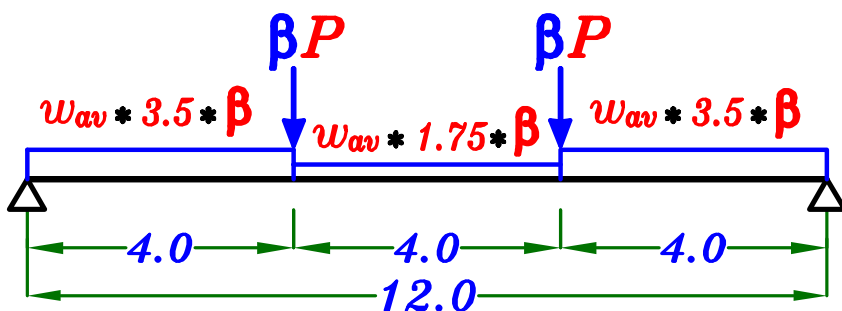
Designed as **L-sec.**



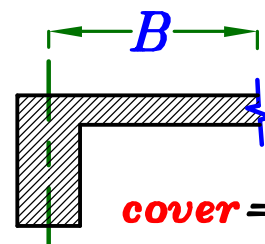
cover = 50 mm

B_2

$$\Theta_{B2} = \frac{3.5}{5.25} * 90^\circ = 60^\circ$$

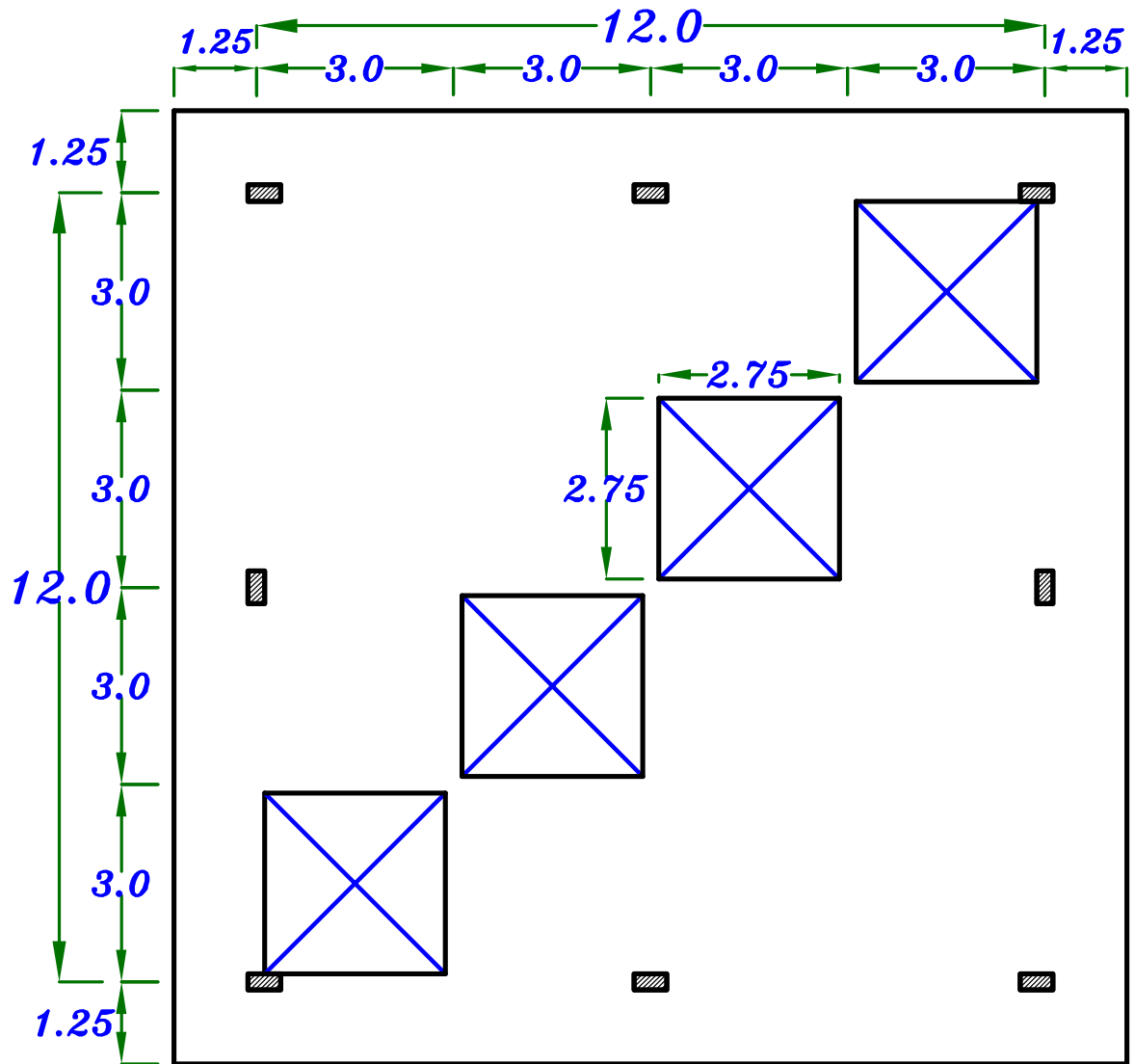


Designed as **L-sec.**



cover = 70 mm

Example.



Data.

$$F_{cu} = 25 \text{ N/mm}^2$$

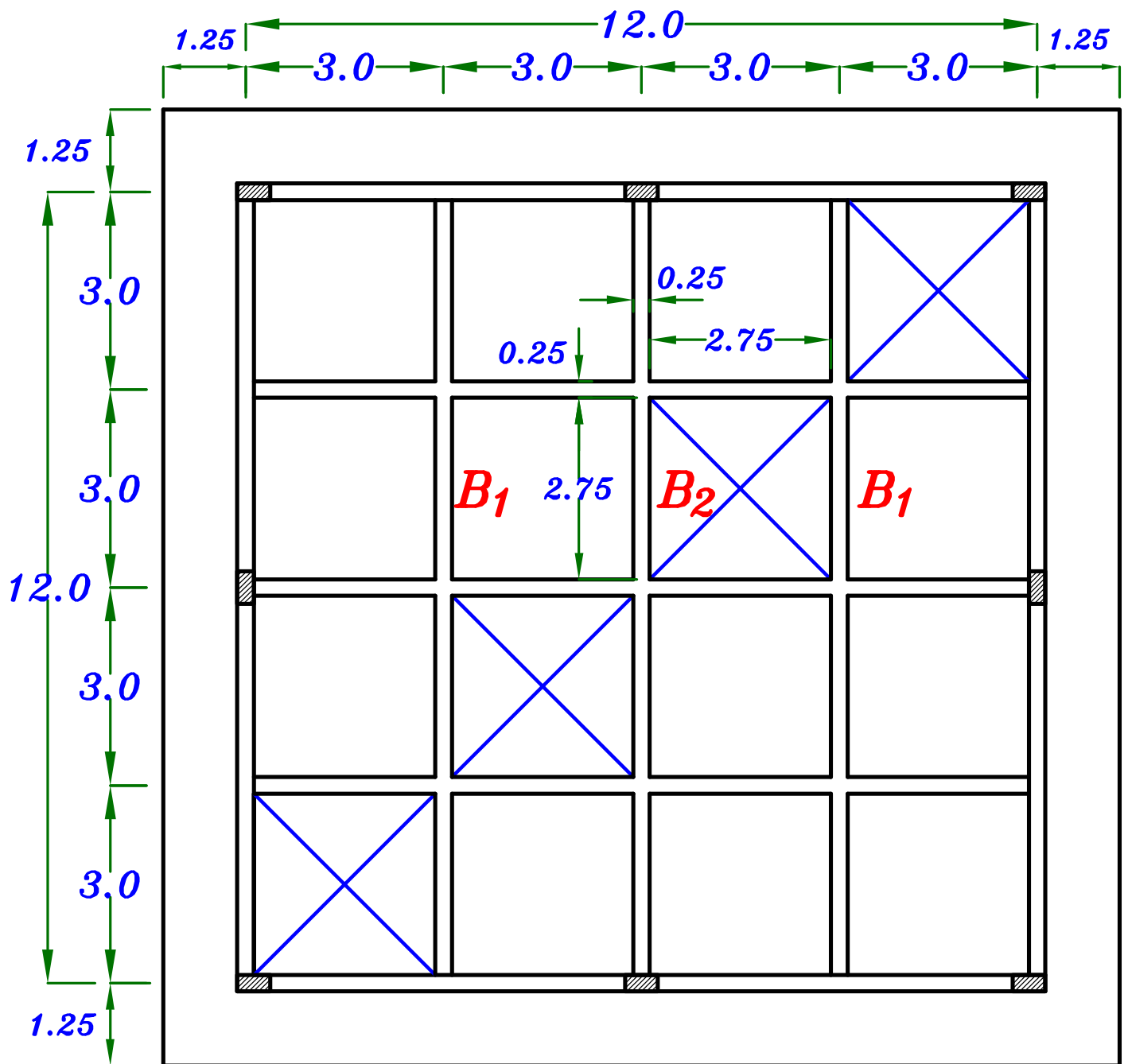
$$F_y = 360 \text{ N/mm}^2$$

$$F.C. + L.L. = 5.0 \text{ kN/m}^2$$

Req.

- ① Choose a system of slabs and panelled beams to cover this area.
- ② Design all Panelled Beams.
- ③ Draw Details of RFT. of the beams
in elevation & cross sections.

① Choose a system of slabs and panelled beams to cover this area.



Design of Panelled Beams.

1 - Choose the Thickness of the Slab. (t_s).

S_1 two way $L_s = 3.0$ m

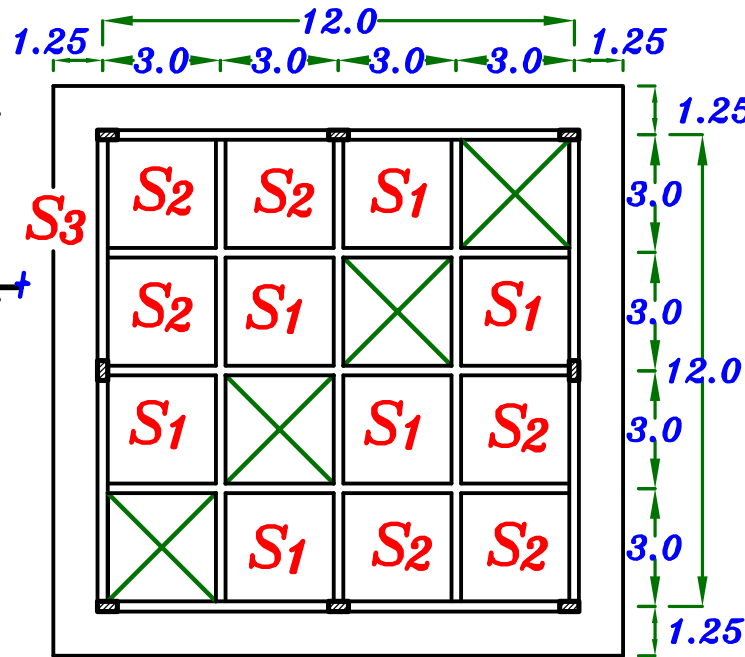
$$t_s = \frac{3000}{40} = 75.0 \text{ mm}$$

S_2 two way $L_s = 3.0$ m

$$t_s = \frac{3000}{45} = 66.6 \text{ mm}$$

S_3 Cantilever $L_c = 1.25$ m

$$t_s = \frac{1250}{10} = 125 \text{ mm}$$



Take (t_s) the bigger value

$$t_s = 140 \text{ mm}$$

2 - Get the Loads on the Slab (w_s).

$$w_s = 1.5 (0.14 * 25 + 5.0) = 12.75 \text{ kN/m}^2$$

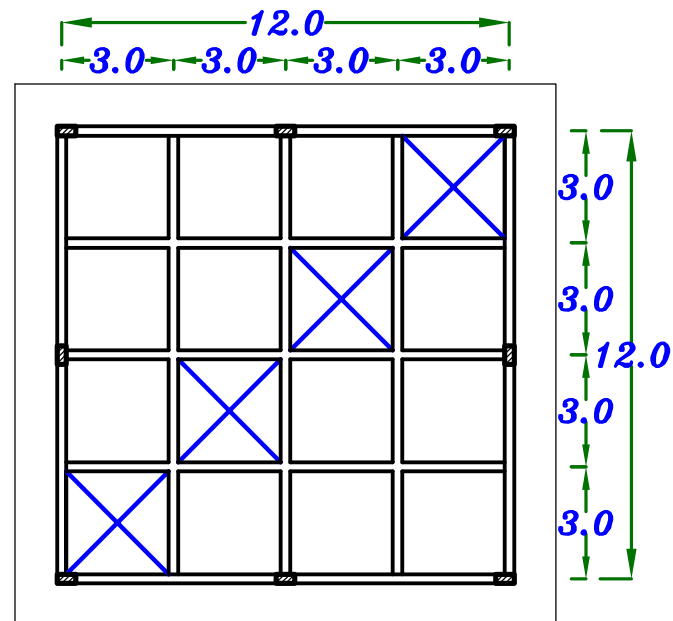
a - Get the Dimensions of the beam. (b, t)

Take $b = 0.25$ m

$$t = \frac{L_s}{16} = \frac{12.0}{16} = 0.75 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$t = 0.75 \text{ m}$$



b – Get the Loads on the Slab. (w_{av})

$$W_{av.} = W_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s - \text{Voids}}$$

$$w_{av.} = w_s + \frac{1.4 * b(t - t_s) [\text{مجموع أطوال الكمرات الداخلية}] * \delta_c}{L * L_s - Voids}$$

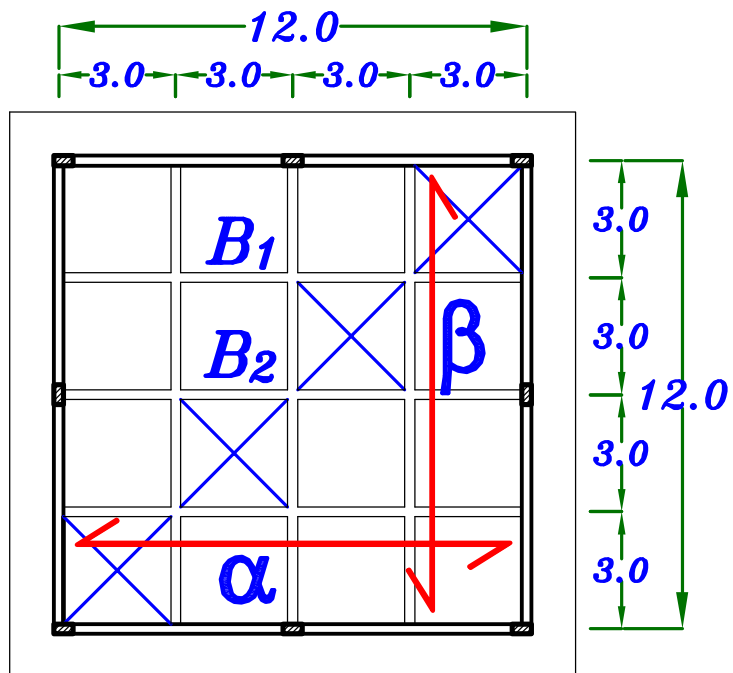
$$W_{av.} = 12.75 + \frac{1.4 * 0.25 (0.75 - 0.14) [3 * 12.0 + 3 * 12.0] * 25}{12.0 * 12.0 - 4.0 * (3.0 * 3.0)} = 16.31 \text{ kN/m}^2$$

C – Calculate α , β By using Grashoff.

$$r = \frac{m L}{m L_s} = \frac{(1.0) 12.0}{(1.0) 12.0} = 1.0$$

$$\alpha = \frac{r^4}{1+r^4} = \frac{(1.0)^4}{1+(1.0)^4} = 0.50$$

$$\beta = \frac{1}{1+r^4} = \frac{1}{1+(1.0)^4} = 0.50$$



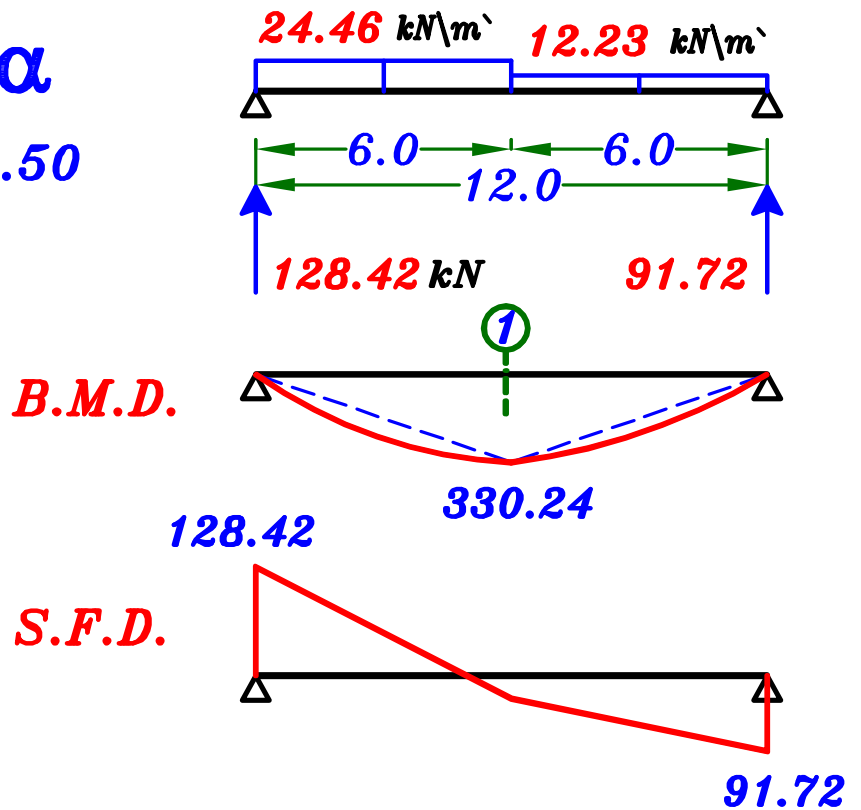
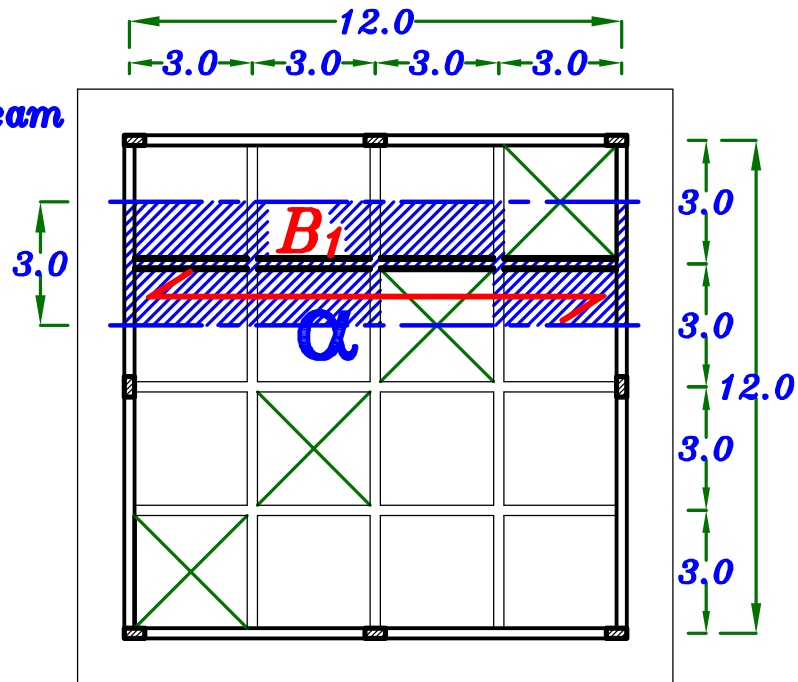
B_1 α Direction.

d – Get the Loads on the Panelled Beam & Calculate the B.M.

$$\alpha_1 = 3.0 \text{ m} , \alpha_2 = 1.5 \text{ m}$$

$$\begin{aligned} w_1 &= w_{av.} * \alpha_1 * \alpha \\ &= 16.31 * 3.0 * 0.50 \\ &= 24.46 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} w_2 &= w_{av.} * \alpha_2 * \alpha \\ &= 16.31 * 1.5 * 0.50 \\ &= 12.23 \text{ kN/m} \end{aligned}$$



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

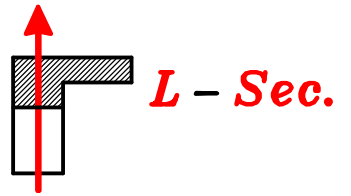
$$X = 3.0 \text{ m} , \frac{L}{2} = 6.0 \text{ m} \quad \theta_{B_1} = \frac{3.0}{6.0} * 90^\circ = 45^\circ$$

$$M_1 = 330.24 * \frac{\sin 45^\circ}{\sin 90^\circ} = 233.5 \text{ kN.m}$$

F- Design the Panelled Beam. B_1

\therefore Cover = 70 mm Symmetric

$$t = 750 \text{ mm} \quad d = 750 - 70 = 680 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 1.5 \text{ m} = 1500 \text{ mm} \\ 6 t_s + b = 6 * 140 + 250 = 1090 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{12000}{10} + 250 = 1450 \text{ mm} \end{array} \right\}$$

$$B = 1090 \text{ mm}$$

$$680 = C_1 \sqrt{\frac{233.5 * 10^6}{25 * 1090}} \rightarrow C_1 = 7.34 \rightarrow J = 0.826$$

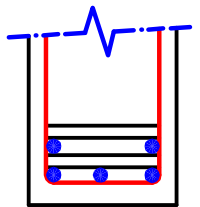
$$A_s = \frac{233.5 * 10^6}{0.826 * 360 * 680} = 1154.7 \text{ mm}^2$$

Check $A_{s \min}$ $A_{s \text{ req.}} = 1154.7 \text{ mm}^2$

$$\mu_{\min} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 680 = 531.2 \text{ mm}^2$$

$\therefore A_{s \text{ req.}} > \mu_{\min} b d \therefore$ Take $A_s = A_{s \text{ req.}} = 1154.7 \text{ mm}^2$ **5 ϕ 18**

$$n = \frac{b - 25}{\phi + 25} = \frac{250 - 25}{18 + 25} = 5.23 = 5.0 \text{ bars}$$



Stirrup Hangers = (0.1 \rightarrow 0.2) $A_s = (115 \rightarrow 230 \text{ mm}^2)$

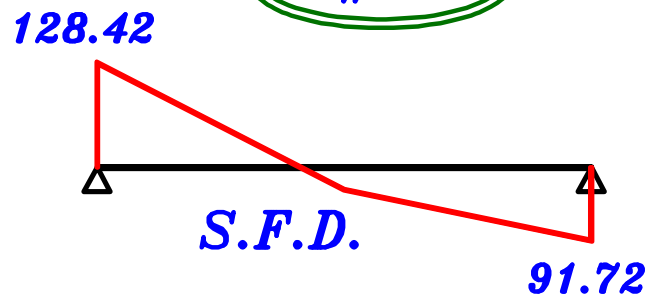
$$3 \phi 10$$

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u \text{ max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

$$q_s = \frac{Q_{\text{max}}}{b d} = \frac{128.42 * 10^3}{250 * 680} = 0.755 \text{ N/mm}^2 \therefore q_s < q_{cu}$$



\therefore Use min. Shear RFT.

$$5 \phi 8 \text{ m}$$

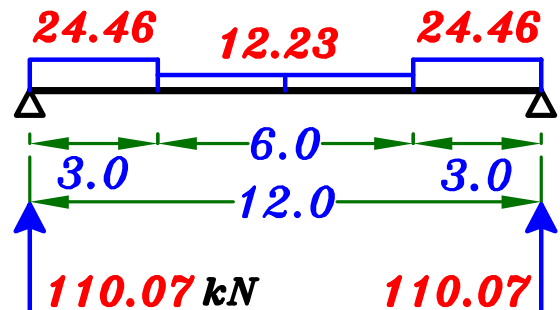
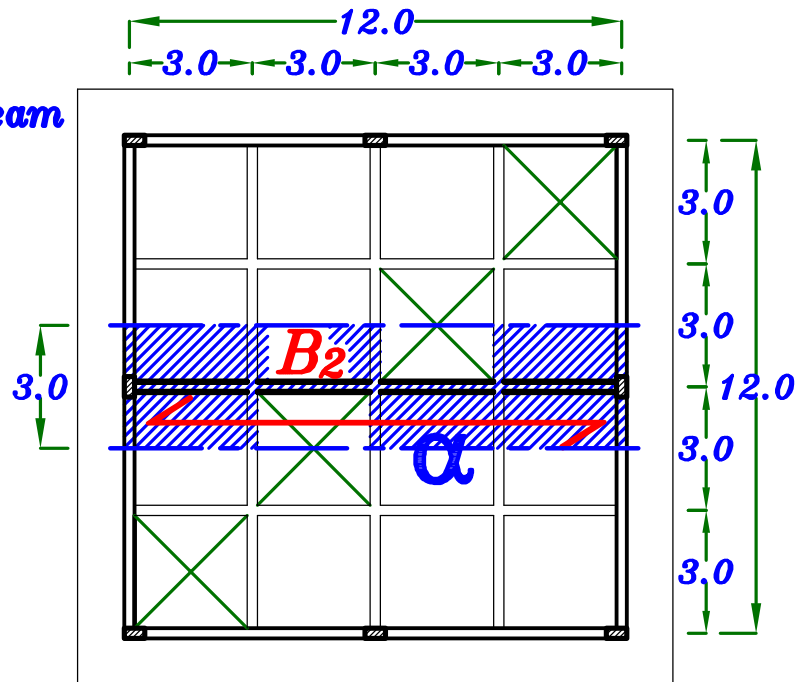
B₂ α Direction.

d- Get the Loads on the Panelled Beam & Calculate the B.M.

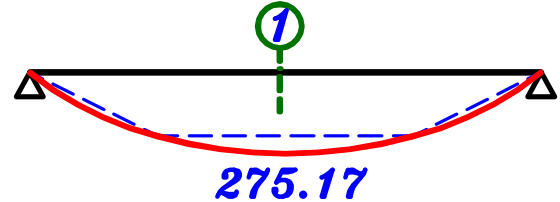
$$\alpha_1 = 3.0 \text{ m} , \quad \alpha_2 = 1.5 \text{ m}$$

$$\begin{aligned} w_2 &= w_{av.} * \alpha_1 * \alpha \\ &= 16.31 * 3.0 * 0.50 \\ &= 24.46 \text{ kN/m} \end{aligned}$$

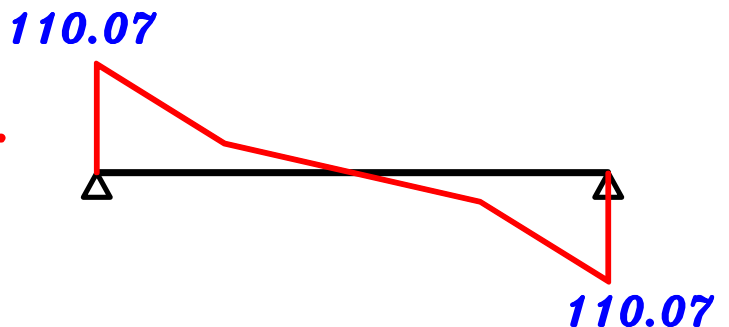
$$\begin{aligned} w_2' &= w_{av.} * \alpha_2 * \alpha \\ &= 16.31 * 1.5 * 0.50 \\ &= 12.23 \text{ kN/m} \end{aligned}$$



B.M.D.



S.F.D.



e - Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

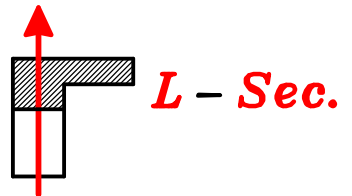
$$X = 6.0 \text{ m} , \quad \frac{L}{2} = 6.0 \text{ m} \quad \theta_{B_1} = \frac{6.0}{6.0} * 90^\circ = 90^\circ$$

$$M_1 = 275.17 * \frac{\sin 90^\circ}{\sin 90^\circ} = 275.17 \text{ kN.m}$$

F- Design the Panelled Beam. B_2

\therefore **Cover** = 70 mm Symmetric

$$t = 750 \text{ mm} \quad d = 750 - 70 = 680 \text{ mm}$$



L - Sec.

$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 1.5 \text{ m} = 1500 \text{ mm} \\ 6 t_s + b = 6 * 140 + 250 = 1090 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{12000}{10} + 250 = 1450 \text{ mm} \end{array} \right\} \quad \boxed{B = 1090 \text{ mm}}$$

$$680 = C_1 \sqrt{\frac{275.17 * 10^6}{25 * 1090}} \rightarrow C_1 = 6.76 \rightarrow J = 0.826$$

$$A_s = \frac{275.17 * 10^6}{0.826 * 360 * 680} = 1360.8 \text{ mm}^2$$

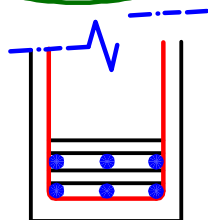
Check $A_{s \min.}$ $A_{s \text{ req.}} = 1360.8 \text{ mm}^2$

$$\mu_{\min} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 680 = 531.2 \text{ mm}^2$$

$\therefore A_{s \text{ req.}} > \mu_{\min} b d \therefore$ Take $A_s = A_{s \text{ req.}} = 1360.8 \text{ mm}^2$ **6 ϕ 18**

Stirrup Hangers = (0.1 \rightarrow 0.2) A_s = (136 \rightarrow 272 mm²)

3 ϕ 10

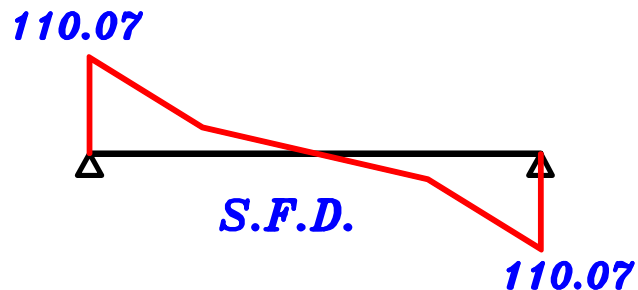


Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u \text{ max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

$$q_s = \frac{Q_{\text{max}}}{b d} = \frac{110.07 * 10^3}{250 * 680} = 0.64 \text{ N/mm}^2 \therefore q_s < q_{cu}$$

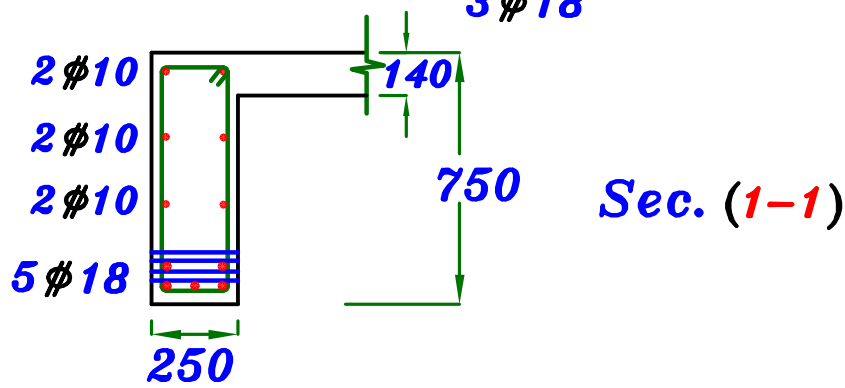
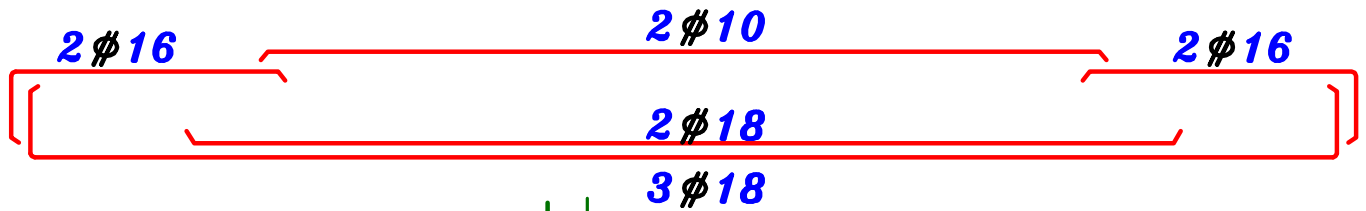
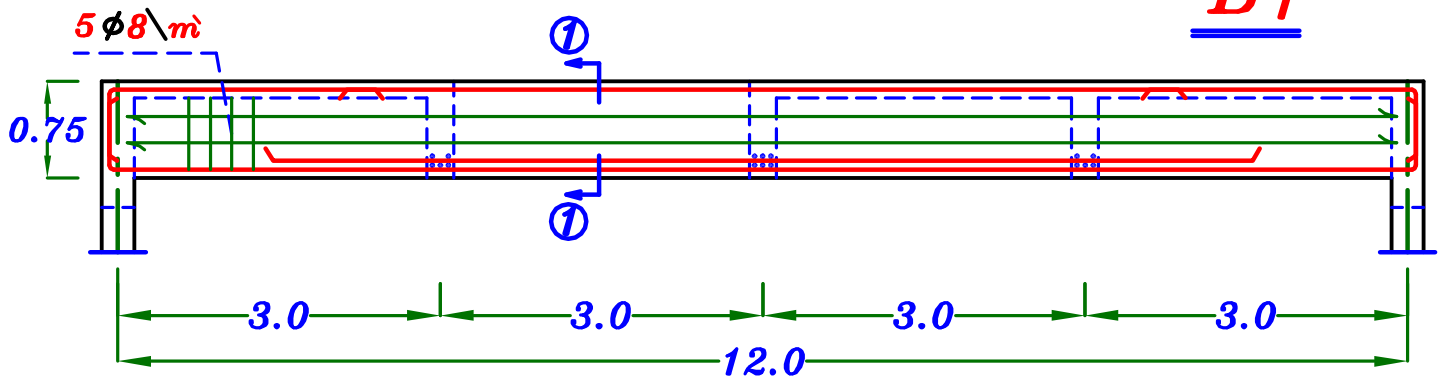


\therefore Use min. Shear RFT.

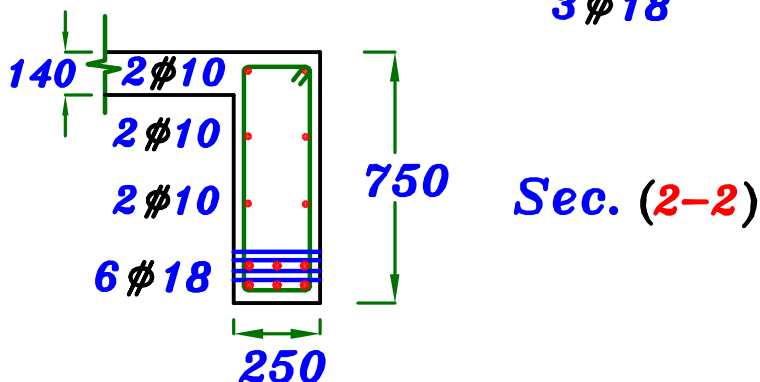
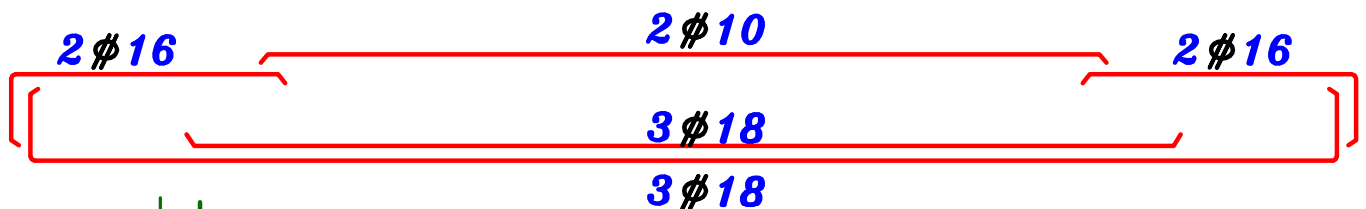
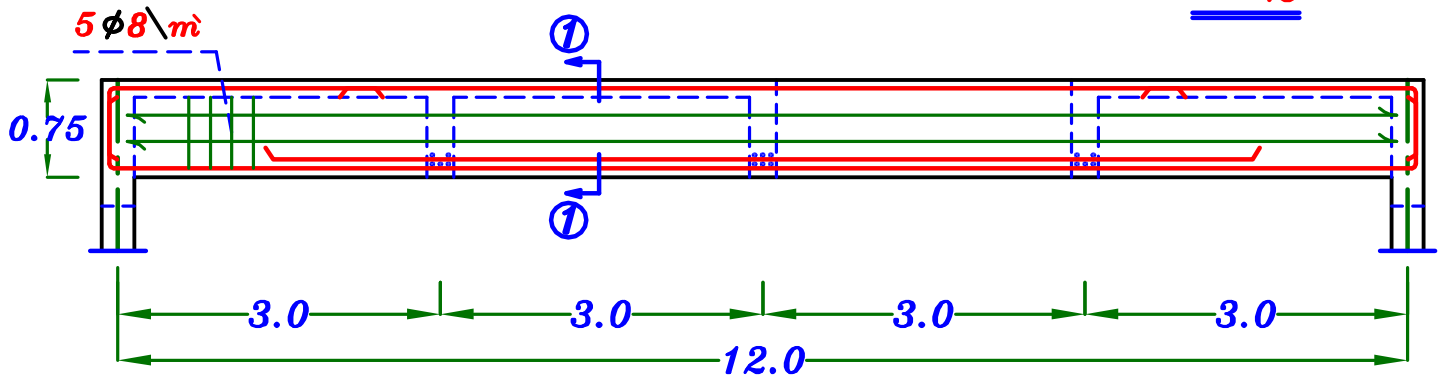
5 ϕ 8/m

Draw Details of RFT. For the Beams. (B_1, B_2)

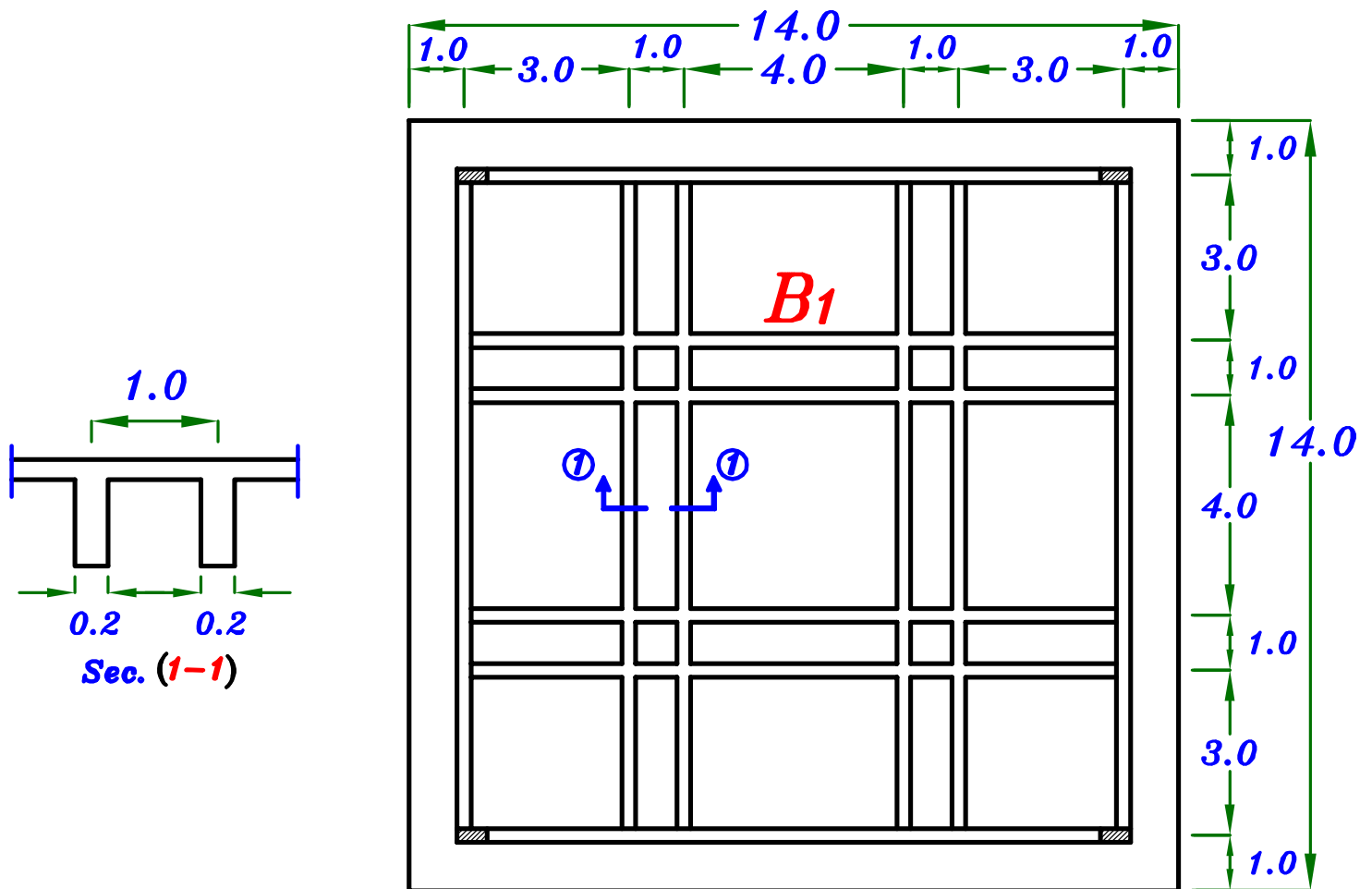
B_1



B_2



Example.



Data.

$$F_{cu} = 25 \text{ N/mm}^2 \quad F_y = 360 \text{ N/mm}^2$$

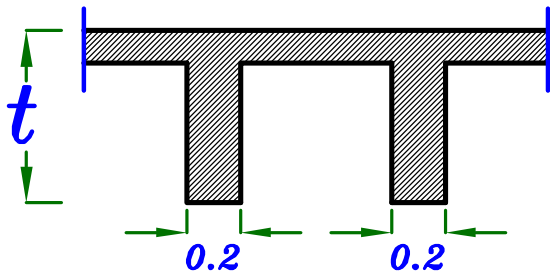
$$F.C. + L.L. = 3.0 \text{ kN/m}^2$$

Req.

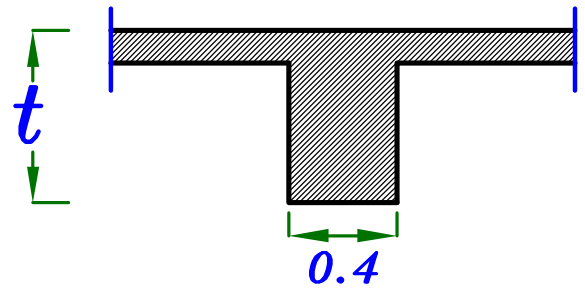
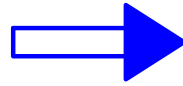
- ① Design the Slabs **as Solid Slabs.**
- ② Draw Details **of RFT.** of Slabs **in plan.**
- ③ Design Beam **B_1**
- ④ Draw Details **of RFT.** of the beam **in elevation & cross sections.**

فكره المسأله .

ممكن للتسهيل عند حساب الاحمال و تصميم كلا من البلاطه و الكمره اعتبار انه تم ضم الكمرتين المتجاورتين معا و اعتبارهم فى الحسابات كأنها كمره واحده .

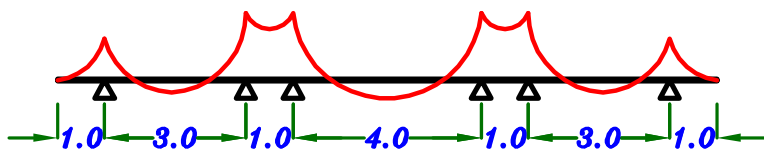
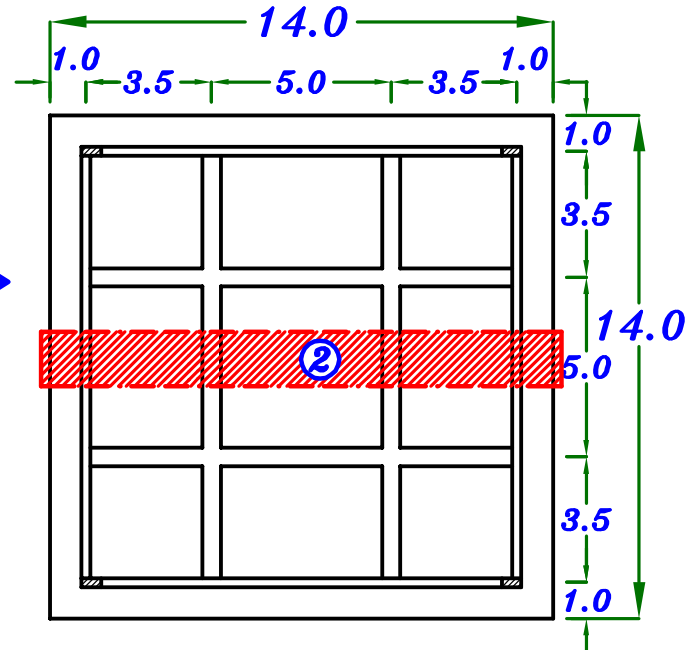
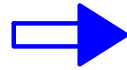
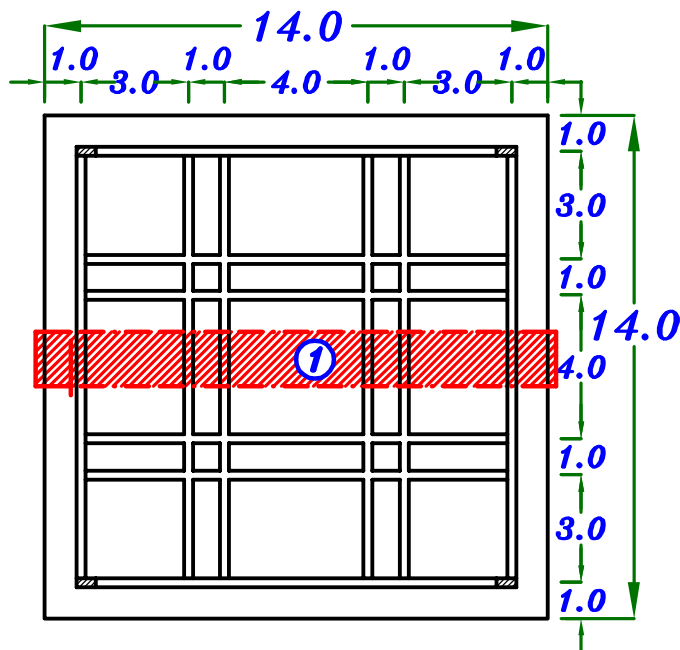


Sec. (1-1)

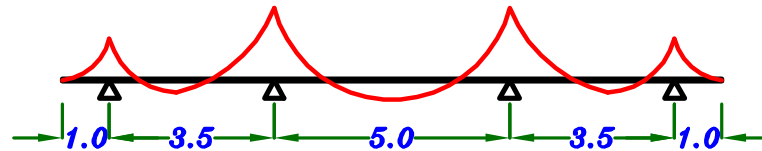


Sec. (1-1)

و ذلك أثناء حسابات الاحمال و التصميم فقط لكن عند رسم التسليح يجب ان نسلح على الشكل الاصلى . لان هذا ما سيتم تنفيذه فى الحقيقه



Strip ①



Strip ②

① Design the Slabs as Solid Slabs.

a - Choose the Thickness of the Slab. (t_s)

S_1 two way $L_s = 3.5$ m

$$t_s = \frac{3500}{45} = 77.7 \text{ mm}$$

S_2 two way $L_s = 3.5$ m

$$t_s = \frac{3500}{45} = 77.7 \text{ mm}$$

S_3 two way $L_s = 5.0$ m

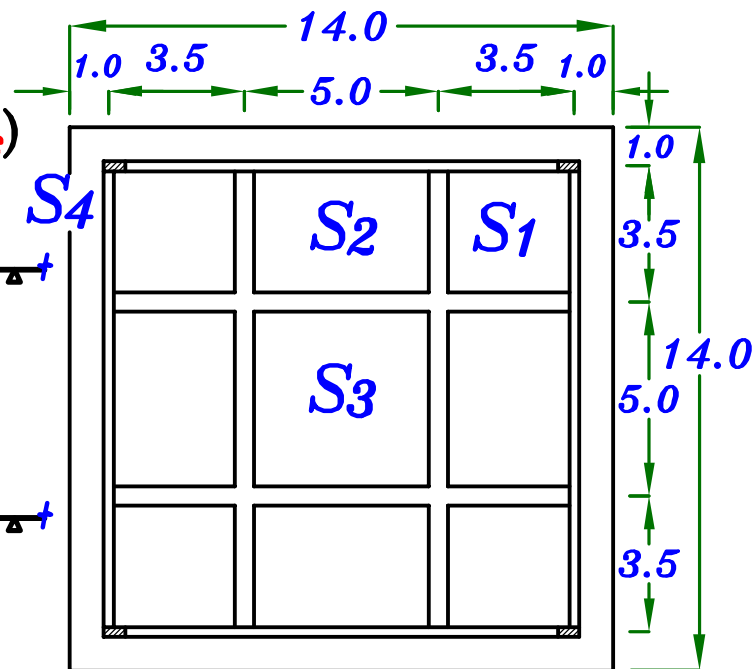
$$t_s = \frac{5000}{45} = 111.1 \text{ mm}$$

S_4 Cantilever $L_c = 1.0$ m

$$t_s = \frac{1000}{10} = 100 \text{ mm}$$

Take (t_s) the bigger value

$$t_s = 120 \text{ mm}$$

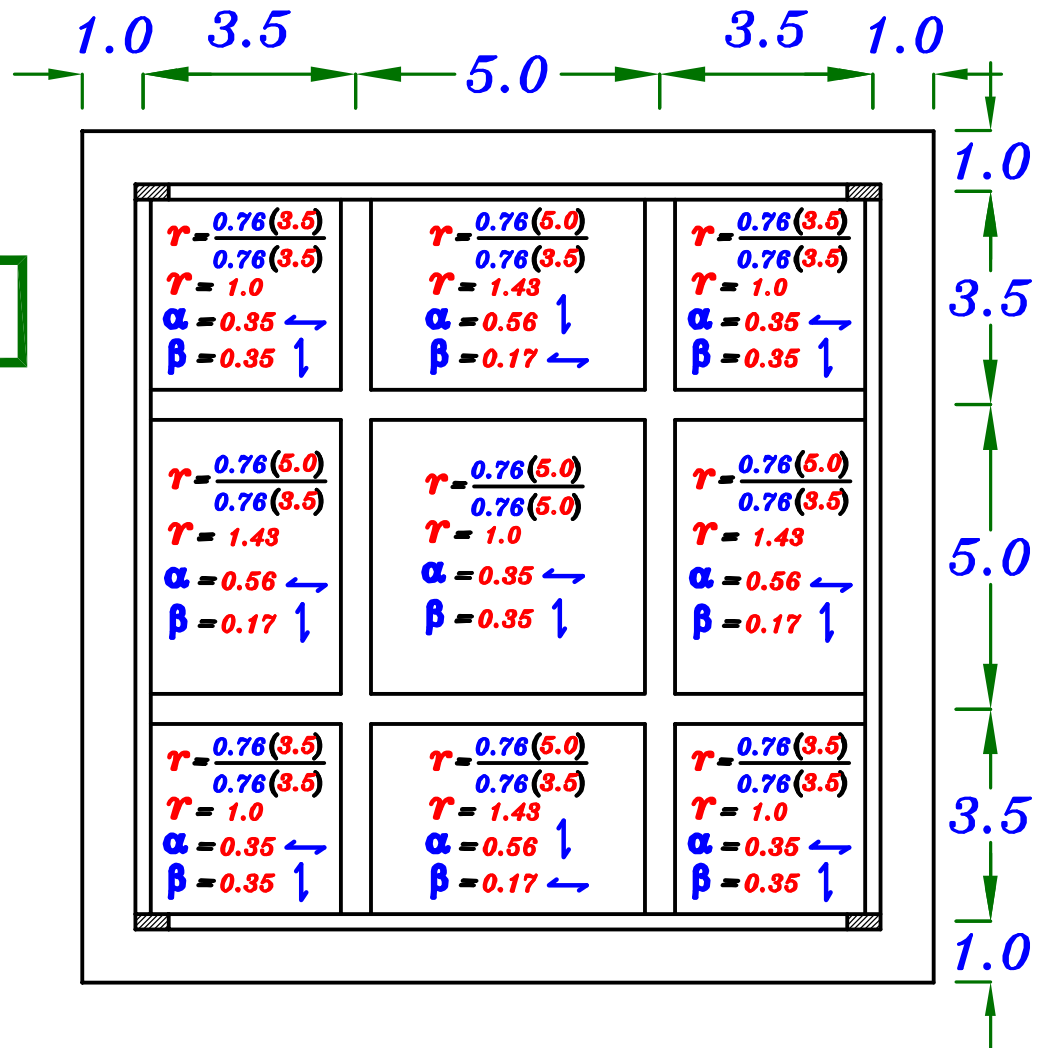


b - Get the Loads on the Slab (w_s).

$$w_s = 1.5 (t_s \delta_c + F.C. + L.L.) \text{ kN/m}^2$$

$$w_s = 1.5 (0.10 * 25 + 3.0) = 9.0 \text{ kN/m}^2$$

c – Get the Load Factors α , β



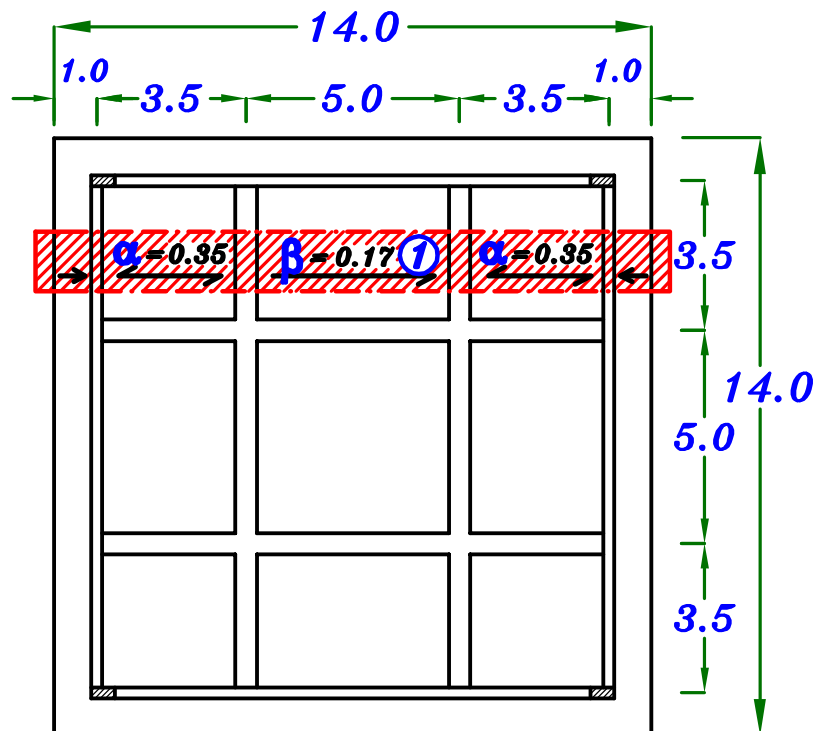
$$\alpha = 0.5 r - 0.15$$

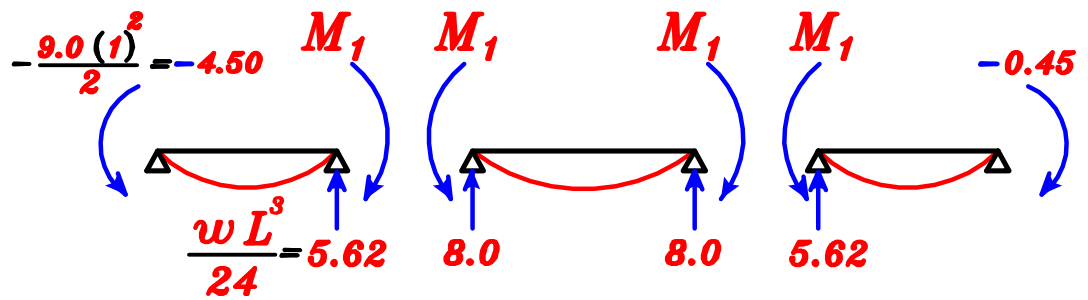
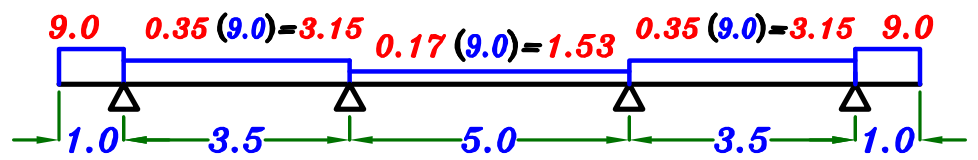
$$\beta = \frac{0.35}{r^2}$$

d – Take a strips in the slab (at the Load direction)

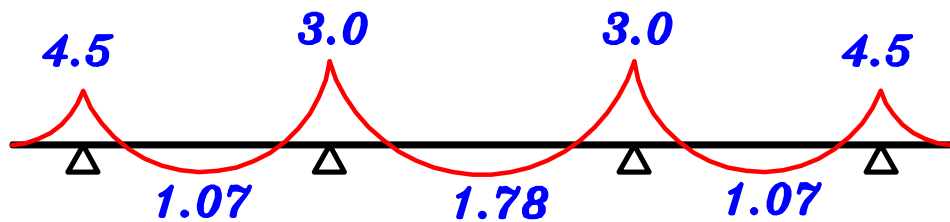
And then Get (B.M.) on the Slab & Design the slab.

Strip ①

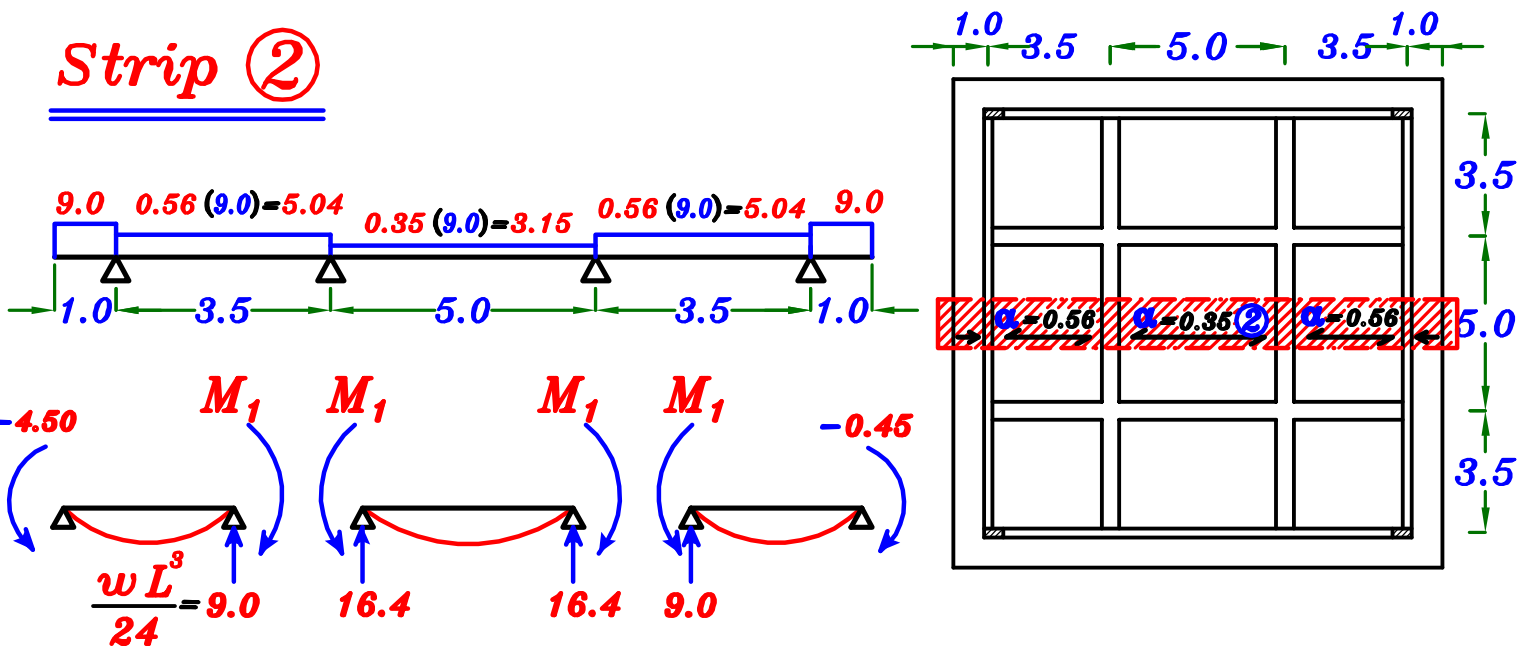




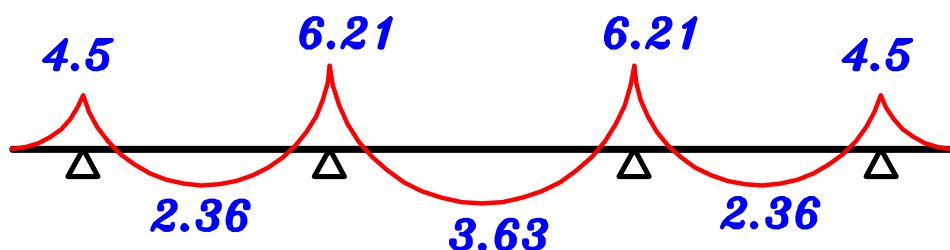
$$-4.5(3.5) + 2M_1(3.5+5.0) + M_1(5.0) = -6(5.62+8.0) \quad \boxed{M_1 = -3.0 \text{ kN.m}}$$



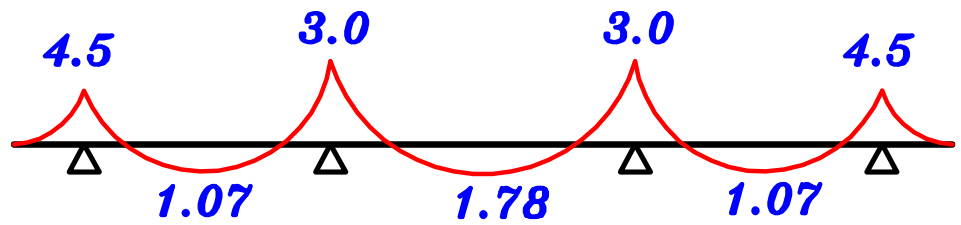
Strip ②



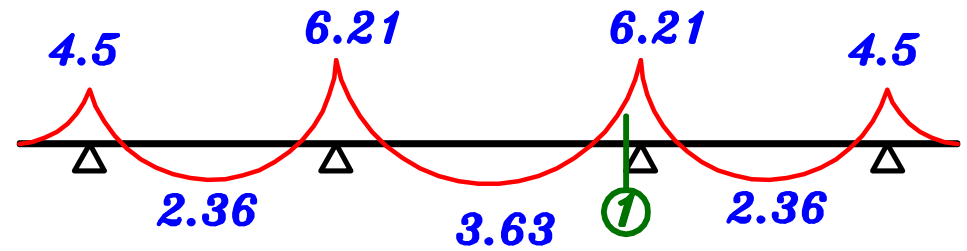
$$-4.5(3.5) + 2M_1(3.5+5.0) + M_1(5.0) = -6(9.0+16.4) \quad \boxed{M_1 = -6.21 \text{ kN.m}}$$



Strip ①



Strip ②



Sec. ①

$$M_{U.L.} = 6.21 \text{ kN.m/m}$$

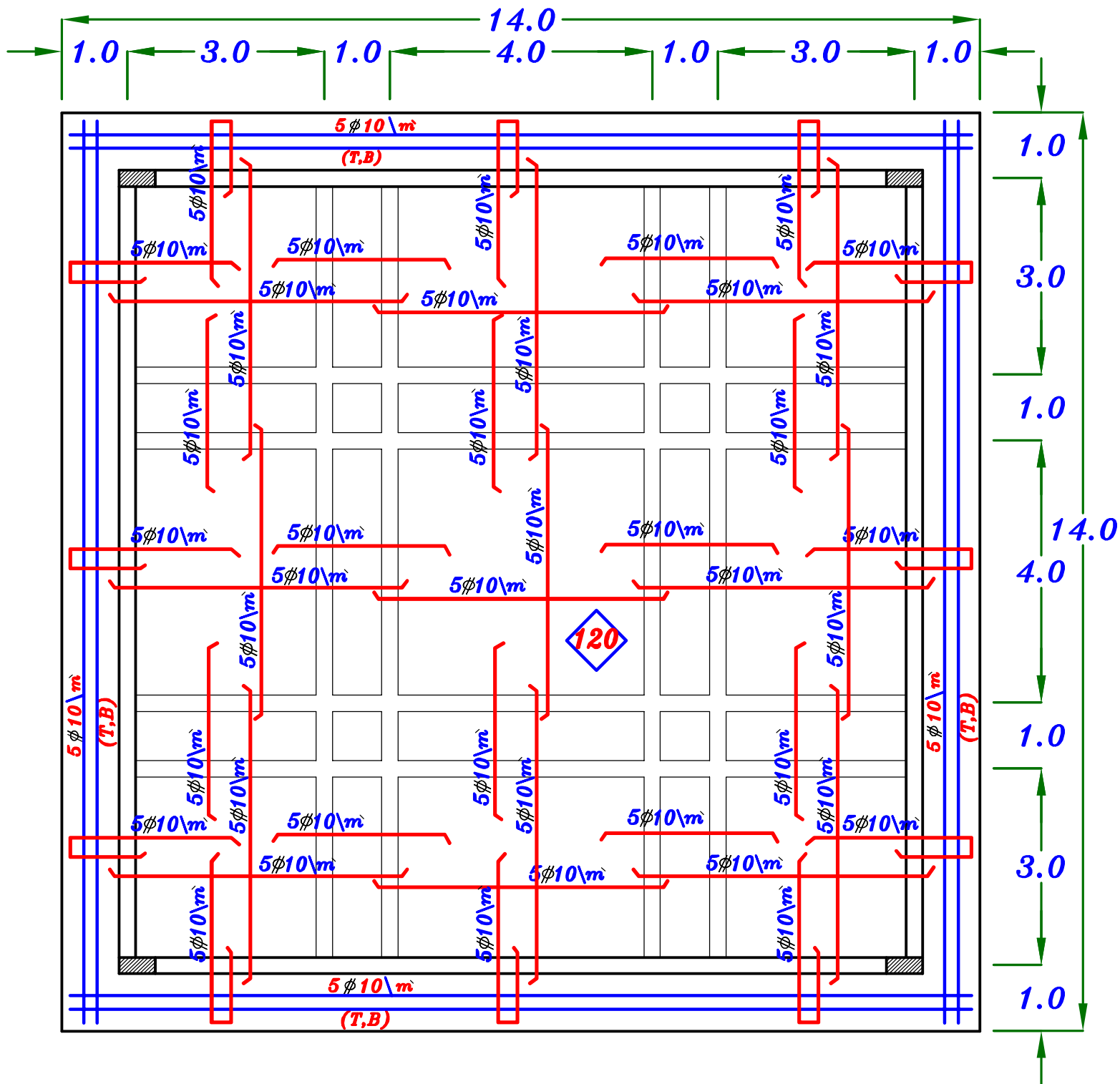
$t_s = 120 \text{ mm}$, $d = 120 - 20 = 100 \text{ mm}$, $B = 1000 \text{ mm}$ عرض الشريحة

$$100 = C_1 \sqrt{\frac{6.21 * 10^6}{25 * 1000}} \longrightarrow C_1 = 6.34 \longrightarrow J = 0.826$$

$$A_s = \frac{6.21 * 10^6}{0.826 * 360 * 100} = 208.8 \text{ mm}^2/\text{m} \quad \textcircled{5 \phi 10 \setminus \text{m}}$$

∴ سيؤخذ تسليح باقى القطاعات $5 \phi 10 \setminus \text{m}$

Details of RFT. For the Slab.



F- Design the Panelled Beam. B_1

a – Get the Dimensions of the beam. (b, t)

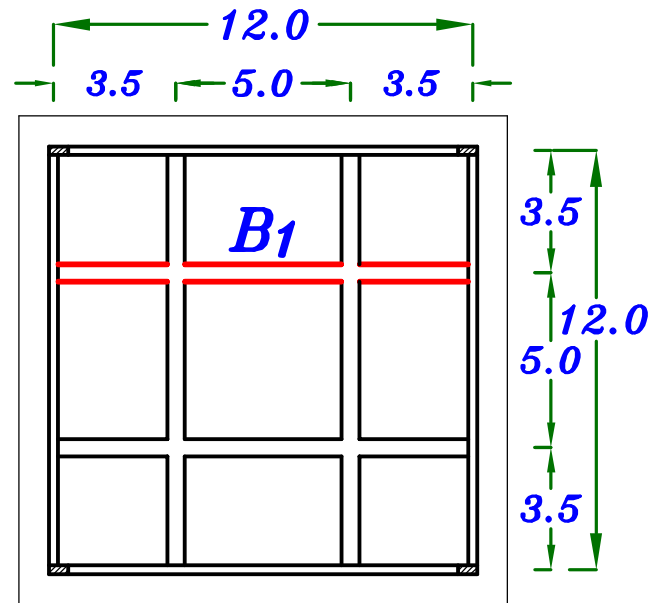
Take $b = 0.40$ m

as Ginev in data

$$t = \frac{L_s}{16} = \frac{12.0}{16} = 0.75 \text{ m}$$

$b = 0.25 \text{ m}$

$t = 0.75 \text{ m}$



b – Get the Loads on the Slab. (w_{av})

$$w_{av.} = w_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s}$$

$$w_{av.} = w_s + \frac{1.4 * b * (t - t_s) [\text{مجموع أطوال الكمرات الداخلية}] * \delta_c}{L * L_s}$$

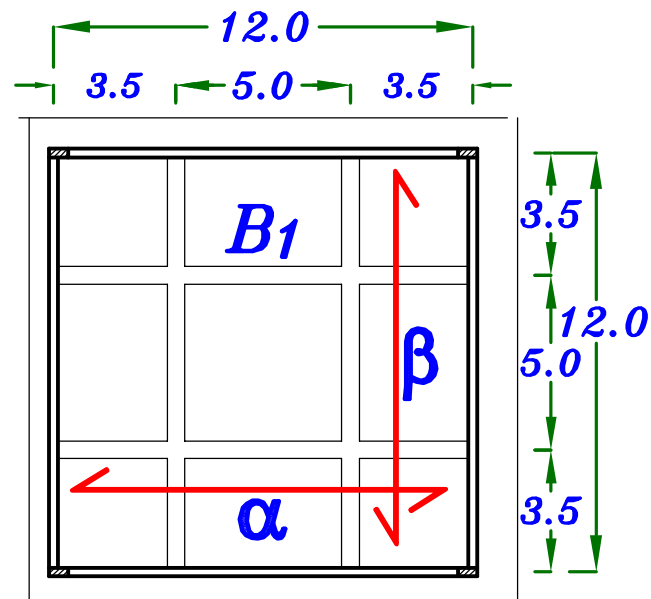
$$w_{av.} = 9.0 + \frac{1.4 * 0.40 * (0.75 - 0.12) [2 * 12 + 2 * 12] * 25}{12 * 12} = 11.94 \text{ kN/m}^2$$

c – Calculate α, β By using Grashoff.

$$r = \frac{m}{m'} \frac{L}{L_s} = \frac{(1.0)}{(1.0)} \frac{9.0}{9.0} = 1.0$$

$$\alpha = \frac{r^4}{1 + r^4} = \frac{(1.0)^4}{1 + (1.0)^4} = 0.50$$

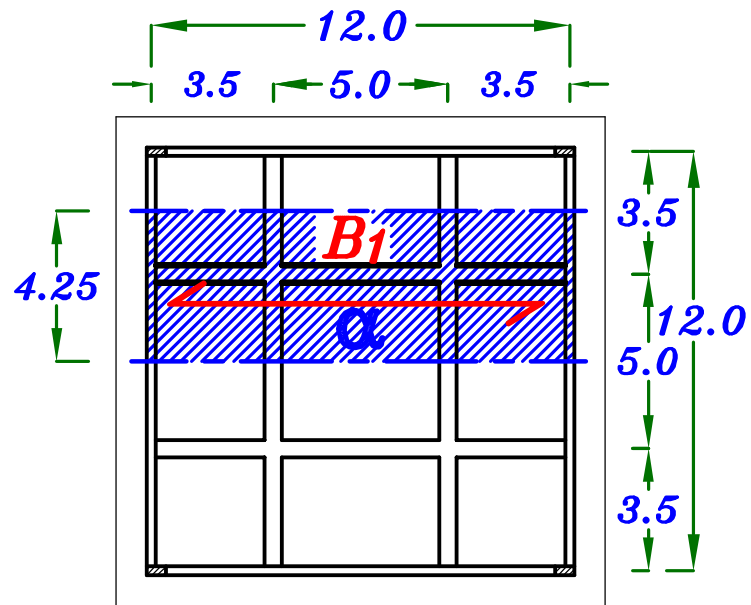
$$\beta = \frac{1}{1 + r^4} = \frac{1}{1 + (1.0)^4} = 0.5$$



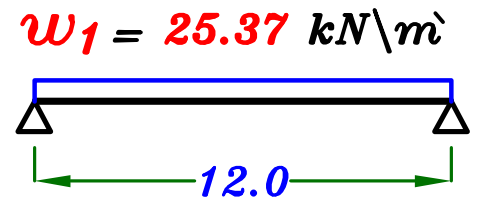
B_1 α Direction.

$$\alpha = \frac{3.5}{2} + \frac{5.0}{2} = 4.25 \text{ m}$$

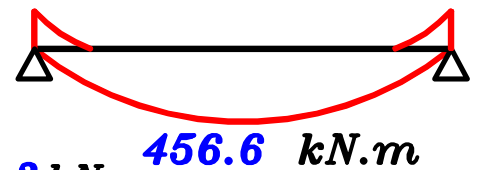
$$\begin{aligned} w_1 &= w_{av.} * \alpha * \alpha \\ &= 11.94 * 4.25 * 0.50 \\ &= 25.37 \text{ kN/m} \end{aligned}$$



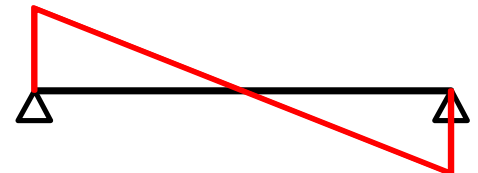
$$M = 25.37 * \frac{12.0^2}{8} = 456.6 \text{ kN.m}$$



B.M.D.



S.F.D.



e - Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

$$X = 3.5 \text{ m} , \quad \frac{L}{2} = 6.0 \text{ m}$$

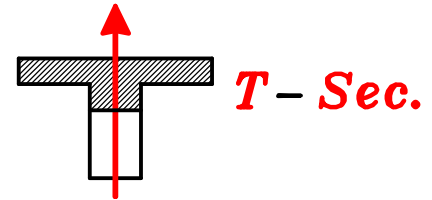
$$\theta_{B_1} = \frac{3.5}{6.0} * 90^\circ = 52.5^\circ$$

$$M_1 = 456.6 * \frac{\sin 52.5^\circ}{\sin 90^\circ} = 362.2 \text{ kN.m}$$

F – Design the Panelled Beam. B_1

فى الكمرات ال **symmetric** نصمم كمره واحده فقط و نضع تسليح الكمرتين مثل بعض و يفضل ان نأخذ **cover** كمره β لانه الاكبر لانه فى التصميم كلما فرضنا ان ال **cover** اكبر تقل قيمه **d** فى التصميم فتزيد كميته الحديد .

β Direction. $\therefore \text{Cover} = 70 \text{ mm}$
 $t = 750 \text{ mm}$ $d = 750 - 70 = 680 \text{ mm}$



$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = \frac{3.5}{2} + \frac{5.0}{2} = 4.25 \text{ m} = 4250 \text{ mm} \\ 16 t_s + b = 16 * 120 + 400 = 2320 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{12000}{5} + 400 = 2800 \text{ mm} \end{array} \right\} \quad \boxed{B = 2320 \text{ mm}}$$

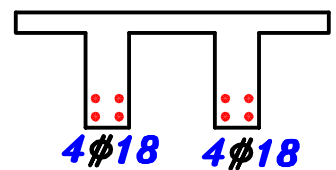
$$680 = C_1 \sqrt{\frac{362.2 * 10^6}{25 * 2320}} \rightarrow C_1 = 8.60 \rightarrow J = 0.826$$

$$A_s = \frac{362.2 * 10^6}{0.826 * 360 * 680} = 1791 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1791 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 680 = 850 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1791 \text{ mm}^2 \quad \boxed{8 \phi 18}$$



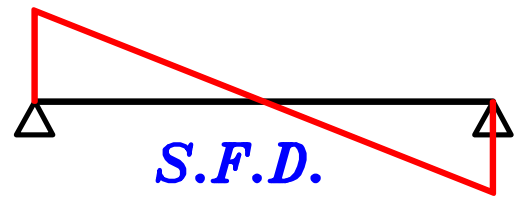
$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (179 \rightarrow 358 \text{ mm}^2) \quad \boxed{4 \phi 10}$$

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

152.2 kN

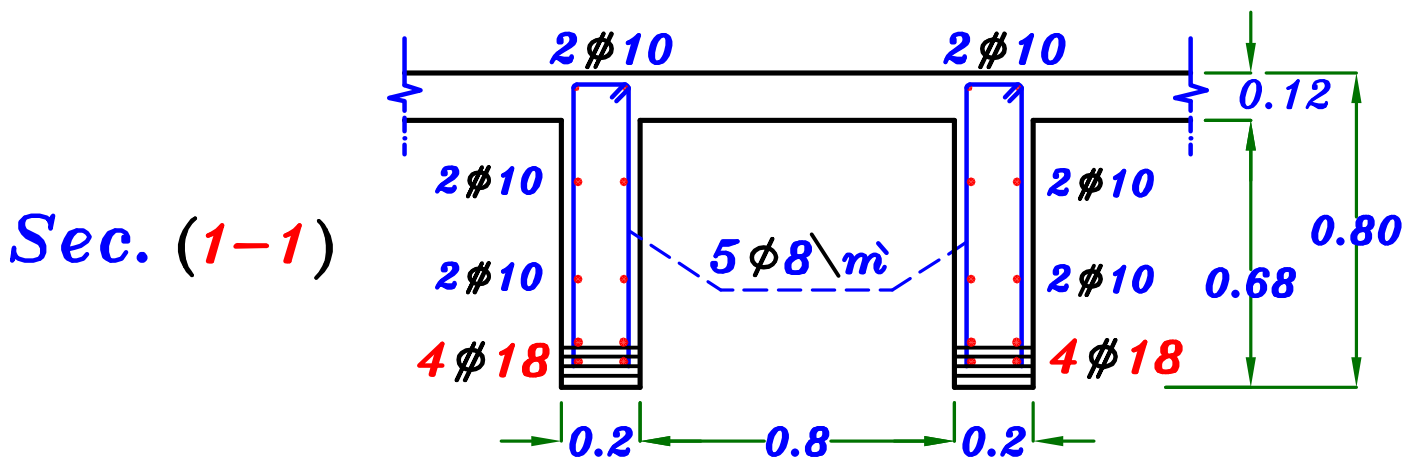
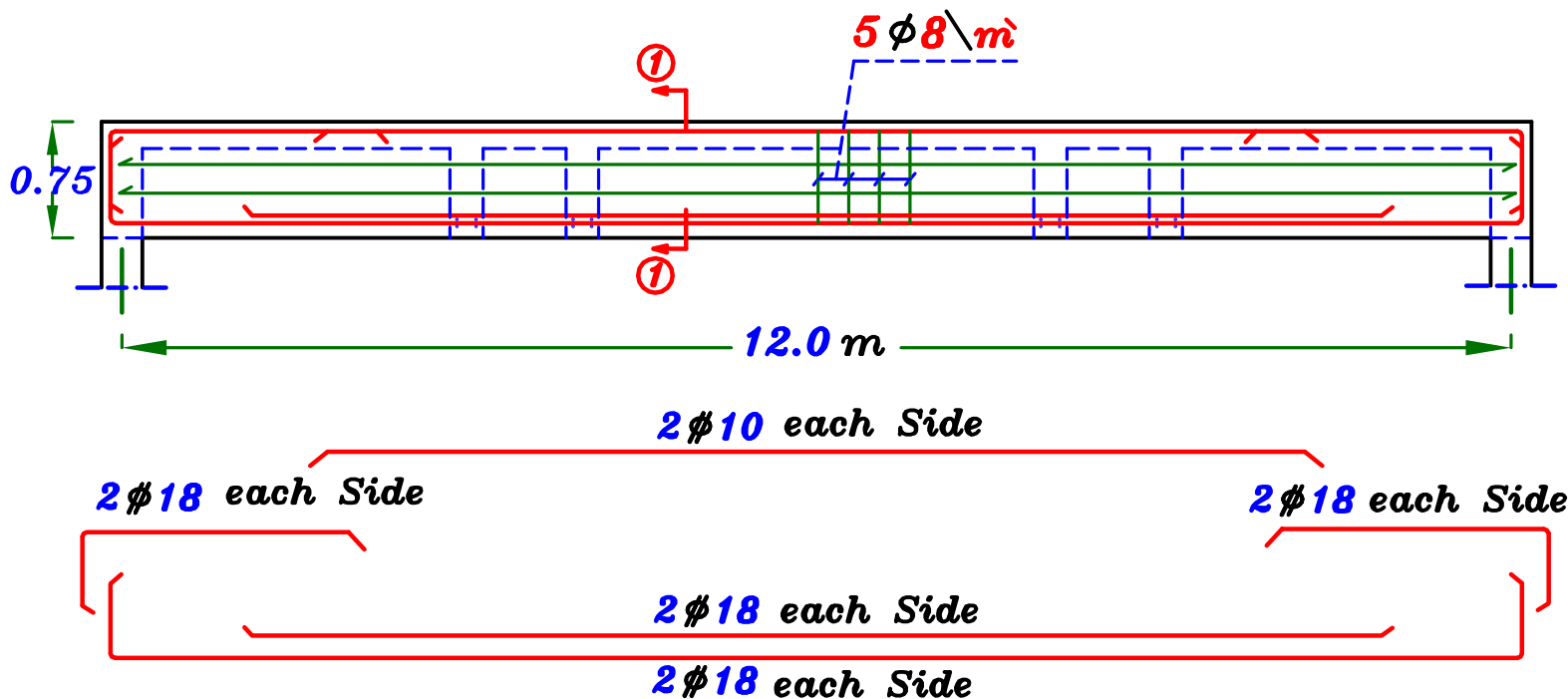


$$q_s = \frac{Q_{max}}{b d} = \frac{152.2 * 10^3}{250 * 680} = 0.89 \text{ N/mm}^2 \therefore q_s < q_{cu}$$

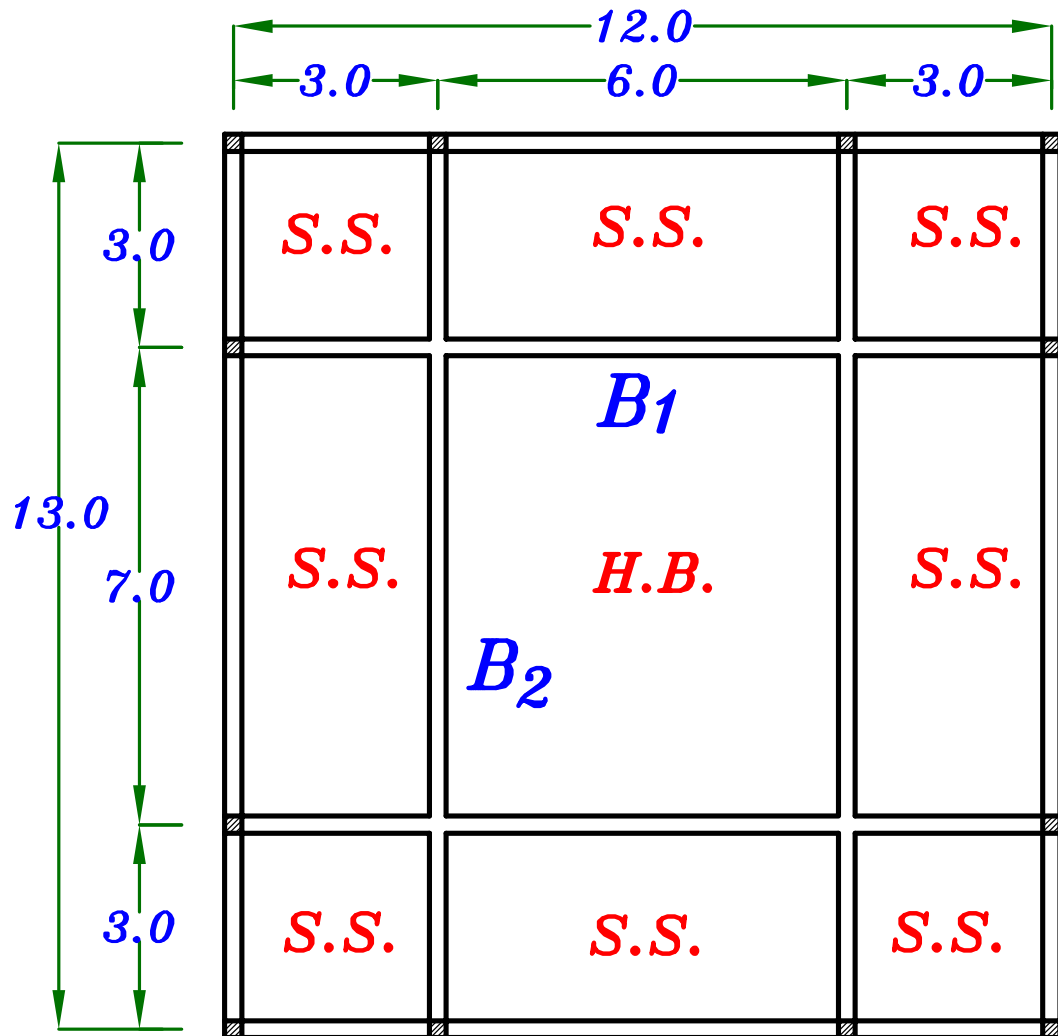
\therefore Use min. Shear RFT.

5 ϕ 8/m

Draw Details of RFT. For the Beams.



Example.



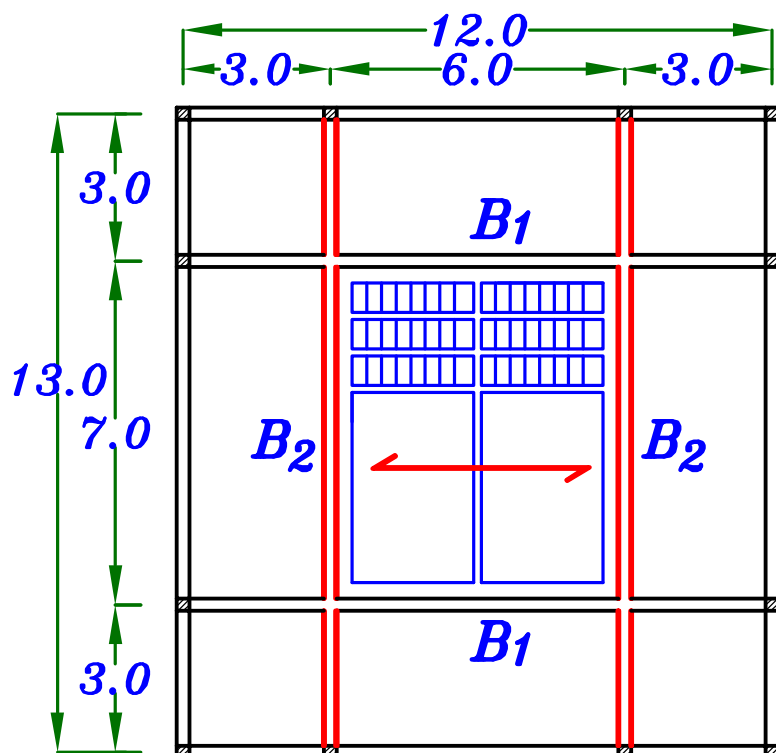
Data.

$$F_{cu} = 25 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

$$F.C. = 1.50 \text{ kN/m}^2, \quad L.L. = 2.0 \text{ kN/m}^2$$

Req.

- ① Design the slab & Draw Details of RFT.
- ② Design the panelled Beams B_1, B_2 & Draw Details of RFT. in elevation.



إذا اخذنا البلاطه $(6.0 * 7.0)$

عبارة عن *One way H.B.*

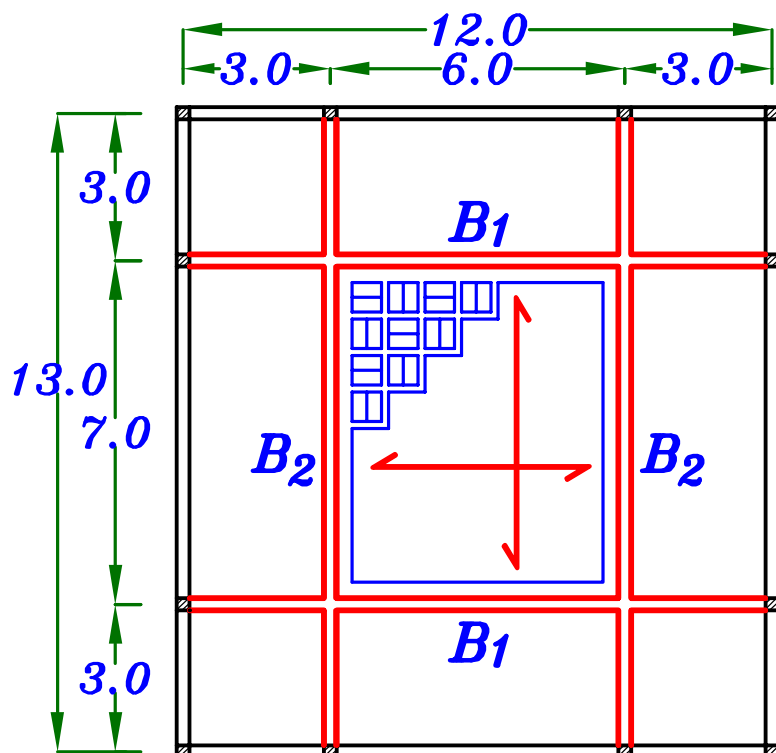
هذا معناه ان الكمرتين B_1

هما من سيحملان البلاطه كلها

والكمرتان B_2 لن يحملن شياء من البلاطه

فستصبح شبكه ال *Panelled Beams*

غير منتظمه و بذلك تفقد ميزاتها .



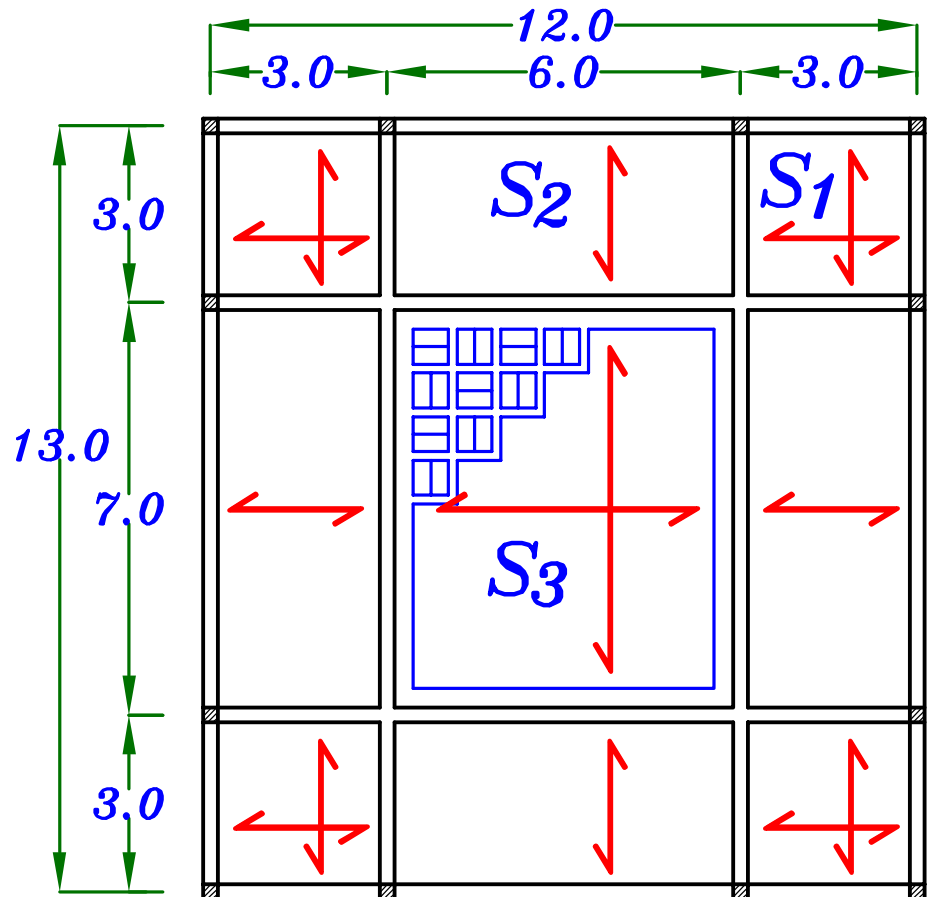
لذا سنضطر اخذ البلاطه فى المنتصف


Two way H.B.


حتى يتوزع حملها على ال ϵ كمرات

خصوصا ان $\frac{L}{L_s} \gg \frac{4}{3}$


a- Choose the Thickness of the Slabs.



S_1 two way $L_s = 3.0 \text{ m}$  $t_s = \frac{3000}{40} = 75.0 \text{ mm}$

S_2 One way $L_s = 3.0 \text{ m}$  $t_s = \frac{3000}{30} = 100 \text{ mm}$

Take (t_s) the bigger value $t_s = 100 \text{ mm}$

S_3 Two way H.B. $L_s = 6.0 \text{ m}$ 

$t = \frac{6000}{45} = 133 \text{ mm}$ $t = 200 \text{ mm}$

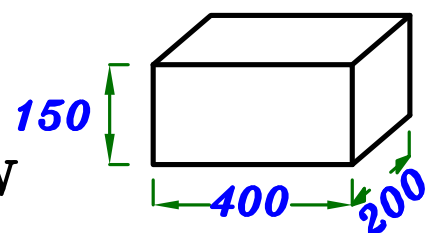
Take $t = 200 \text{ mm}$

$t_s = 50 \text{ mm}$

$h = 150 \text{ mm}$

The Block ($200 * 400 * 150$)

$h = 150 \text{ mm} \rightarrow \text{Weight of Block} = 100 \text{ N}$



b – Get the Loads on the Slab

For Solid Slabs.

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 L.L.$$

$$w_s = 1.4 (0.10 * 25 + 1.5) + 1.6 (2.0) = 8.80 \text{ kN/m}^2$$

For Two way Hollow Blocks.

$$w_{ribT} = [1.4 (t_s \delta_c + F.C.) + 1.6 (L.L.)] (S * S) + 1.4 * b * h * (2S - b) * \delta_c + 1.4 * (\text{Block ال وزن}) \left(\frac{e}{a} \right)$$

$$\therefore w_{ribT} = [1.4 (0.05 * 25 + 1.5) + 1.6 (2.0)] (0.5 * 0.5) + 1.4 (0.1 * 0.15 * (2 * 0.5 - 0.1) * 25) + 1.4 \left(\frac{100}{1000} \right) \left(\frac{0.4}{0.2} \right) = 2.515 \text{ (kN / (S * S))}$$

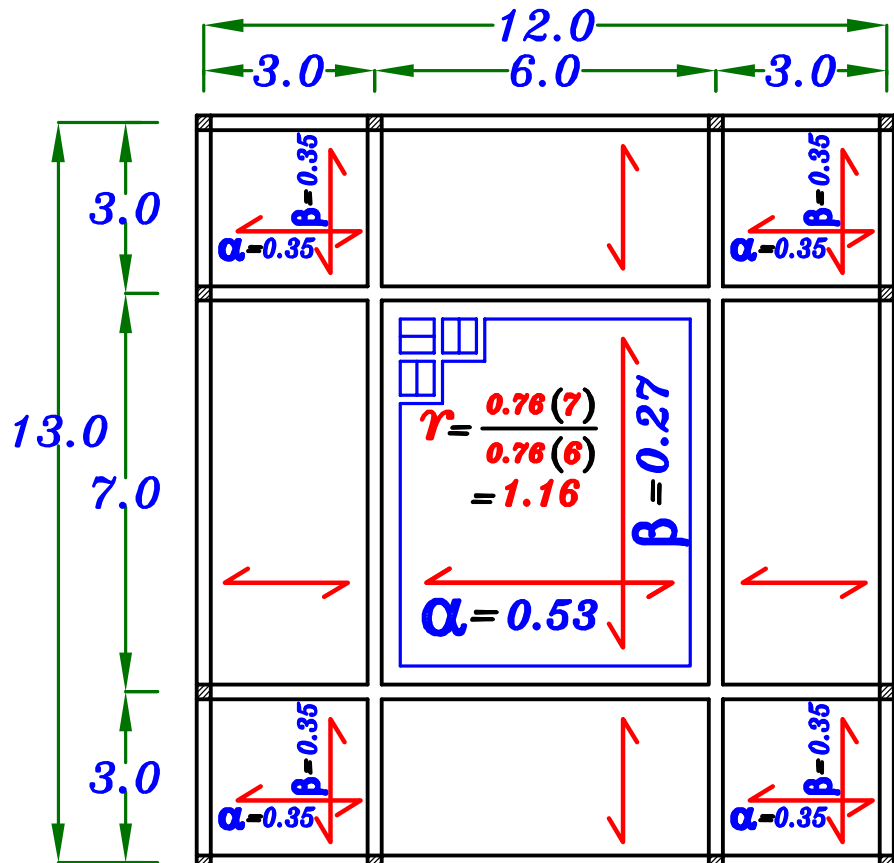
$$w_{rib} = \frac{w_{ribT}}{S} = \frac{2.515}{0.5} = 5.03 \text{ kN / (S * m)}$$

For **H.B.**

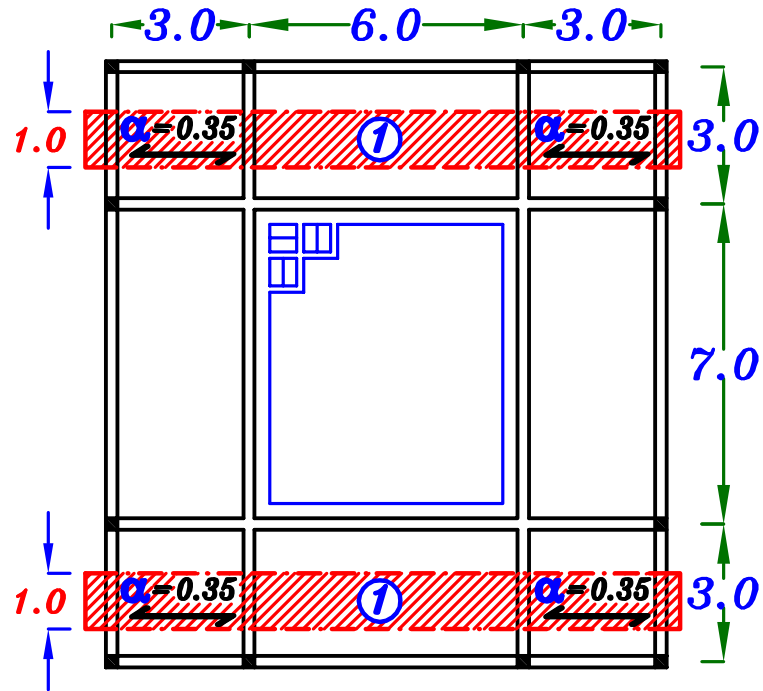
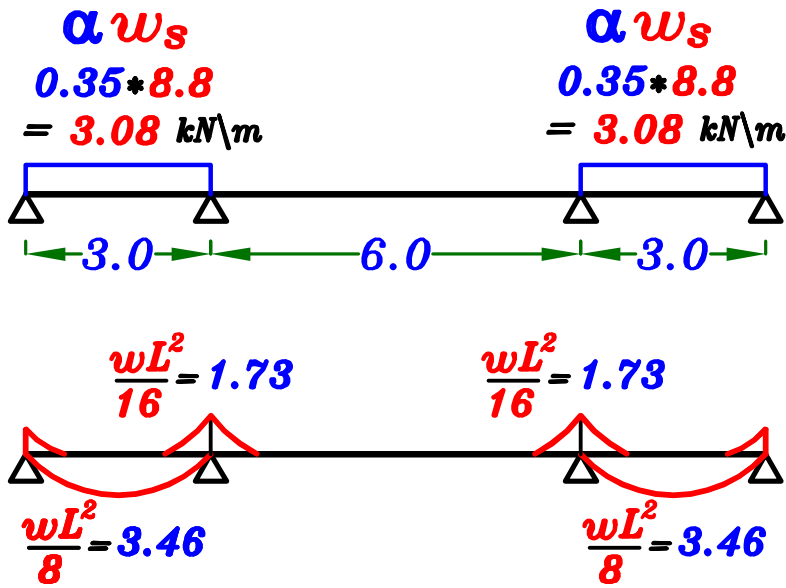
Use **Marcus**

For **S.S.**

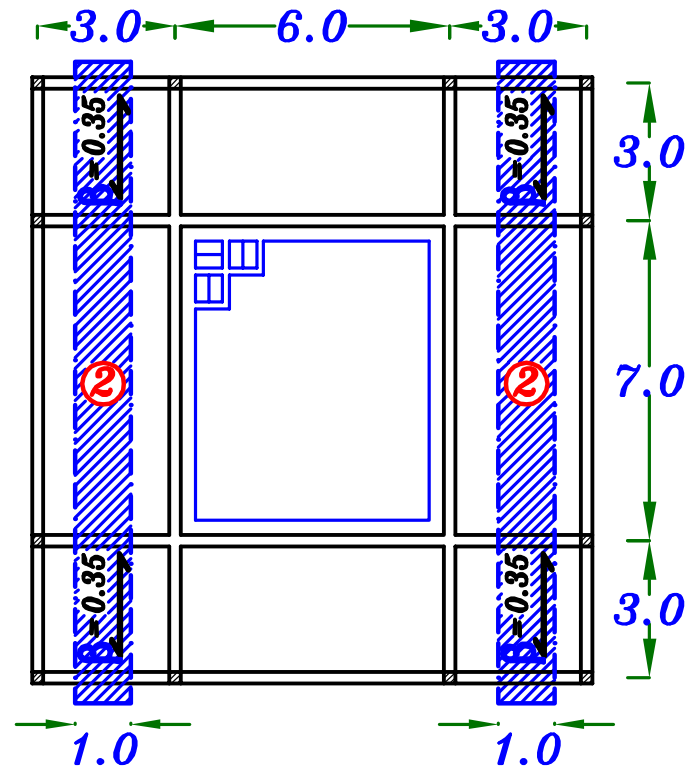
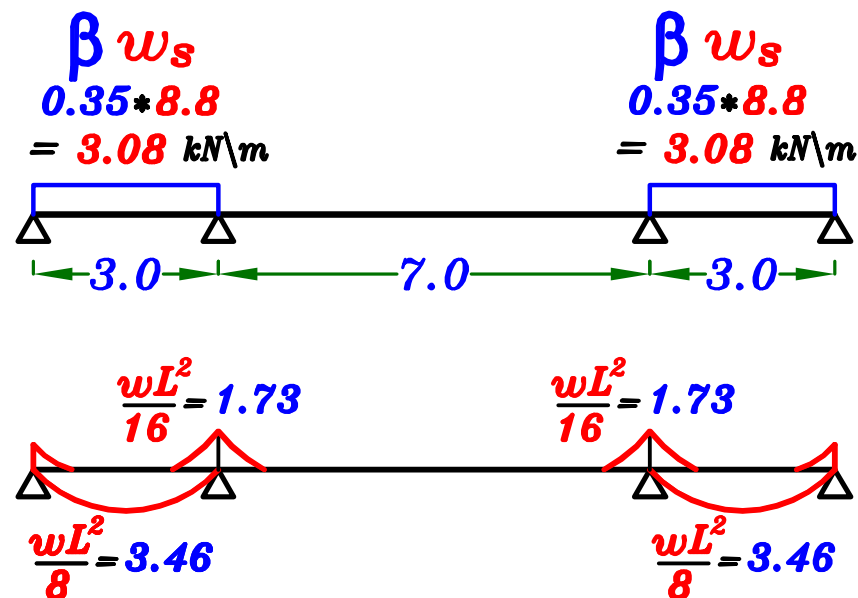
Use **C.P.**



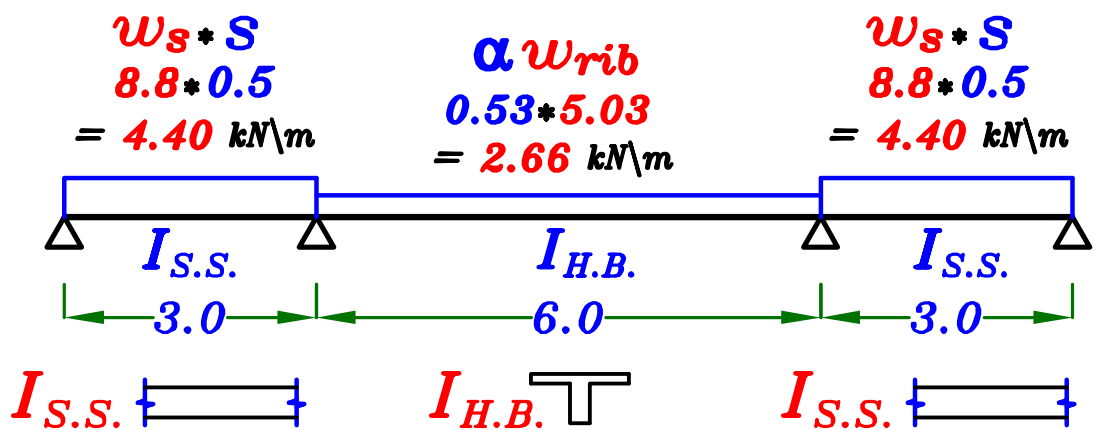
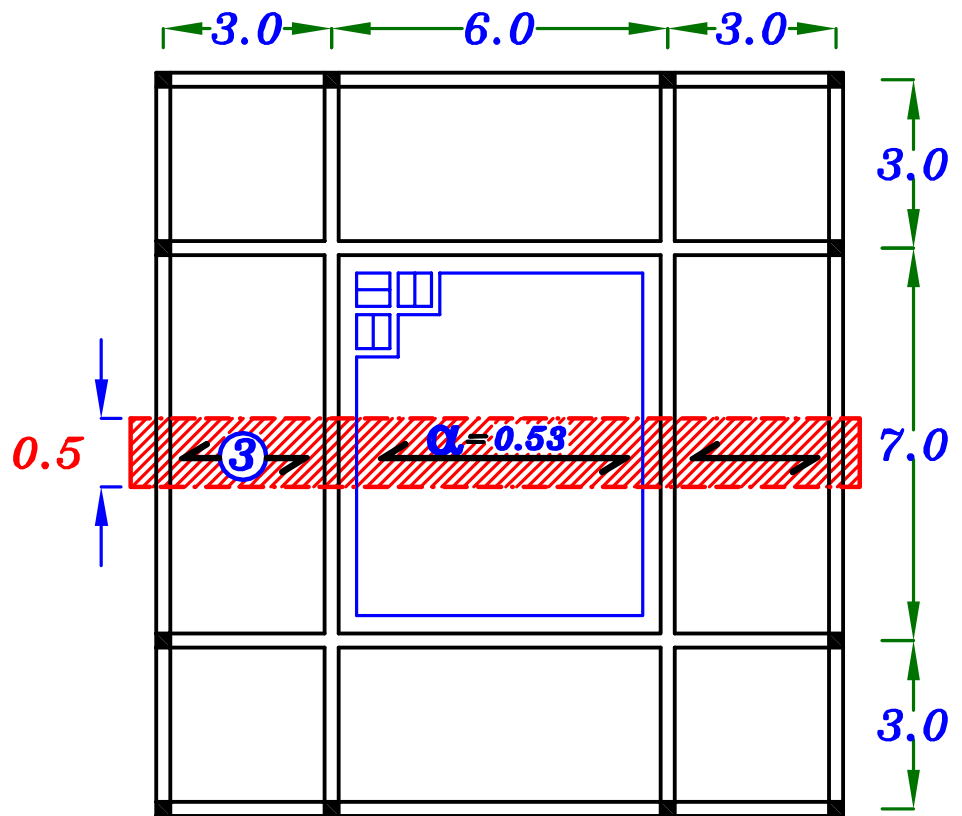
Strip ①



Strip ②



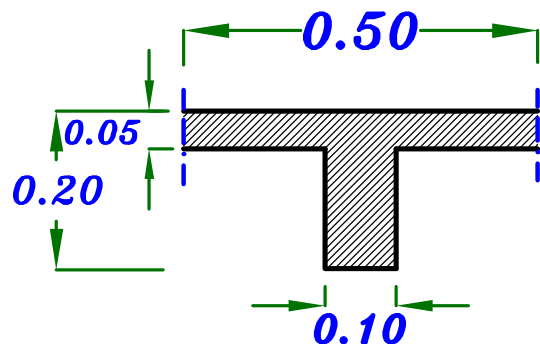
Strip ③



$$I_{H.B.} = \text{T-section} \quad I_1 = (\mu \cdot 10^{-4}) B t^3$$

$$B = 0.5 \text{ m}, \quad t = 0.20 \text{ m}$$

$$\frac{t_s}{t} = \frac{0.05}{0.20} = 0.25, \quad \frac{b_s}{B} = \frac{0.1}{0.5} = 0.2$$



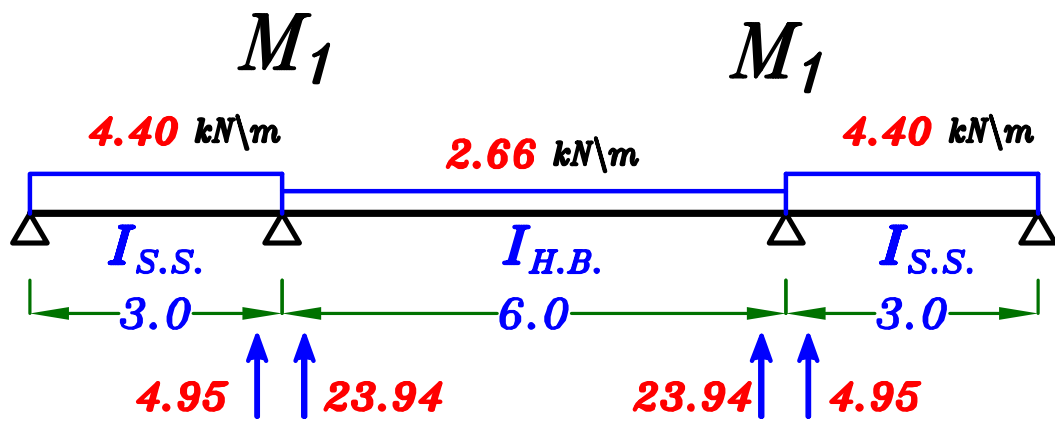
From Tables page 91 $\mu = 318$

$$I_{H.B.} = (318 \cdot 10^{-4} \cdot 0.5 \cdot 0.20^3) = 1.27 \cdot 10^{-4} \text{ m}^4$$

$$I_{S.S.} = \frac{S (t_s)^3}{12} = \frac{0.5 (0.10)^3}{12} = 4.16 \cdot 10^{-5} \text{ m}^4$$

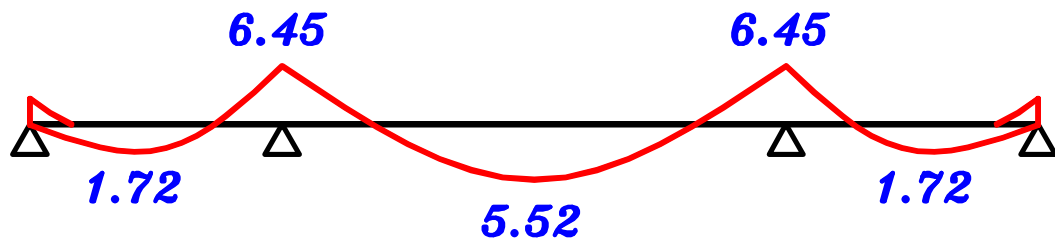
$$\therefore \frac{I_{H.B.}}{I_{S.S.}} = \frac{1.27 \cdot 10^{-4}}{4.16 \cdot 10^{-5}} = 3.05$$

$$\therefore \boxed{I_{H.B.} = 3.05 I_{S.S.}}$$

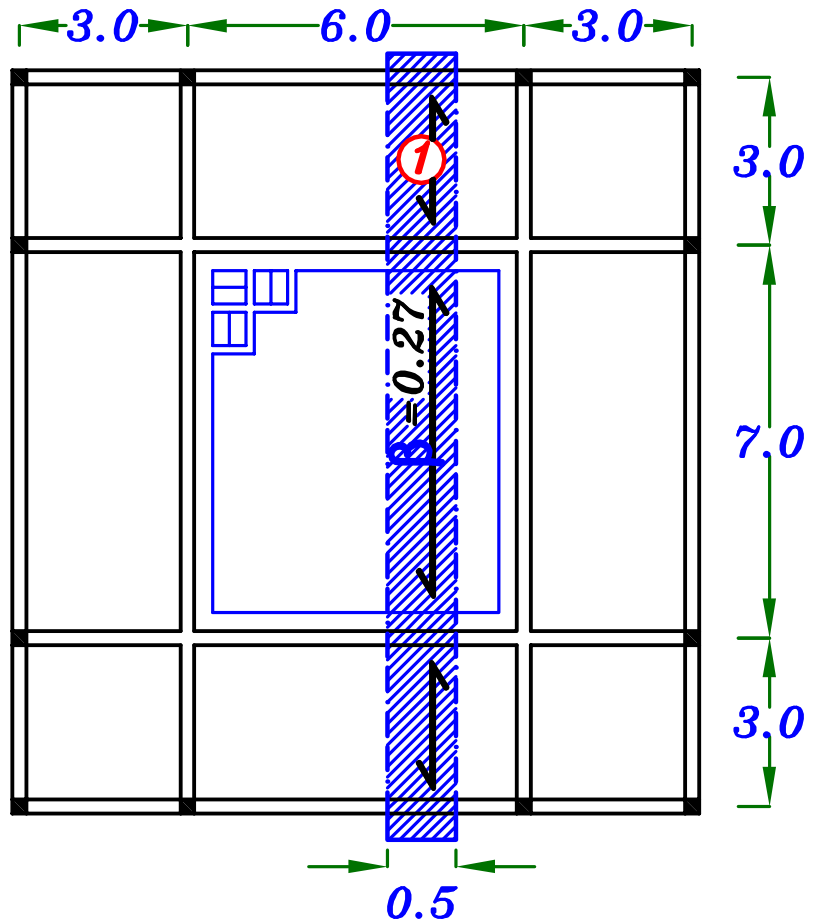


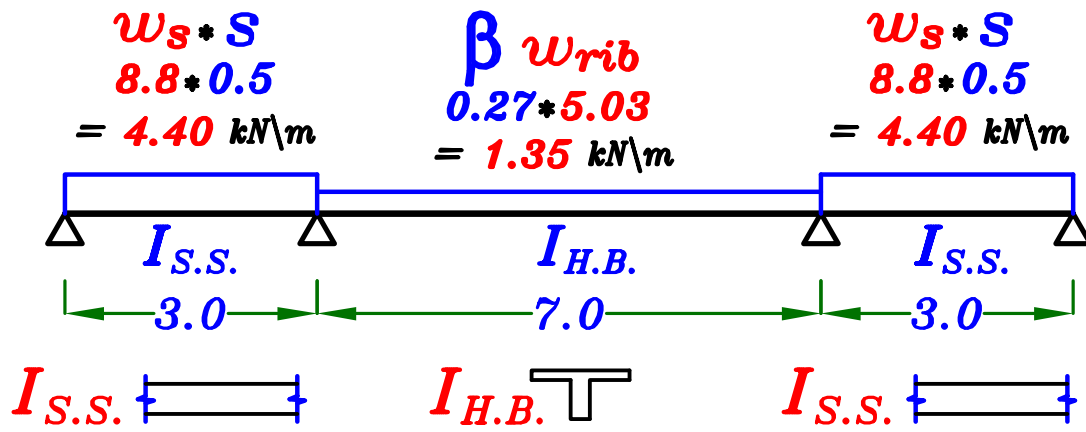
$$0.0 + 2M_1 \left(\frac{3.0}{I_{S.S.}} + \frac{6.0}{3.05I_{S.S.}} \right) + M_1 \left(\frac{6.0}{3.05I_{S.S.}} \right) = -6 \left(4.95 + \frac{23.94}{3.05I_{S.S.}} \right)$$

$$M_1 = -6.45 \text{ kN.m/0.5m}$$

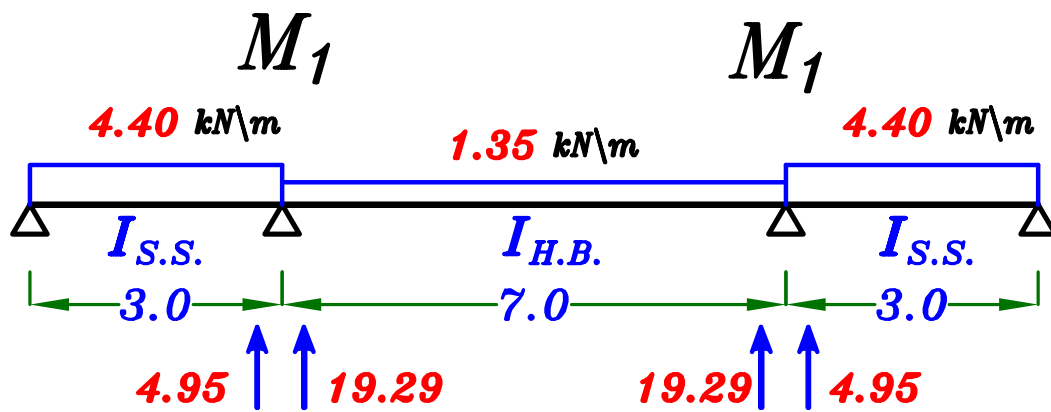


Strip ④



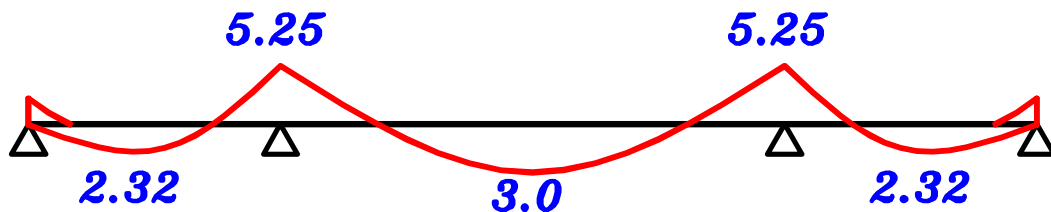


$$I_{H.B.} = 3.05 I_{S.S.}$$

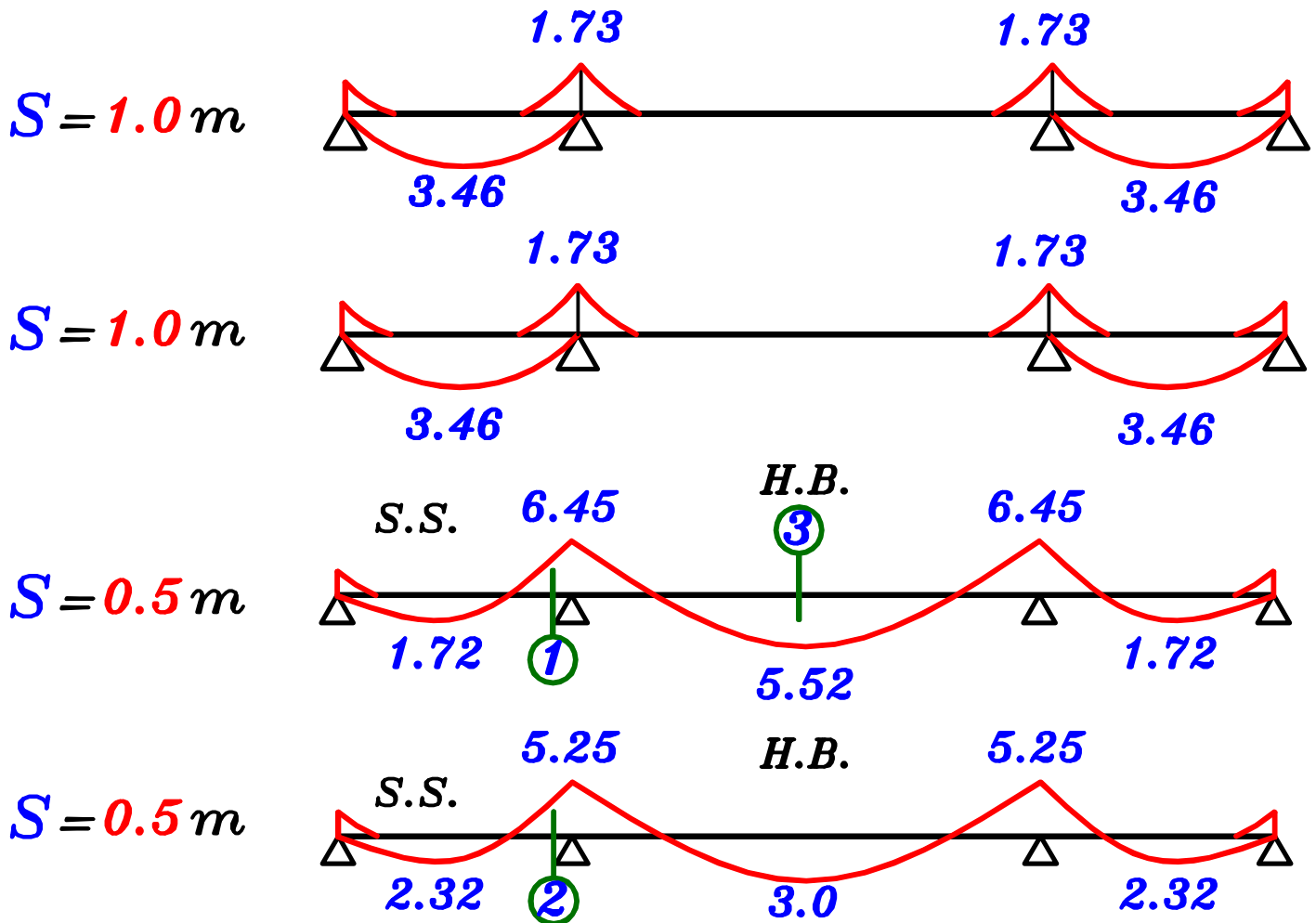


$$0.0 + 2M_1 \left(\frac{3.0}{I_{S.S.}} + \frac{7.0}{3.05 I_{S.S.}} \right) + M_1 \left(\frac{7.0}{3.05 I_{S.S.}} \right) = -6 \left(4.95 + \frac{19.29}{3.05 I_{S.S.}} \right)$$

$$M_1 = -5.25 \text{ kN.m/0.5m}$$



٥- نعمل تصميم للشرايح مع مراعاة عرض الشريحة .



Sec. ① S.S. $M_{U.L.} = 6.45\text{ kN.m/rib}$

$t = 100\text{ mm}$, $d = 100 - 20 = 80\text{ mm}$, $S = 500\text{ mm}$ عرض الشريحة

$$80 = C_1 \sqrt{\frac{6.45 * 10^6}{25 * 500}} \longrightarrow C_1 = 3.52 \longrightarrow J = 0.780$$

$$A_s = \frac{6.45 * 10^6}{0.780 * 360 * 80} = 287.1\text{ mm}^2 / 0.5\text{ m}$$

$$A_s = \frac{287.1}{0.50} = 574.2\text{ mm}^2 / \text{m}$$

8 ϕ 10 \text{m}

عدد زوجي

Sec. ② S.S. $M_{U.L.} = 5.25 \text{ kN.m/rib}$

$t = 100 \text{ mm}$, $d = 100 - 20 = 80 \text{ mm}$, $S = 500 \text{ mm}$ عرض الشريحة

$$80 = C_1 \sqrt{\frac{5.25 * 10^6}{25 * 500}} \longrightarrow C_1 = 3.90 \longrightarrow J = 0.80$$

$$A_s = \frac{5.25 * 10^6}{0.80 * 360 * 80} = 227.8 \text{ mm}^2 / 0.5 \text{ m}$$

$$A_s = \frac{227.8}{0.50} = 455.7 \text{ mm}^2 / \text{m} \quad \text{عدد زوجي} \quad \boxed{6 \phi 10 \backslash \text{m}}$$

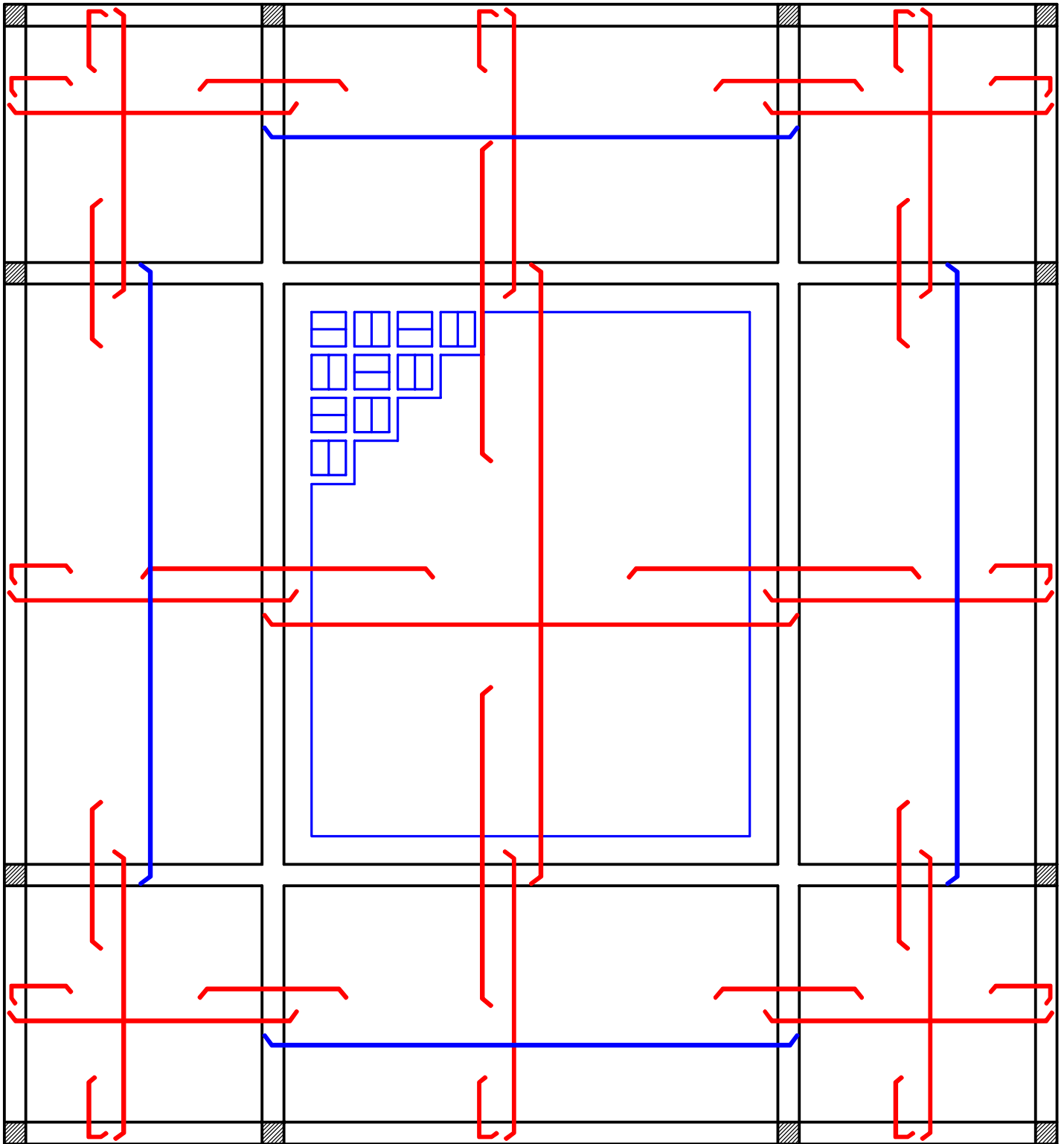
Sec. ③ H.B. $M_{U.L.} = 5.52 \text{ kN.m/rib}$

$t = 200 \text{ mm}$, $d = 200 - 30 = 170 \text{ mm}$, $S = 500 \text{ mm}$ عرض الشريحة

$$170 = C_1 \sqrt{\frac{5.52 * 10^6}{25 * 500}} \longrightarrow C_1 = 8.09 \longrightarrow J = 0.826$$

$$A_s = \frac{5.52 * 10^6}{0.826 * 360 * 170} = 109.1 \text{ mm}^2 / \text{rib} \quad \boxed{2 \phi 10 \backslash \text{rib}}$$

RFT. of the slabs.



Design of Panelled Beams.

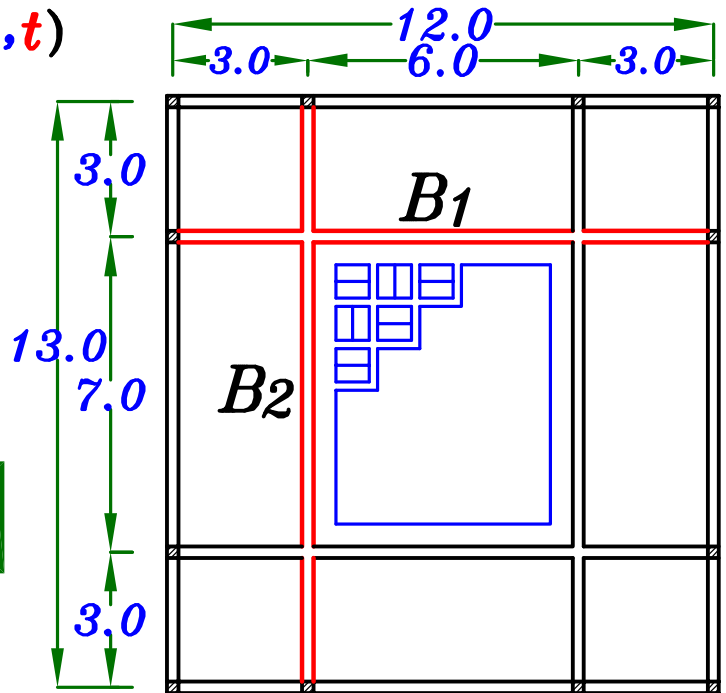
a – Get the Dimensions of the beam. (**b, t**)

Take **b** = 0.25 m

$$t = \frac{L_s}{16} = \frac{12.0}{16} = 0.75 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$t = 0.75 \text{ m}$$



b – Get the Loads on the Slab. (**w_{av}**)

$$w_{av.} = \frac{\text{Total Weight of Solid slabs} + \text{Total Weight of H.B. slabs} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

$$w_{av.} = \frac{w_s \cdot \text{area (s.s.)} + \left(\frac{w_{rib}}{S}\right) \cdot \text{area (H.B.)} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

$$w_{av.} = \frac{w_s \cdot (L \cdot L_s - a \cdot b) + \left(\frac{w_{rib}}{S}\right) \cdot (a \cdot b) + [1.4 \cdot b(t - t_s)(2L + 2L_s) \cdot \delta_c]}{L \cdot L_s}$$

$$w_{av.} = \frac{8.80(12 \cdot 13 - 6 \cdot 7) + \left(\frac{5.03}{0.5}\right)(6 \cdot 7) + 1.4 \cdot 0.25(0.75 - 0.1)[2 \cdot 12 + 2 \cdot 13] \cdot 25}{12 \cdot 13}$$

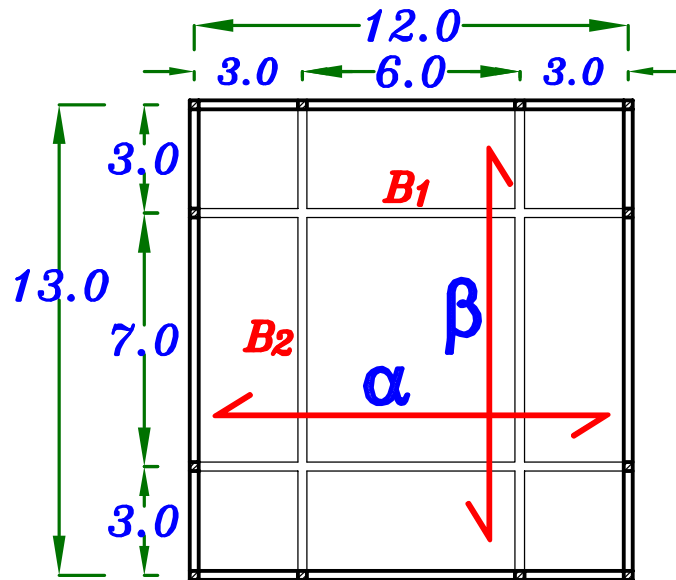
$$= 10.96 \text{ kN/m}^2$$

C – Calculate α , β By using Grashoff.

$$r = \frac{m L}{m_s L_s} = \frac{(1.0) 13.0}{(1.0) 12.0} = 1.083$$

$$\alpha = \frac{r^4}{1 + r^4} = \frac{(1.083)^4}{1 + (1.083)^4} = 0.58$$

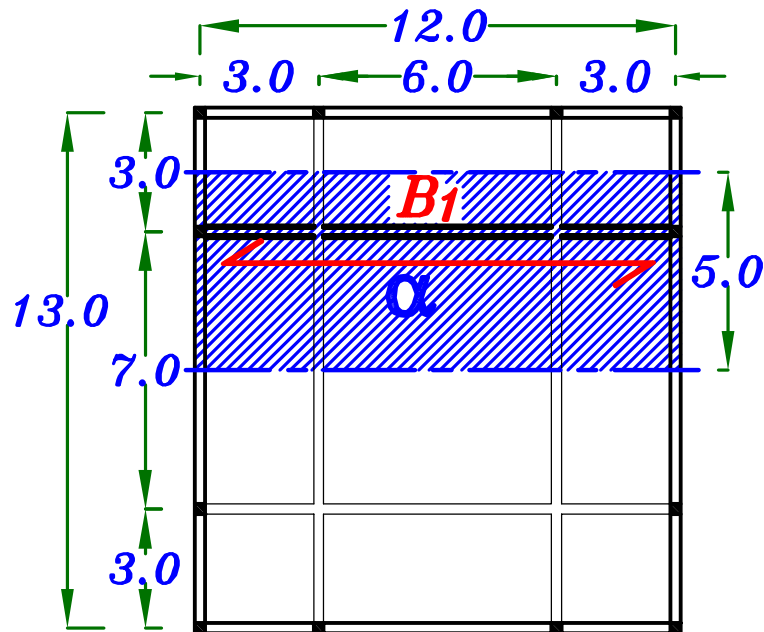
$$\beta = \frac{1}{1 + r^4} = \frac{1}{1 + (1.083)^4} = 0.42$$



B₁ α Direction.

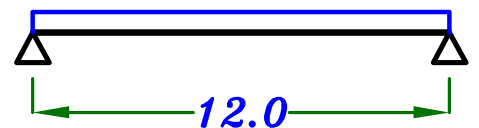
$$\alpha = 5.0 \text{ m}$$

$$\begin{aligned} w_1 &= w_{av.} * \alpha * \beta \\ &= 10.96 * 5.0 * 0.58 \\ &= 31.78 \text{ kN/m} \end{aligned}$$



$$M = 31.78 * \frac{12.0^2}{8} = 572.0 \text{ kN.m}$$

$$w_1 = 31.78 \text{ kN/m}$$

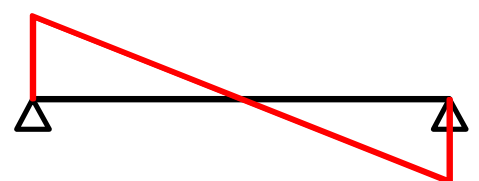


B.M.D.



$$190.7 \text{ kN}$$

S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

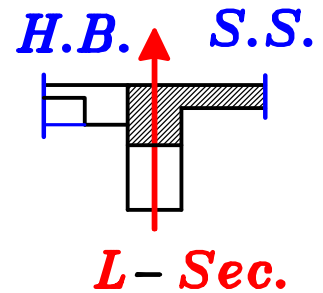
$$X = 3.0 \text{ m} , \frac{L}{2} = 6.5 \text{ m} \quad \Theta_{B_1} = \frac{3.0}{6.5} * 90^\circ = 41.52^\circ$$

$$M_1 = 572.0 * \frac{\sin 41.52^\circ}{\sin 90^\circ} = 379.17 \text{ kN.m}$$

F – Design the Panelled Beam. B_1

α Direction. $\therefore \text{Cover} = 50 \text{ mm}$

$$t = 750 \text{ mm} \quad d = 750 - 50 = 700 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 1.5 \text{ m} = 1500 \text{ mm} \\ 6 t_s + b = 6 * 100 + 250 = 850 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{12000}{10} + 250 = 1450 \text{ mm} \end{array} \right\} \quad \boxed{B = 850 \text{ mm}}$$

$$700 = C_1 \sqrt{\frac{379.17 * 10^6}{25 * 850}} \rightarrow C_1 = 5.24 \rightarrow J = 0.826$$

$$A_s = \frac{379.17 * 10^6}{0.826 * 360 * 700} = 1821.6 \text{ mm}^2$$

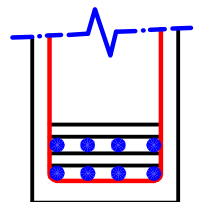
Check $A_{s_{min.}}$ $A_{s_{req.}} = 1821.6 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 700 = 546.87 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1821.6 \text{ mm}^2 \quad \boxed{8 \phi 18}$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (182 \rightarrow 364 \text{ mm}^2)$$

$$\boxed{3 \phi 10}$$

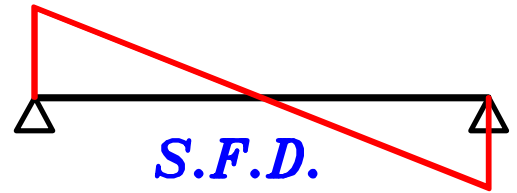


Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

190.7 kN



$$q_s = \frac{Q_{max}}{b d} = \frac{190.7 * 10^3}{250 * 700} = 1.09 \text{ N/mm}^2 \quad \therefore q_{cu} < q_s < q_{u_{max}}$$

$$q_s - \frac{q_{cu}}{2} = \frac{n A_s (F_y \delta_s)}{b S} \quad \text{Take } n = 2, \phi 8 = 50.3 \text{ mm}^2$$

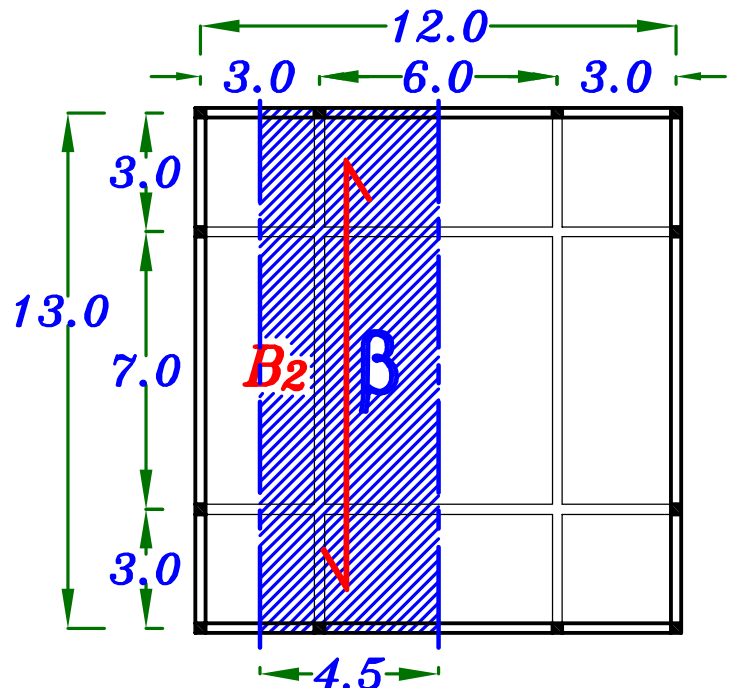
$$1.09 - \frac{0.98}{2} = \frac{2 (50.3) (240 \delta_s)}{250 * S} \quad \rightarrow S = 139.9 \text{ mm}$$

$$\text{No. of stirrups/m} = \frac{1000}{S} = \frac{1000}{139.9} = 7.14 \quad \text{Use } 8 \phi 8 \text{ m}$$

B₂ β Direction.

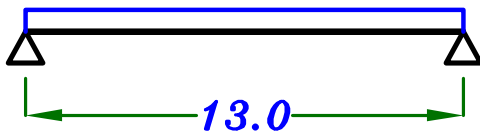
$$b = 4.5 \text{ m}$$

$$\begin{aligned} w_2 &= w_{av} * b * \beta \\ &= 10.96 * 4.5 * 0.42 \\ &= 20.71 \text{ kN/m} \end{aligned}$$

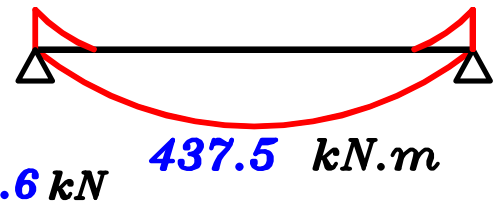


$$M = 20.71 * \frac{13.0^2}{8} = 437.5 \text{ kN.m}$$

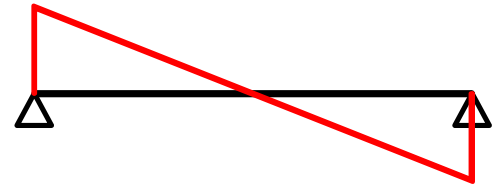
$$w_2 = 20.71 \text{ kN/m}$$



B.M.D.



S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

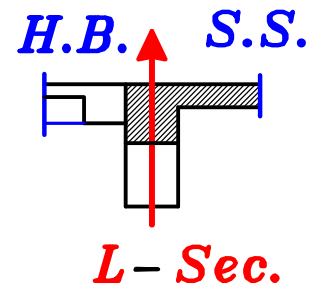
$$X = 3.0 \text{ m}, \quad \frac{L}{2} = 6.0 \text{ m} \quad \Theta_{B_1} = \frac{3.0}{6.0} * 90^\circ = 45^\circ$$

$$M_1 = 437.5 * \frac{\sin 45^\circ}{\sin 90^\circ} = 309.3 \text{ kN.m}$$

F– Design the Panelled Beam. B_1

α Direction. $\therefore \text{Cover} = 70 \text{ mm}$

$$t = 750 \text{ mm} \quad d = 750 - 70 = 680 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = 1.5 \text{ m} = 1500 \text{ mm} \\ 6 t_s + b = 6 * 100 + 250 = 850 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{13000}{10} + 250 = 1550 \text{ mm} \end{array} \right\} \quad \boxed{B = 850 \text{ mm}}$$

$$680 = C_1 \sqrt{\frac{309.3 * 10^6}{25 * 850}} \rightarrow C_1 = 5.63 \rightarrow J = 0.826$$

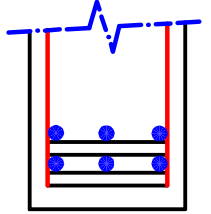
$$A_s = \frac{309.3 * 10^6}{0.826 * 360 * 680} = 1529.6 \text{ mm}^2$$

Check $A_{s_{min.}}$

$$A_{s_{req.}} = 1529.6 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 680 = 531.25 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1529.6 \text{ mm}^2 \quad \textcircled{6 \phi 18}$$



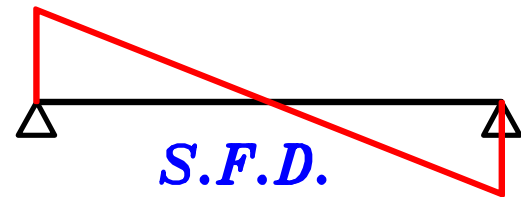
$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (148 \rightarrow 296 \text{ mm}^2) \quad \textcircled{2 \phi 10}$$

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

134.6 kN



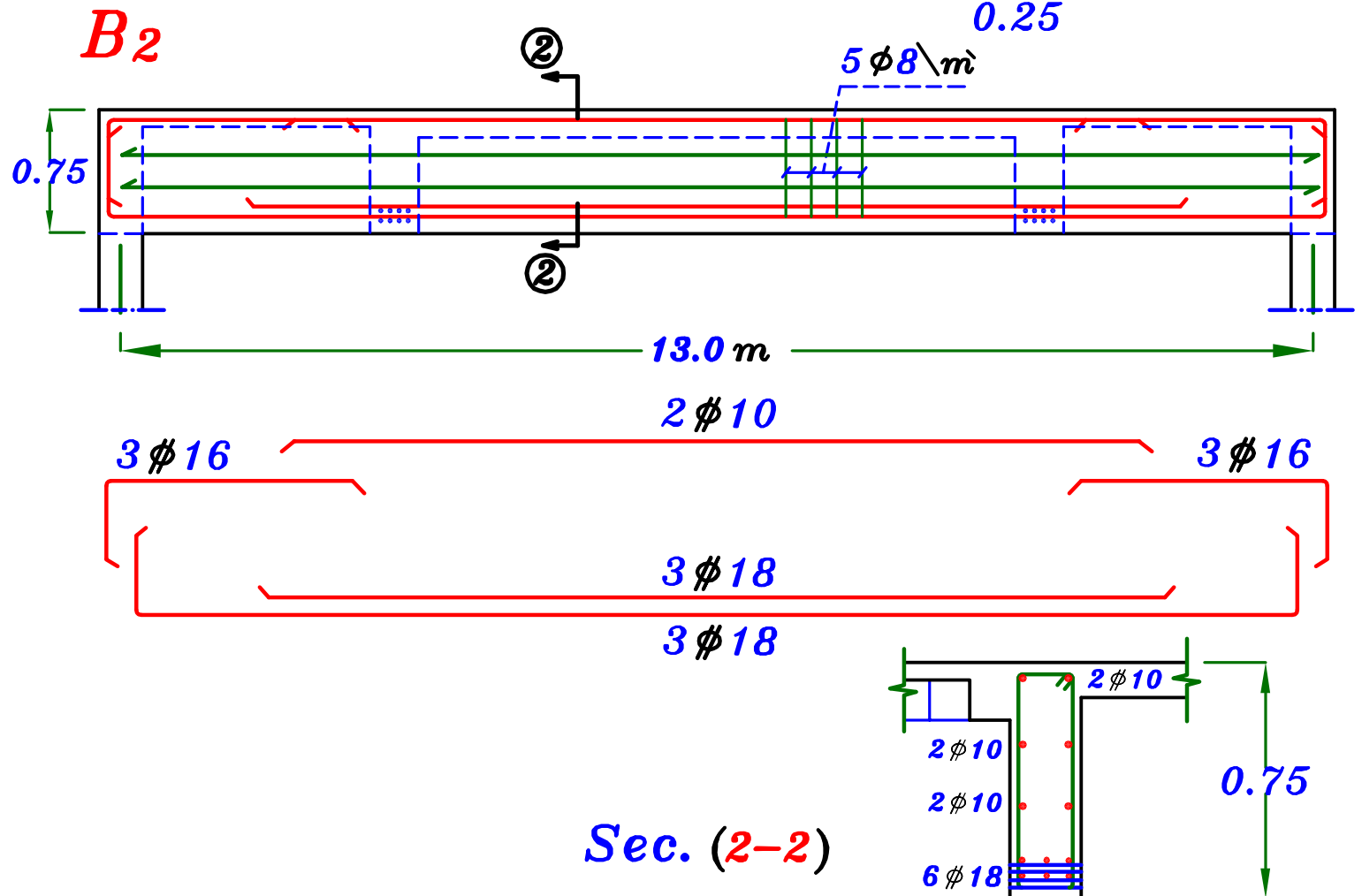
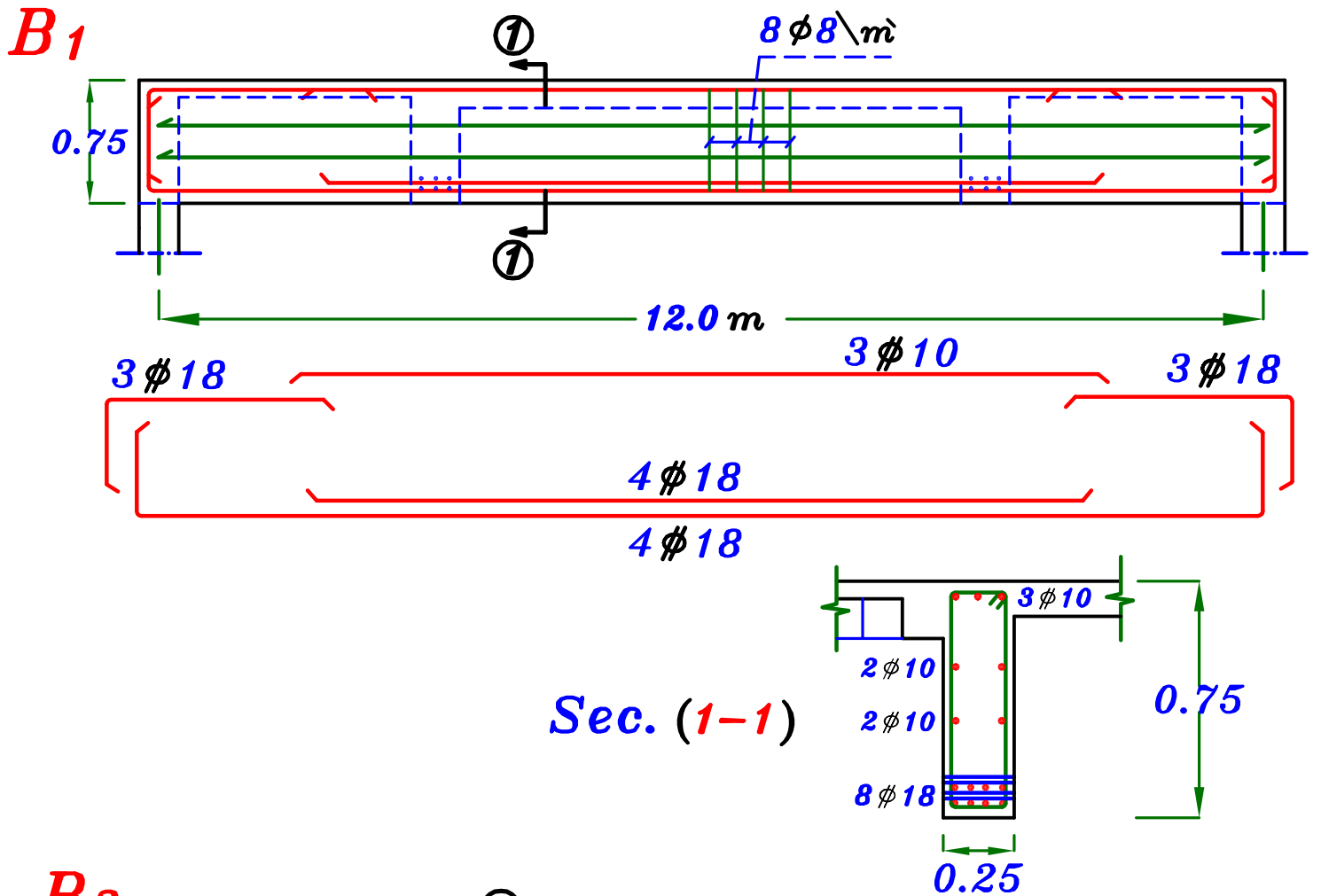
$$q_s = \frac{Q_{max}}{b d} = \frac{134.6 * 10^3}{250 * 700} = 0.77 \text{ N/mm}^2$$

$$\therefore q_s < q_{cu}$$

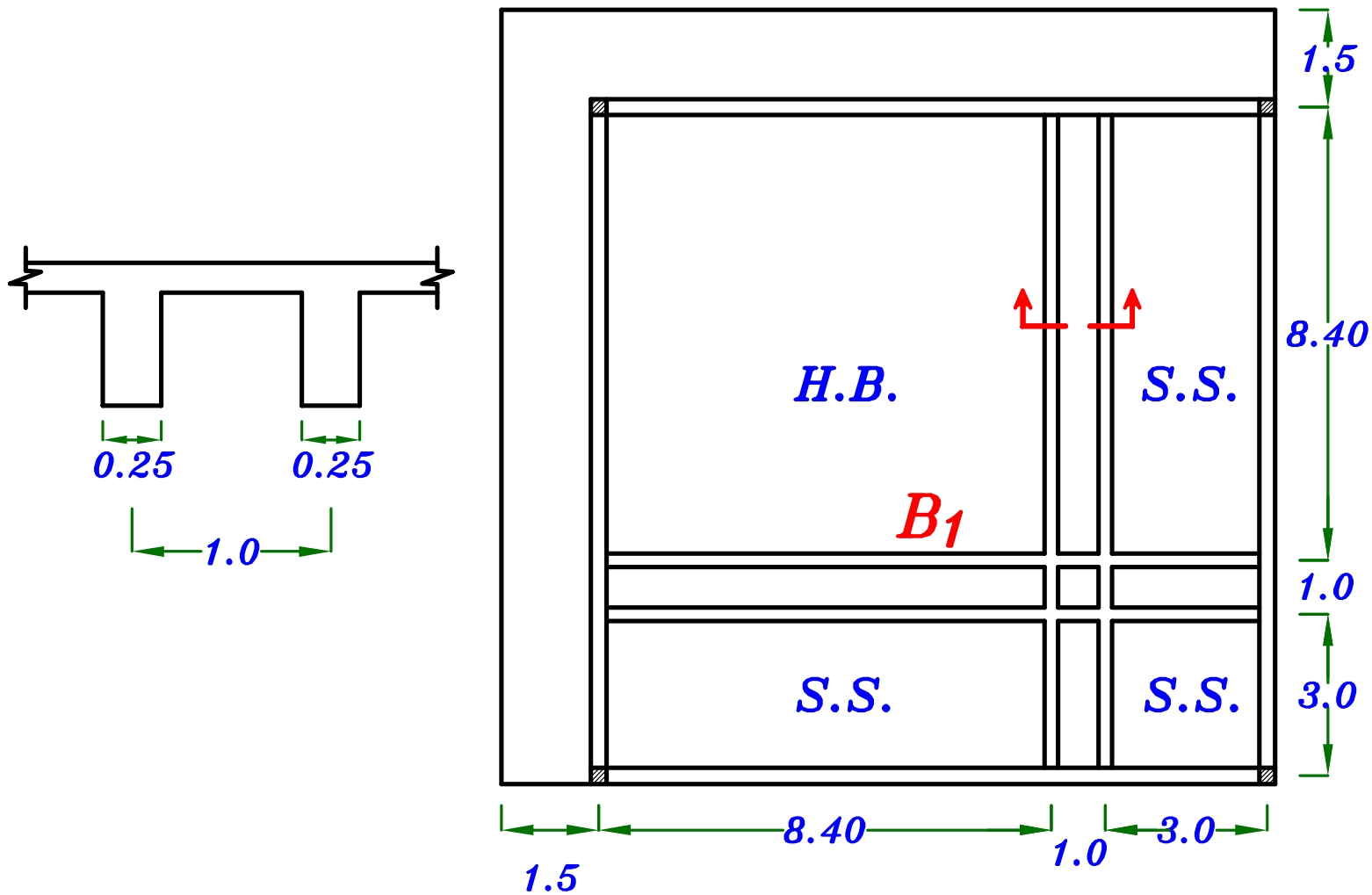
\therefore Use min. Shear RFT.

$$\textcircled{5 \phi 8 \text{ m}}$$

Draw Details of RFT. For the Beams. (B_1, B_2)



Example.



Data.

$$F_{cu} = 25 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

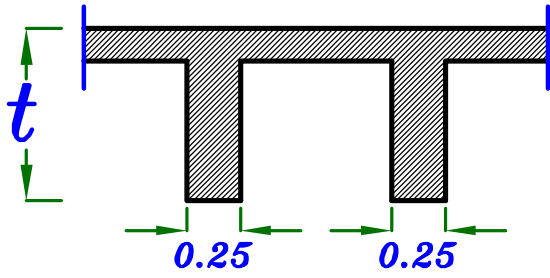
$$F.C. = 2.0 \text{ kN/m}^2, \quad L.L. = 2.0 \text{ kN/m}^2$$

Req.

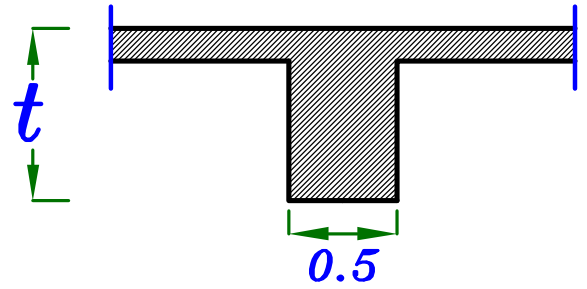
- ① Design the slab & Draw Details of RFT.
- ② Design the panelled Beam B_1
& Draw Details of RFT. in elevation.

فكره المسأله .

ممکن للتسهيل عند حساب الاحمال و تصميم كلا من البلاطه و الكمره اعتبار انه تم ضم الكمرتين المتجاورتين معا و اعتبارهم فى الحسابات كأنها كمره واحده .

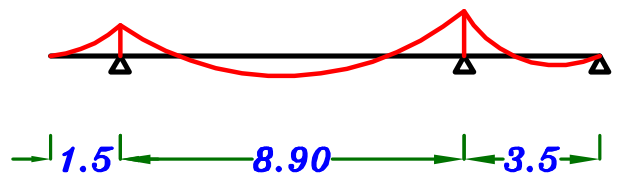
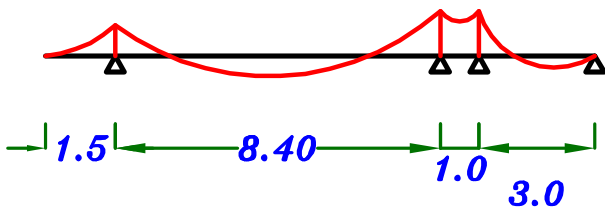
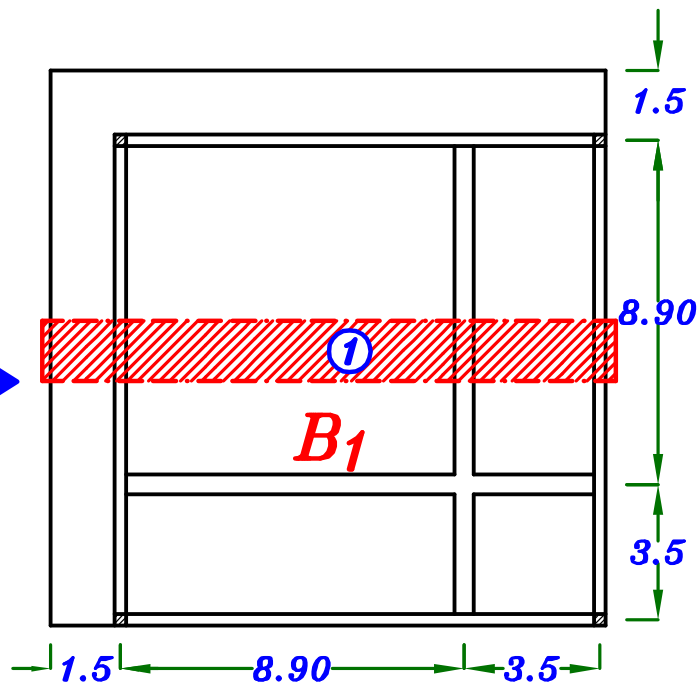
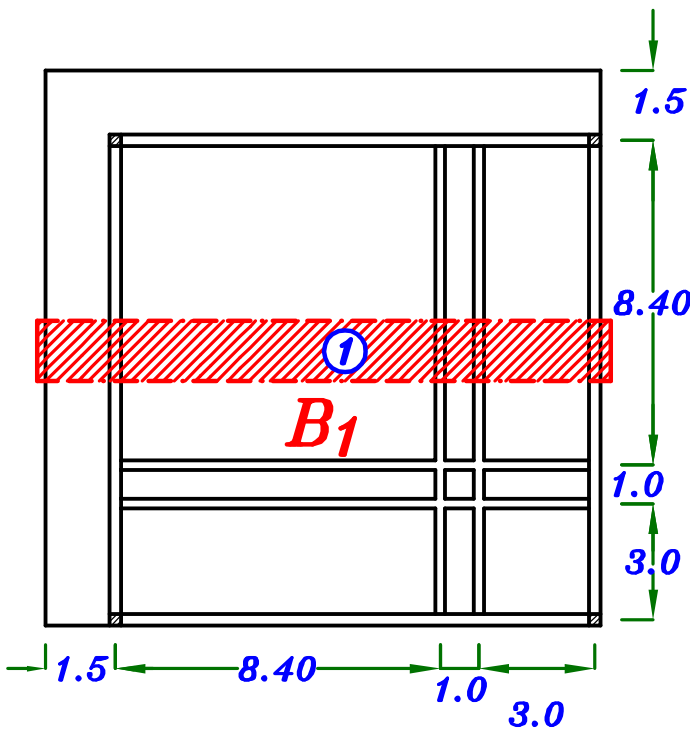


Sec. (1-1)



Sec. (1-1)

و ذلك أثناء حسابات الاحمال و التصميم فقط لكن عند رسم التسليح يجب ان نسلح على الشكل الاصلى . لان هذا ما سيتم تنفيذه فى الحقيقه



α- Choose the Thickness of the Slabs.

α - Choose the Thickness of the Slab. (t_s)

S₁ One way $L_s = 3.5$ m 

$$t_s = \frac{3500}{30} = 116.6 \text{ mm}$$

S₂ two way $L_s = 3.5$ m 

$$t_s = \frac{3500}{40} = 87.5 \text{ mm}$$

S₃ Cantilever $L_c = 1.5$ m

$$t_s = \frac{1500}{10} = 150 \text{ mm}$$

Take (t_s) the bigger value

$$t_s = 150 \text{ mm}$$

S₄ Two way H.B. $L_s = 8.90$ m 

$$t = \frac{8900}{45} = 197 \text{ mm}$$

$$t = 200 \text{ mm}$$

Take

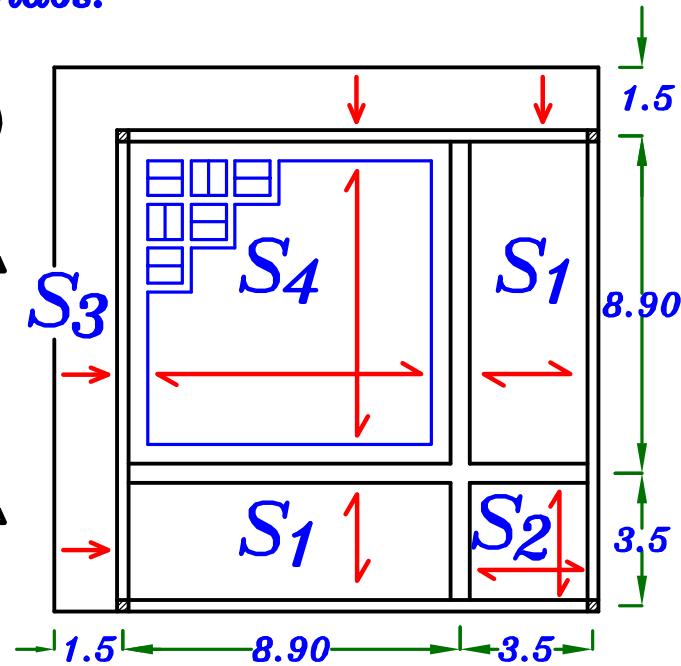
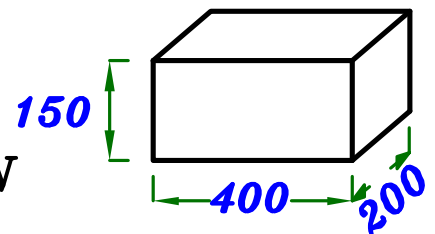
$$t = 200 \text{ mm}$$

$$t_s = 50 \text{ mm}$$

$$h = 150 \text{ mm}$$

The Block ($200 * 400 * 150$)

$h = 150$ mm \longrightarrow Weight of Block = 100 N



***b* – Get the Loads on the Slab**

For Solid Slabs.

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 L.L.$$

$$w_s = 1.4 (0.15 * 25 + 2.0) + 1.6 (2.0) = 11.25 \text{ kN/m}^2$$

For Two way Hollow Blocks.

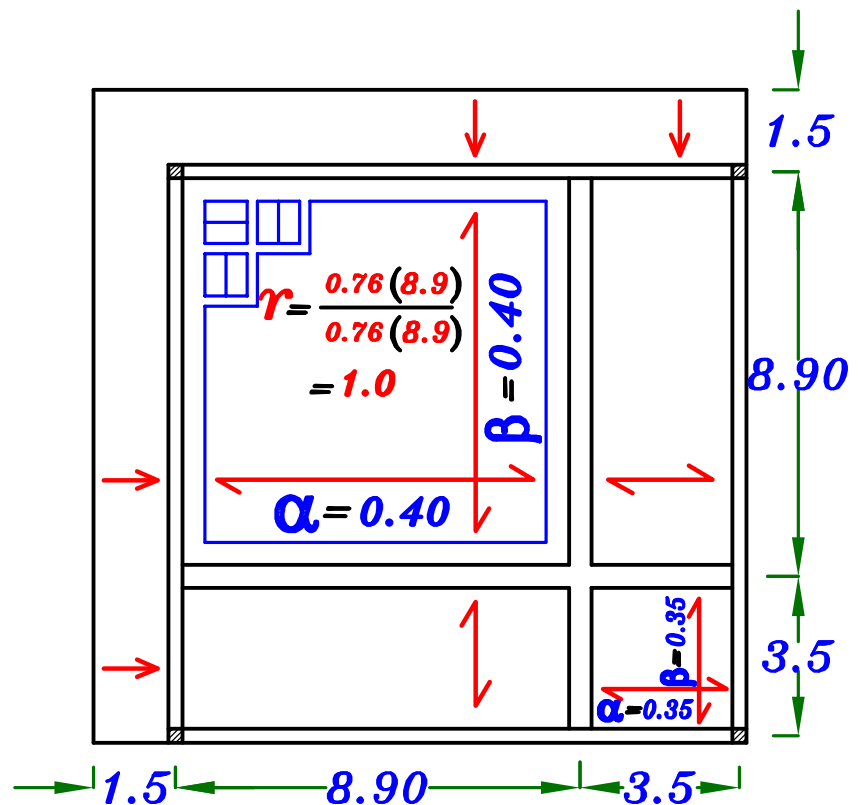
$$w_{ribT} = [1.4 (t_s \delta_c + F.C.) + 1.6 (L.L.)] (S * S) + 1.4 * b * h * (2S - b) * \delta_c + 1.4 * (\text{Block ال وزن}) \left(\frac{e}{a} \right)$$

$$\therefore w_{ribT} = [1.4 (0.05 * 25 + 2.0) + 1.6 (2.0)] (0.5 * 0.5) + 1.4 (0.1 * 0.15 * (2 * 0.5 - 0.1) * 25) + 1.4 \left(\frac{100}{1000} \right) \left(\frac{0.4}{0.2} \right) = 2.69 \text{ (kN \ (S*2S))}$$

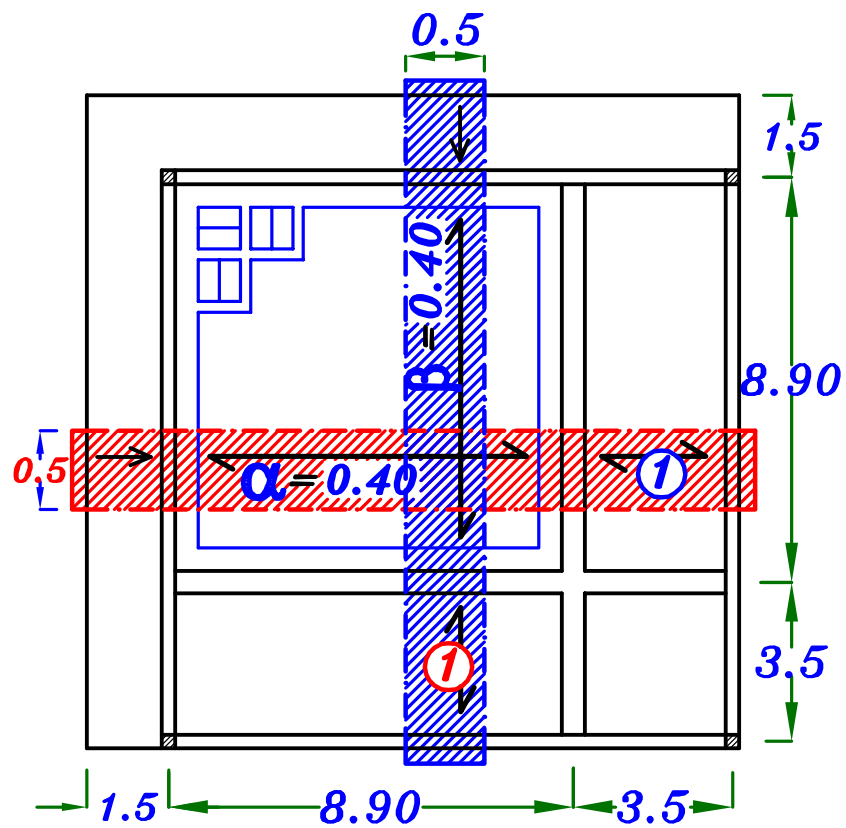
$$w_{rib} = \frac{w_{ribT}}{S} = \frac{2.69}{0.5} = 5.38 \text{ kN \ (S*m)}$$

For H.B.
Use Marcus

For S.S.
Use C.P.



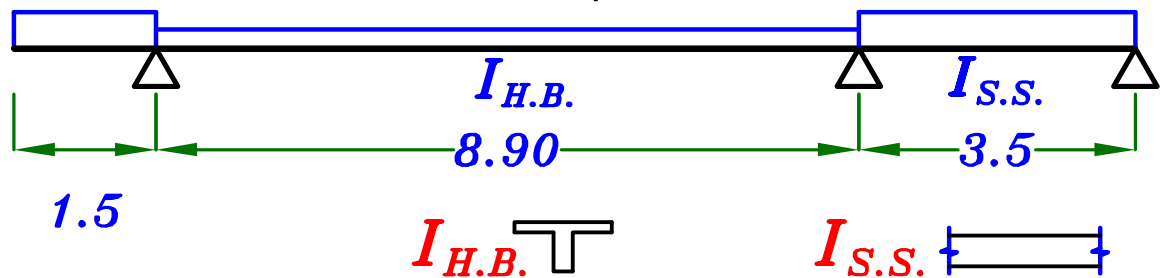
Strip ①



$$\begin{aligned} w_s \cdot S \\ 11.25 \cdot 0.5 \\ = 5.62 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} \alpha w_{rib} \\ 0.40 \cdot 5.38 \\ = 2.15 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} w_s \cdot S \\ 11.25 \cdot 0.5 \\ = 5.62 \text{ kN/m} \end{aligned}$$



$$I_{H.B.} = \text{T-section} \quad I_1 = (\mu \cdot 10^{-4}) B t^3$$

$$B = 0.5 \text{ m}, \quad t = 0.20 \text{ m}$$

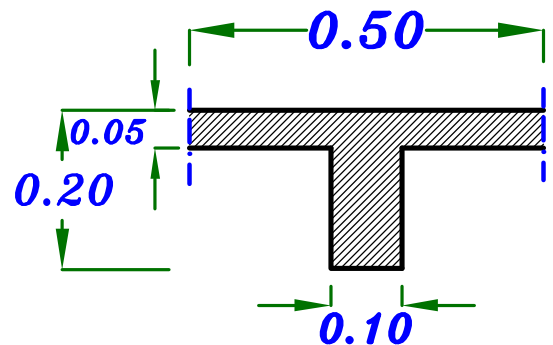
$$\left. \begin{aligned} \frac{t_s}{t} = \frac{0.05}{0.20} = 0.25, \quad \frac{b_o}{B} = \frac{0.1}{0.5} = 0.2 \end{aligned} \right\}$$

From Tables page 91 $\mu = 318$

$$I_{H.B.} = (318 \cdot 10^{-4} \cdot 0.5 \cdot 0.20^3) = 1.27 \cdot 10^{-4} \text{ m}^4$$

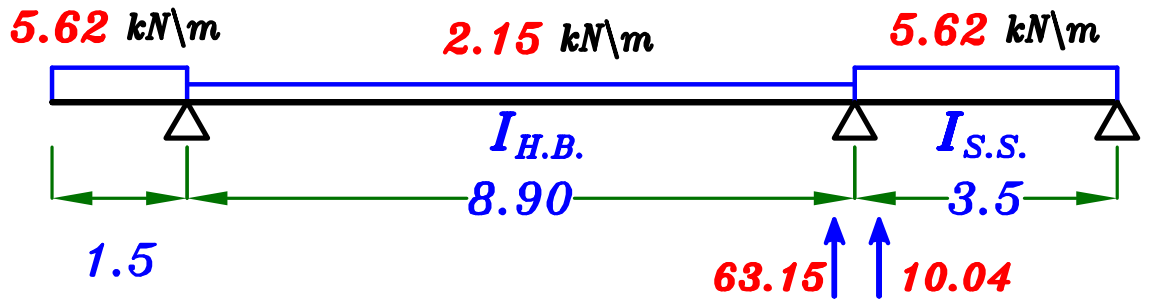
$$I_{S.S.} = \frac{S(t_s)^3}{12} = \frac{0.5(0.15)^3}{12} = 1.40 \cdot 10^{-4} \text{ m}^4$$

$$\therefore \frac{I_{H.B.}}{I_{S.S.}} = \frac{1.27 \cdot 10^{-4}}{1.40 \cdot 10^{-4}} = 0.907 \quad \therefore \boxed{I_{H.B.} = 0.907 I_{S.S.}}$$



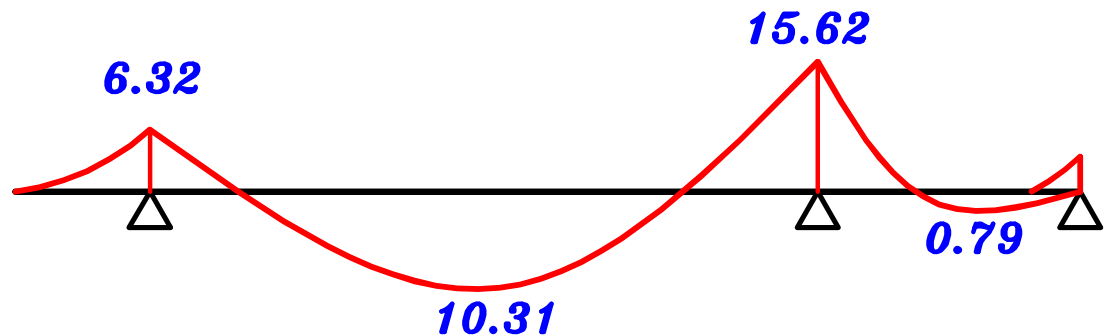
$$M_c = -6.32$$

$$M_1$$

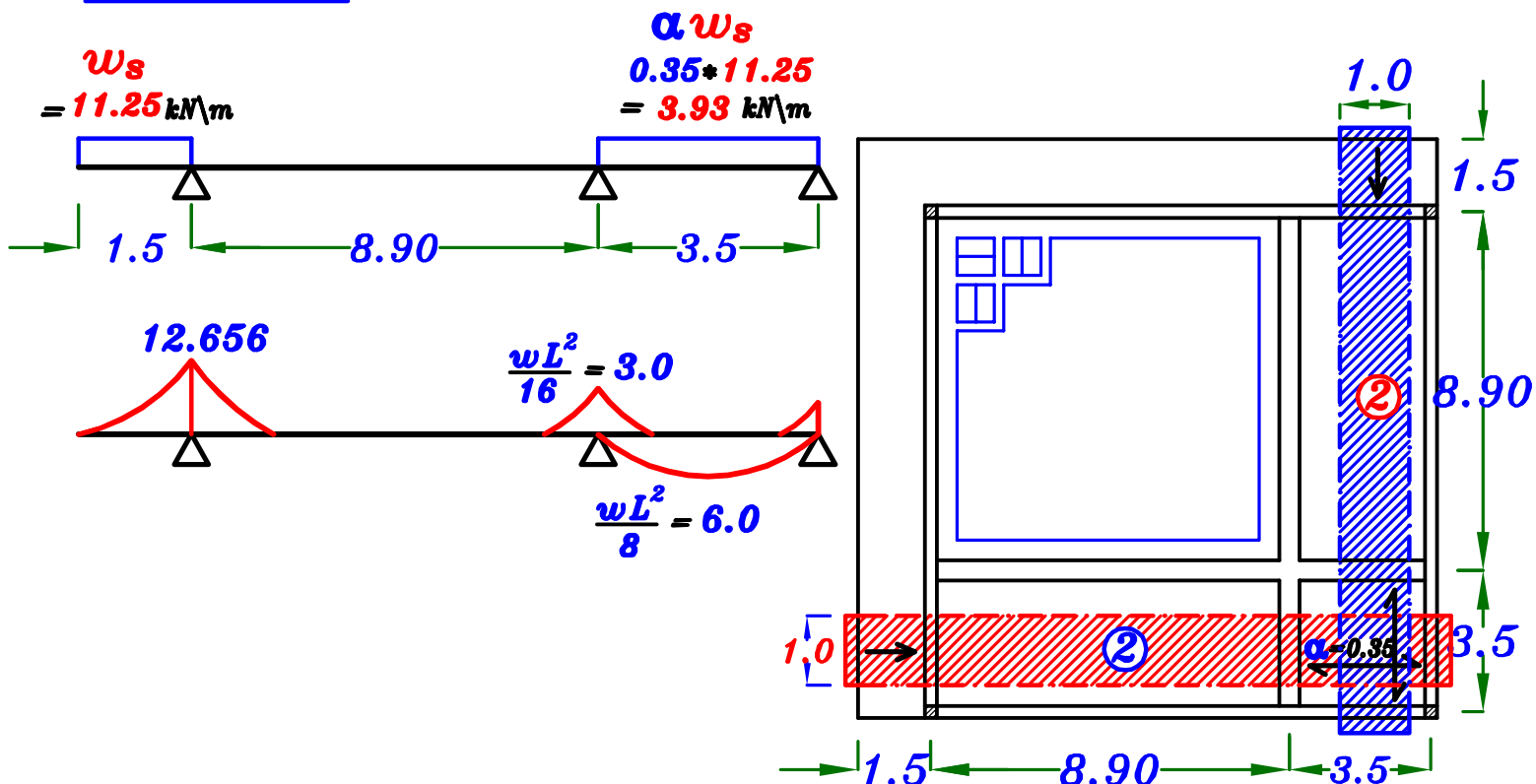


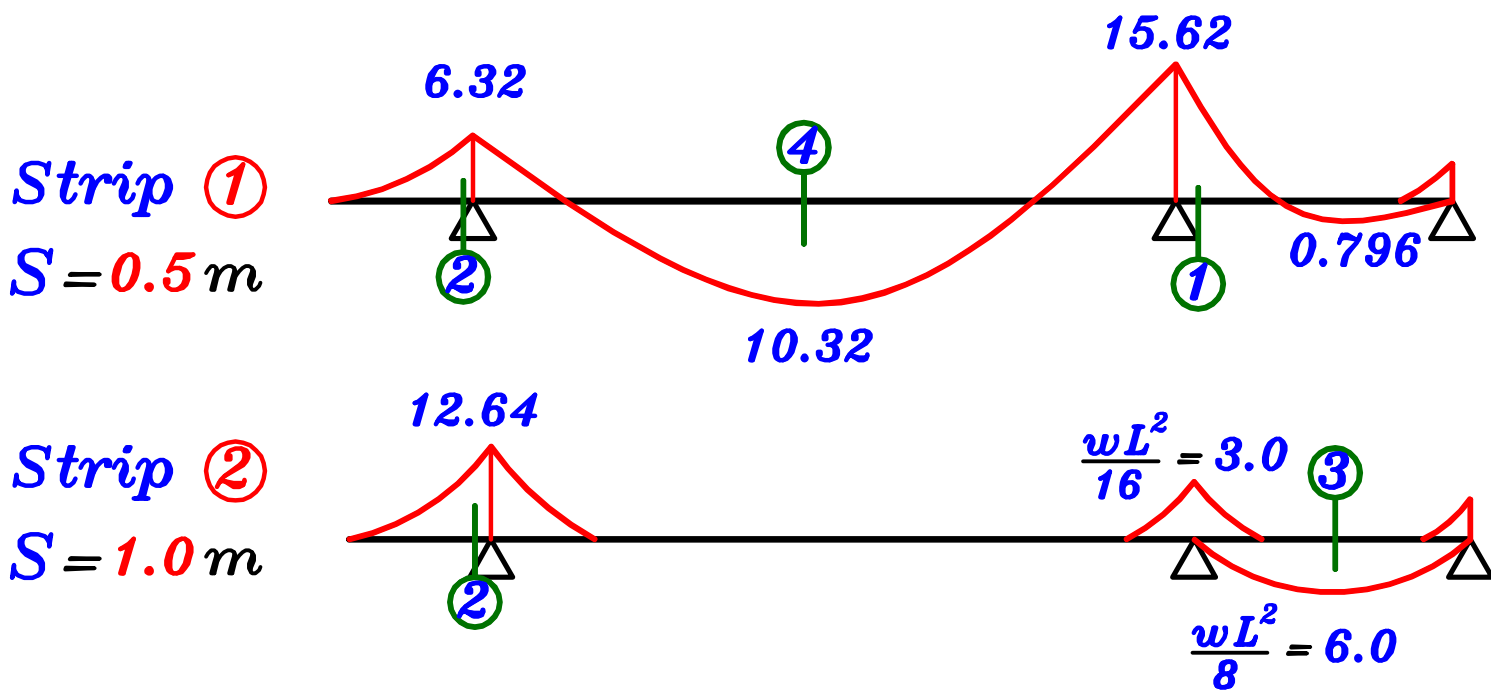
$$-6.32 \left(\frac{8.90}{0.907 I_{S.S.}} \right) + 2M_1 \left(\frac{8.90}{0.907 I_{S.S.}} + \frac{3.5}{I_{S.S.}} \right) + 0.0 = -6 \left(\frac{63.15}{0.907 I_{S.S.}} + \frac{10.04}{I_{S.S.}} \right)$$

$$M_1 = -15.45 \text{ kN.m} / 0.5 \text{ m}$$



Strip ②





Sec. ① S.S. $M_{U.L.} = 15.62 \text{ kN.m/rib}$

$t = 150 \text{ mm}$, $d = 150 - 20 = 130 \text{ mm}$, $S = 500 \text{ mm}$ عرض الشريحة

$$130 = C_1 \sqrt{\frac{15.62 \cdot 10^6}{25 \cdot 500}} \longrightarrow C_1 = 3.678 \longrightarrow J = 0.791$$

$$A_s = \frac{15.62 \cdot 10^6}{0.791 \cdot 360 \cdot 130} = 421.95 \text{ mm}^2 / 0.5 \text{ m}$$

$$A_s = \frac{421.95}{0.50} = 843.9 \text{ mm}^2 / \text{m} \quad \text{عدد زوجي} \quad \boxed{8 \phi 12 \text{ m}}$$

Sec. ② S.S. $M_{U.L.} = 6.32 \text{ kN.m/rib}$

$t = 150 \text{ mm}$, $d = 150 - 20 = 130 \text{ mm}$, $S = 500 \text{ mm}$ عرض الشريحة

$$130 = C_1 \sqrt{\frac{6.32 \cdot 10^6}{25 \cdot 500}} \longrightarrow C_1 = 5.78 \longrightarrow J = 0.826$$

$$A_s = \frac{6.32 \cdot 10^6}{0.826 \cdot 360 \cdot 130} = 163.5 \text{ mm}^2 / 0.5 \text{ m}$$

$$A_s = \frac{163.5}{0.50} = 326.98 \text{ mm}^2 / \text{m} \quad \text{عدد زوجي} \quad \boxed{6 \phi 10 \text{ m}}$$

Sec. ③ S.S. $M_{U.L.} = 6.0 \text{ kN.m/rib}$

$t = 150 \text{ mm}$, $d = 150 - 20 = 130 \text{ mm}$, $S = 1000 \text{ mm}$ عرض الشريحة

$$130 = C_1 \sqrt{\frac{6.0 * 10^6}{25 * 1000}} \longrightarrow C_1 = 8.39 \longrightarrow J = 0.826$$

$$A_s = \frac{6.0 * 10^6}{0.826 * 360 * 130} = 155.2 \text{ mm}^2/\text{m} \quad \textcircled{5 \phi 10 \backslash \text{m}}$$

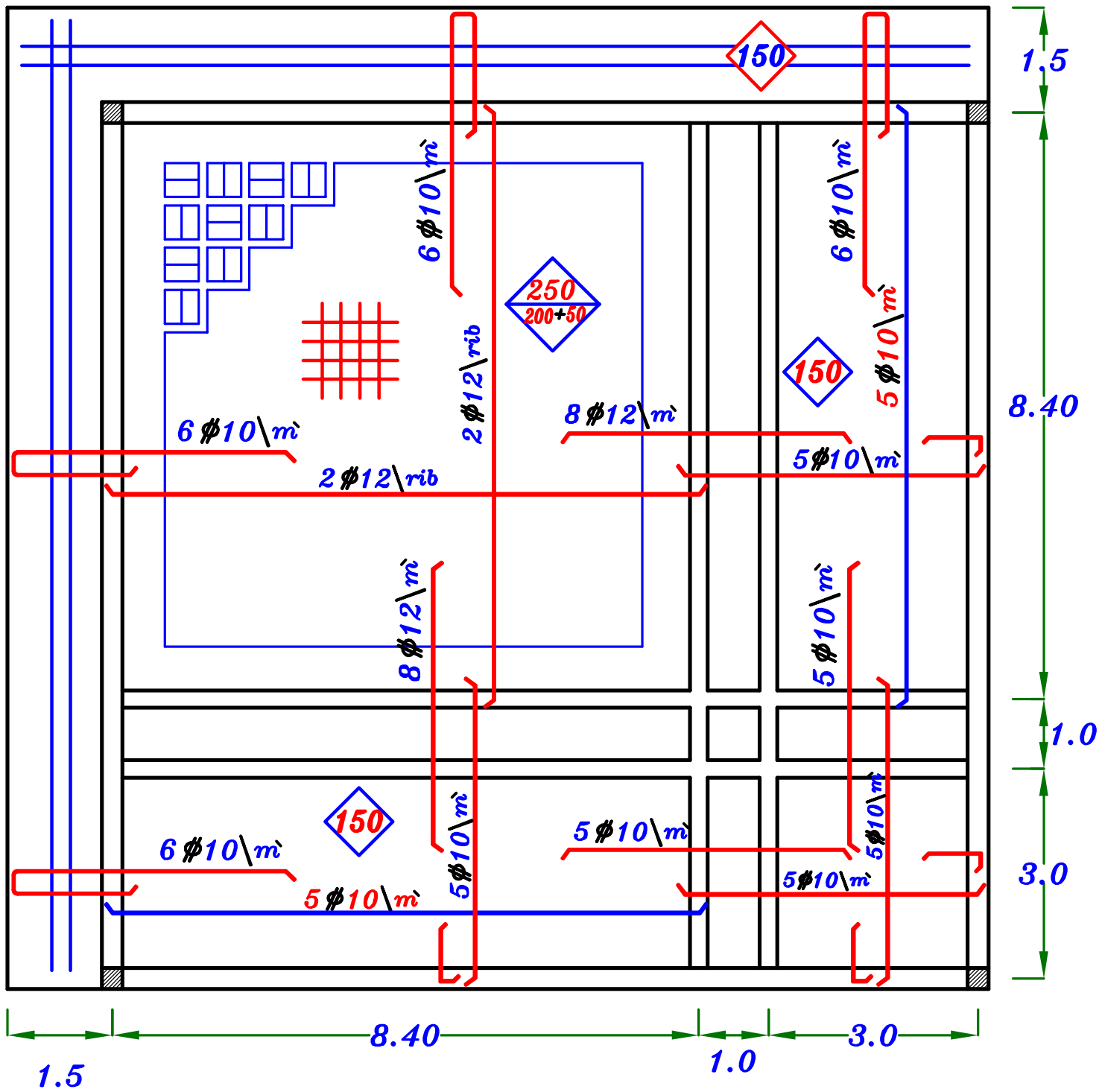
Sec. ④ H.B. $M_{U.L.} = 10.32 \text{ kN.m/rib}$

$t = 200 \text{ mm}$, $d = 200 - 30 = 170 \text{ mm}$, $S = 500 \text{ mm}$ عرض الشريحة

$$170 = C_1 \sqrt{\frac{10.32 * 10^6}{25 * 500}} \longrightarrow C_1 = 5.917 \longrightarrow J = 0.826$$

$$A_s = \frac{10.32 * 10^6}{0.826 * 360 * 170} = 204.11 \text{ mm}^2/\text{rib} \quad \textcircled{2 \phi 12 \backslash \text{rib}}$$

RFT. of the slabs.



Design of Panelled Beams.

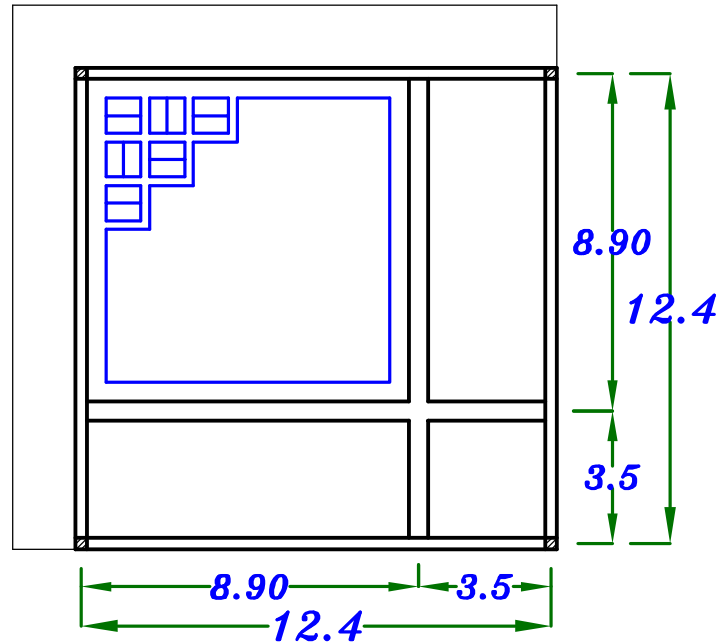
a – Get the Dimensions of the beam. (**b, t**)

Take **b = 0.50 m**

$$t = \frac{L_s}{16} = \frac{12.4}{16} = 0.775 \text{ m} \\ = 0.80 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$t = 0.80 \text{ m}$$



b – Get the Loads on the Slab. (**w_{av}**)

$$w_{av.} = \frac{\text{Total Weight of Solid slabs} + \text{Total Weight of H.B. slabs} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

$$w_{av.} = \frac{w_s \cdot \text{area (s.s.)} + \left(\frac{w_{rib}}{S}\right) \cdot \text{area (H.B.)} + \text{Total Weight of Panelled Beams}}{\text{Total area}}$$

$$w_{av.} = \frac{w_s \cdot (L \cdot L_s - a \cdot b) + \left(\frac{w_{rib}}{S}\right) \cdot (a \cdot b) + [1.4 \cdot b(t - t_s)(2L) \cdot \delta_c]}{L \cdot L_s}$$

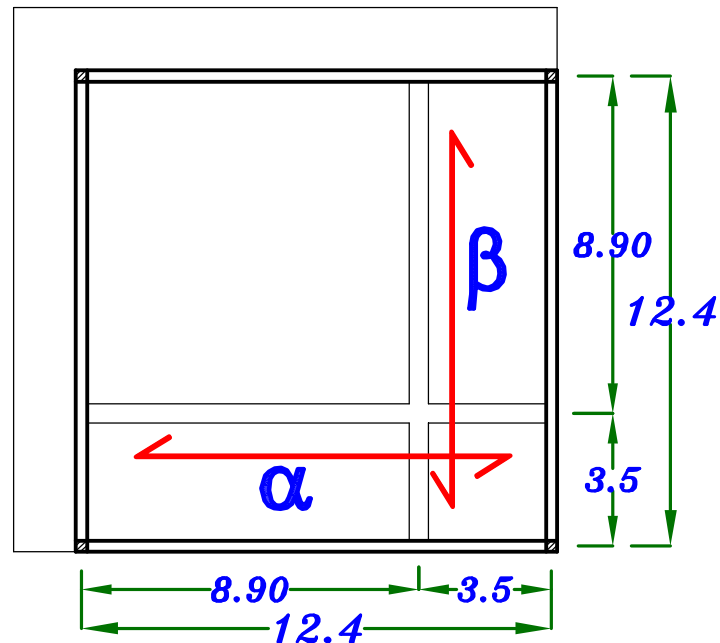
$$w_{av.} = \frac{11.25(12.4 \cdot 12.4 - 8.9 \cdot 8.9) + \left(\frac{5.38}{0.5}\right)(8.9 \cdot 8.9) + 1.4 \cdot 0.50(0.80 - 0.15)[2 \cdot 12.4] \cdot 25}{12.4 \cdot 12.4} \\ = 12.83 \text{ kN/m}^2$$

C – Calculate α , β By using Grashoff.

$$r = \frac{m L}{m' L_s} = \frac{(1.0) 12.4}{(1.0) 12.4} = 1.0$$

$$\alpha = \frac{r^4}{1+r^4} = \frac{(1.0)^4}{1+(1.0)^4} = 0.50$$

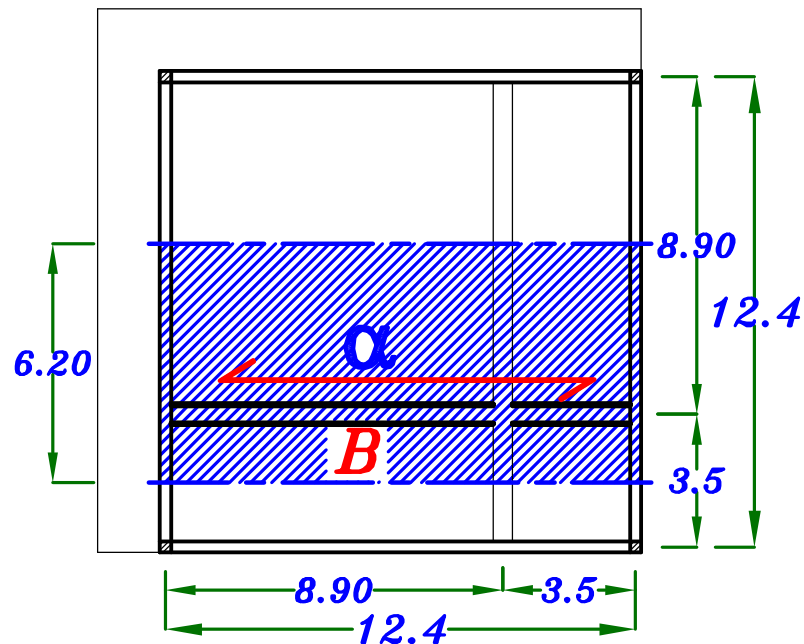
$$\beta = \frac{1}{1+r^4} = \frac{1}{1+(1.0)^4} = 0.50$$



B

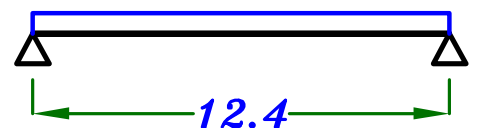
$$\alpha = 6.20 \text{ m}$$

$$\begin{aligned} w_1 &= w_{av.} * \alpha * \beta \\ &= 12.83 * 6.20 * 0.50 \\ &= 39.77 \text{ kN/m} \end{aligned}$$



$$M = 39.77 * \frac{12.4^2}{8} = 764.4 \text{ kN.m}$$

$$w_1 = 39.77 \text{ kN/m}$$

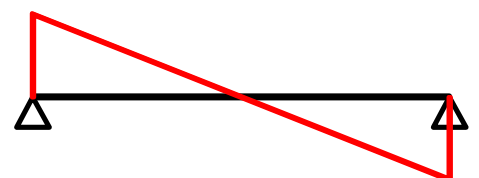


B.M.D.



$$246.5 \text{ kN} \quad 764.4 \text{ kN.m}$$

S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90}\right)$

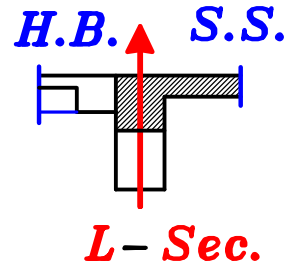
$$X = 3.5 \text{ m}, \frac{L}{2} = 6.2 \text{ m} \quad \Theta_{B_1} = \frac{3.5}{6.2} * 90^\circ = 50.80^\circ$$

$$M_1 = 764.4 * \frac{\sin 50.80^\circ}{\sin 90^\circ} = 592.4 \text{ kN.m}$$

F – Design the Panelled Beam. *B*

\therefore Cover = 70 mm Symmetric

$$t = 800 \text{ mm} \quad d = 800 - 70 = 730 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 1.75 \text{ m} = 1750 \text{ mm} \\ 6 t_s + b = 6 * 150 + 500 = 1400 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{12400}{10} + 500 = 1740 \text{ mm} \end{array} \right\} \quad B = 1400 \text{ mm}$$

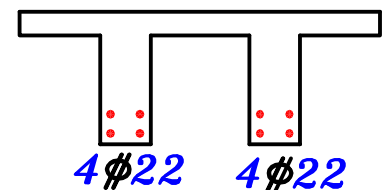
$$730 = C_1 \sqrt{\frac{592.4 * 10^6}{25 * 1400}} \rightarrow C_1 = 5.61 \rightarrow J = 0.826$$

$$A_s = \frac{592.4 * 10^6}{0.826 * 360 * 730} = 2729 \text{ mm}^2$$

Check $A_{s \min.}$ $A_{s \text{ req.}} = 3746.2 \text{ mm}^2$

$$\mu_{\min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y}\right) b d = \left(0.225 * \frac{\sqrt{25}}{360}\right) 350 * 1500 = 1640.6 \text{ mm}^2$$

$$\therefore A_{s \text{ req.}} > \mu_{\min.} b d \therefore \text{Take } A_s = A_{s \text{ req.}} = 3746.2 \text{ mm}^2 \quad (8 \phi 22)$$



$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (272 \rightarrow 544 \text{ mm}^2) \quad (6 \phi 10)$$

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

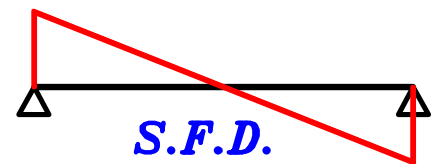
$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

$$q_s = \frac{Q_{max}}{b d} = \frac{246.5 \times 10^3}{500 \times 730} = 0.675 \text{ N/mm}^2 \therefore q_s < q_{cu}$$

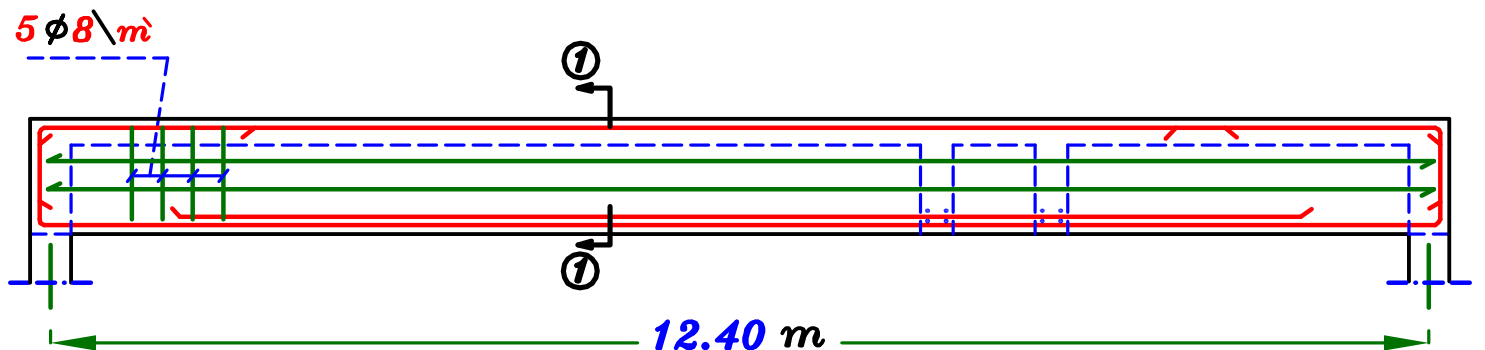
\therefore Use min. Shear RFT.

5 ϕ 8/m

246.5 kN



Draw Details of RFT. For the Beam.



3 ϕ 10 each Side

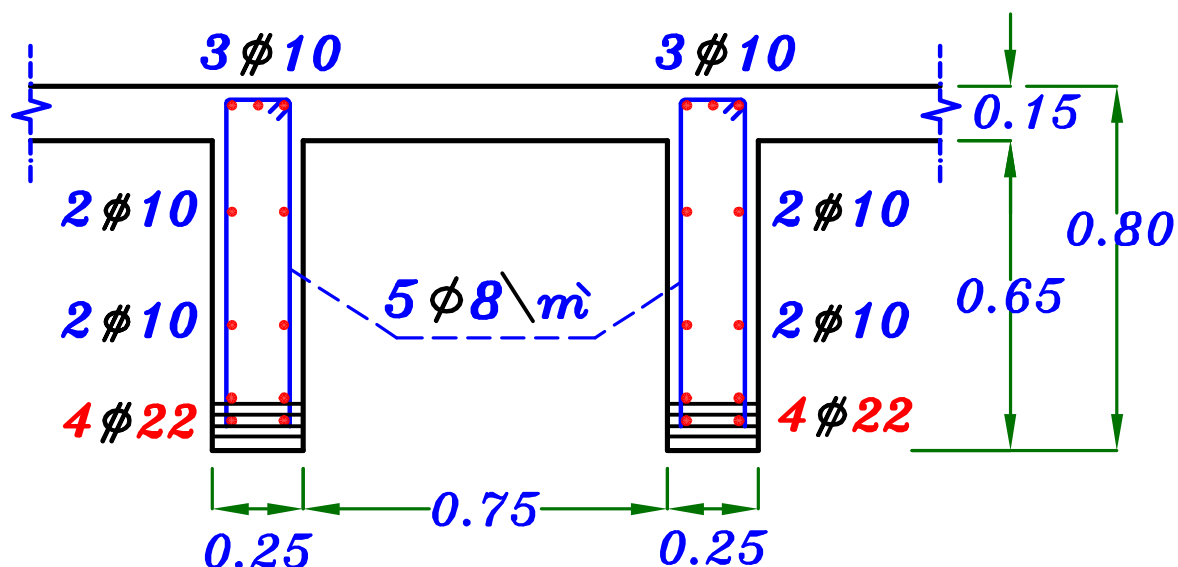
2 ϕ 18 each Side

2 ϕ 18 each Side

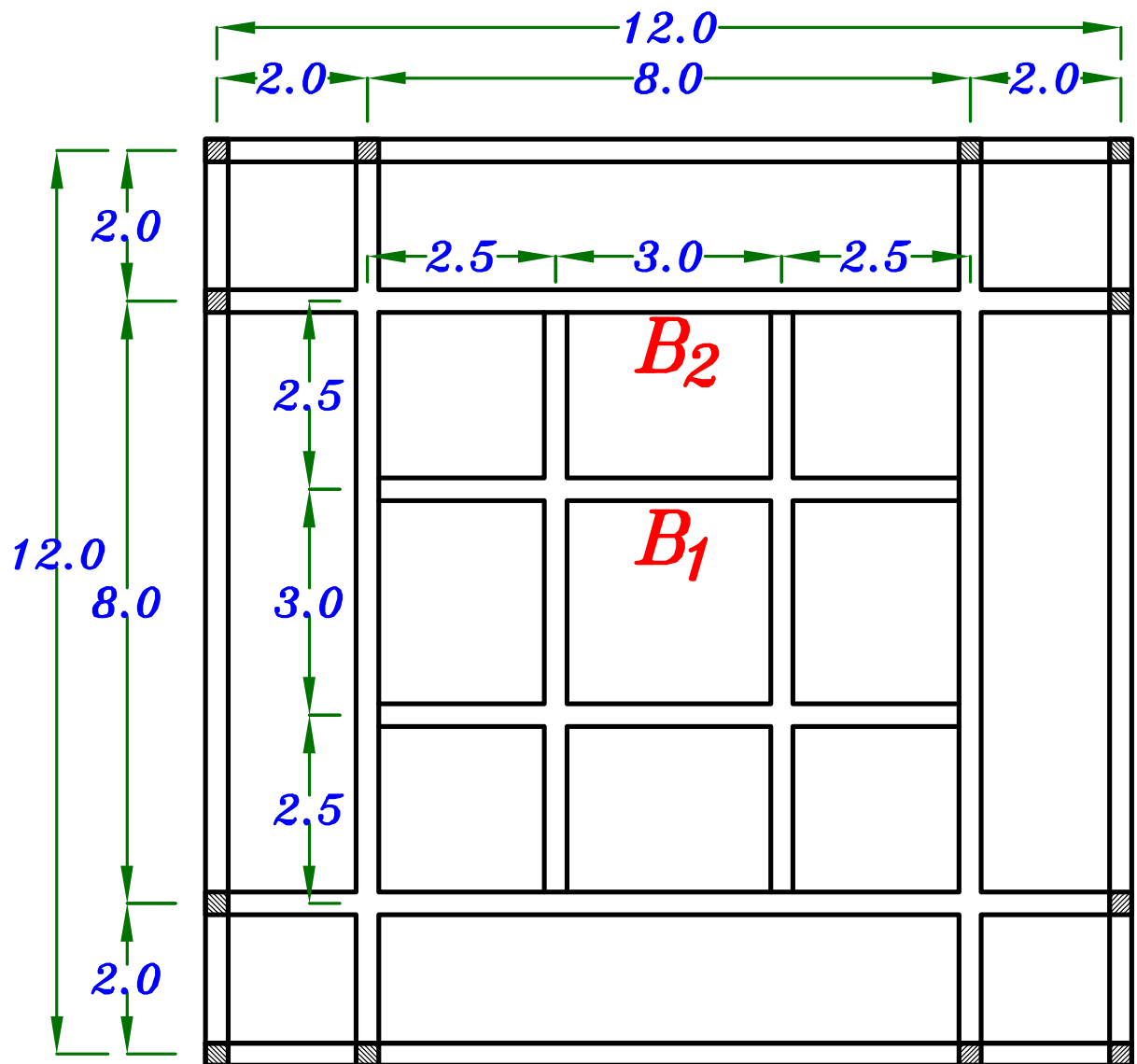
2 ϕ 22 each Side

2 ϕ 22 each Side

Sec. (1-1)



Example.



Data.

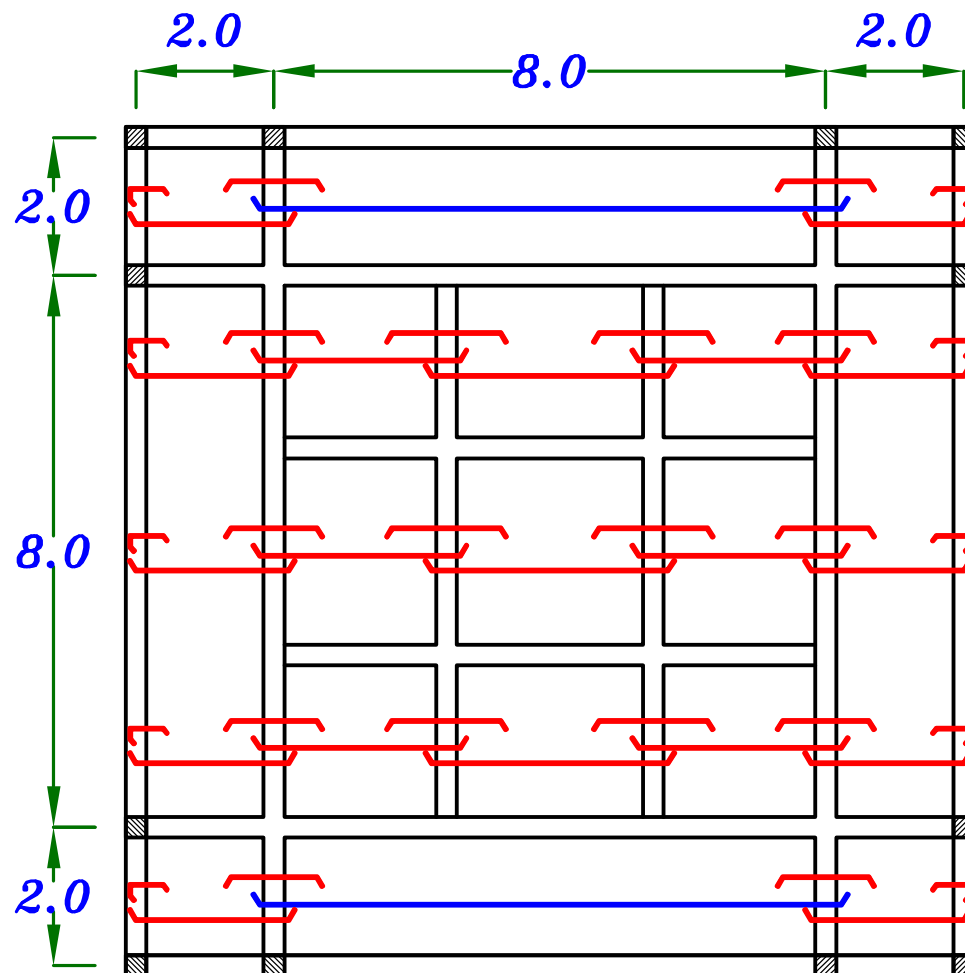
$$F_{cu} = 25 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

$$F.C. = 1.5 \text{ kN/m}^2, \quad L.L. = 2.0 \text{ kN/m}^2$$

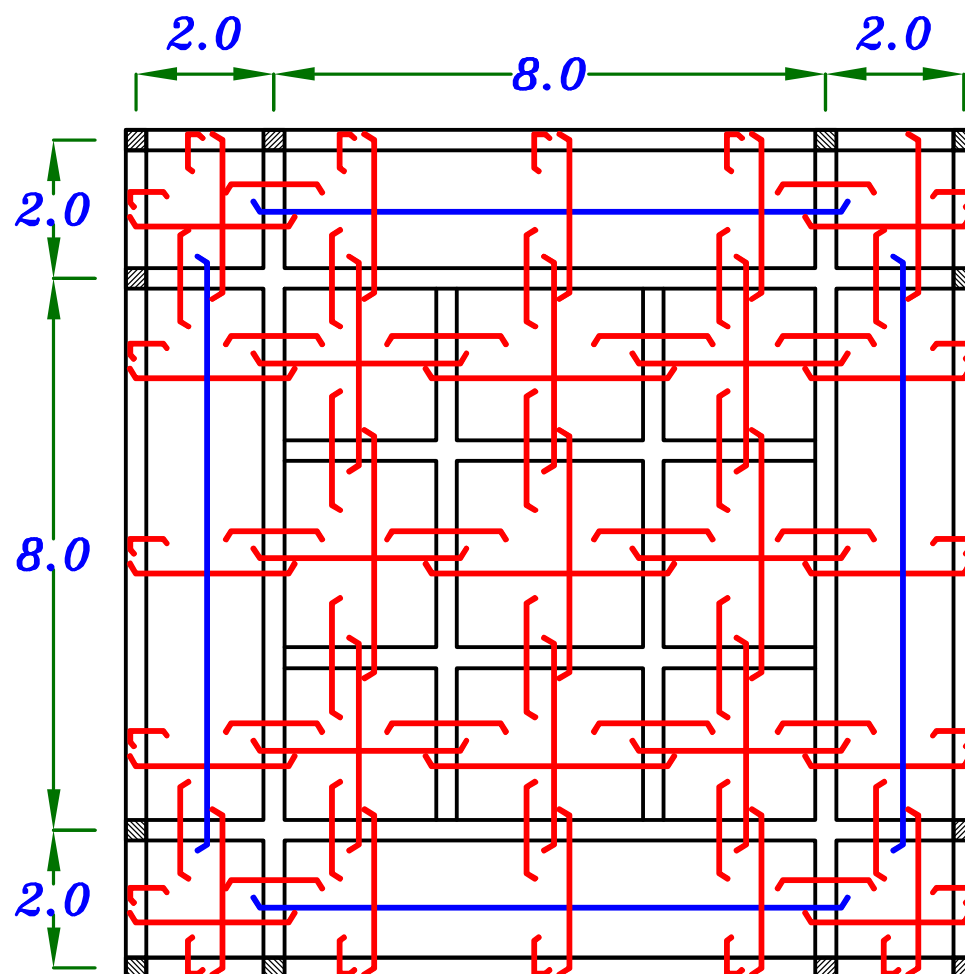
Req.

- ① Draw a sketch For the reinforcement of slabs in plan.
- ② Design the panelled Beams B_1 , B_2
& Draw Details of RFT. in elevation.

Sketch For the reinforcement of slabs in plan.



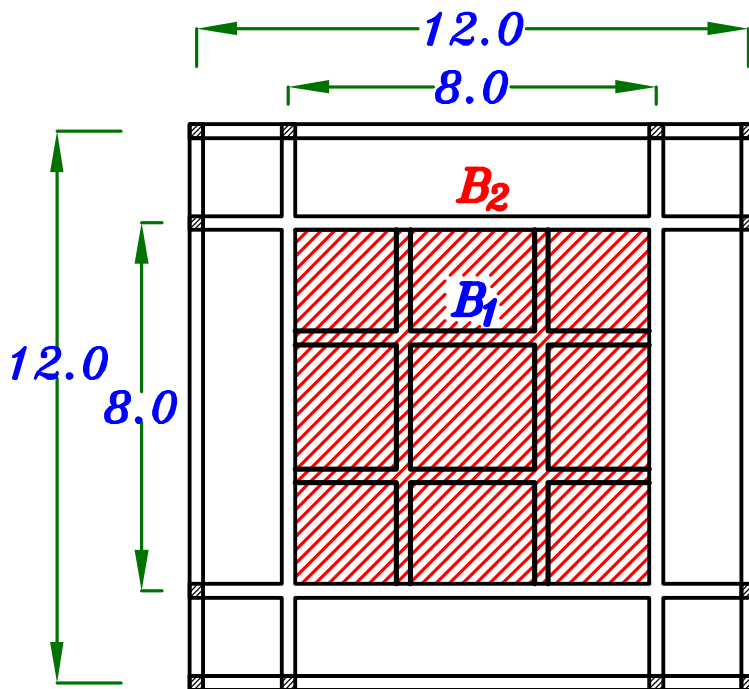
تسليح البلاطات
في اتجاه واحد فقط



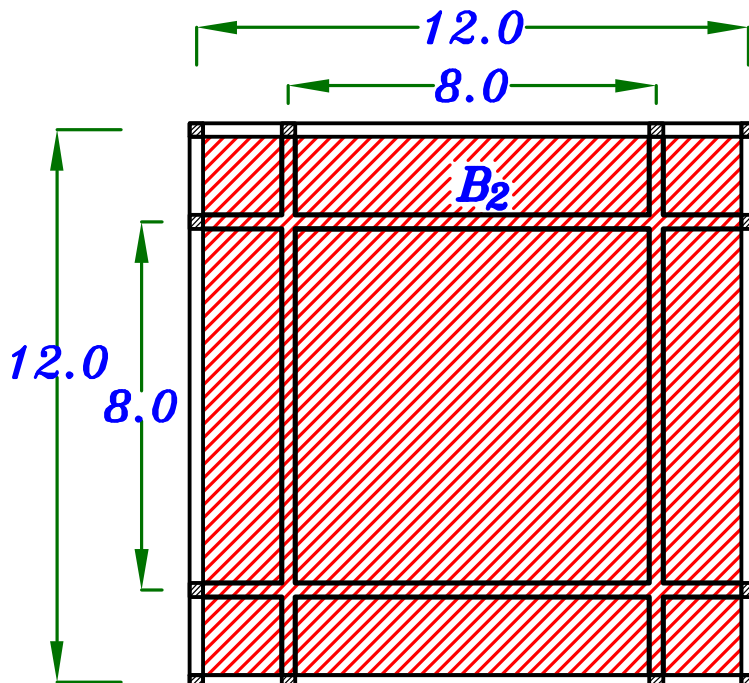
تسليح البلاطات
في الاتجاهين

فكره المسأله .

نصمم اولاً شبكه الكمرات B_1 حيث تكون مساحه الشبكه (8.0×8.0)



ثم نصمم شبكه الكمرات B_2 حيث تكون مساحه الشبكه (12.0×12.0)



a - Choose the Thickness of the Slab. (t_s)

S_1 two way $L_s = 3.0$ m

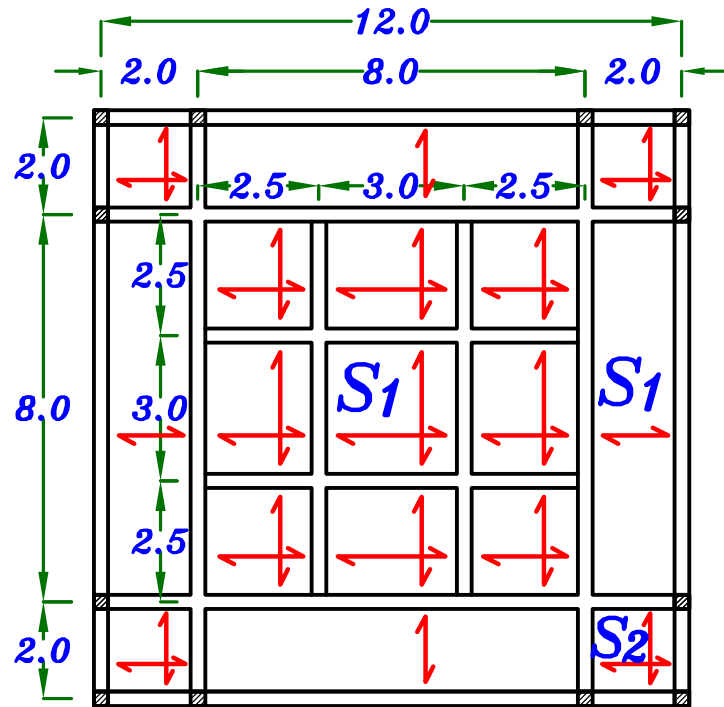
$$t_s = \frac{3000}{45} = 66.6 \text{ mm}$$

S_2 two way $L_s = 2.0$ m

$$t_s = \frac{2000}{40} = 50.0 \text{ mm}$$

S_3 One way $L_s = 2.0$ m

$$t_s = \frac{2000}{30} = 66.6 \text{ mm}$$



Take (t_s) the bigger value

$$t_s = 80 \text{ mm}$$

b - Get the Loads on the Slab (w_s).

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 L.L.$$

$$w_s = 1.4 (0.08 * 25 + 1.5) + 1.6 (2.0) = 8.10 \text{ kN/m}^2$$

Design the Panelled Beam. B_1

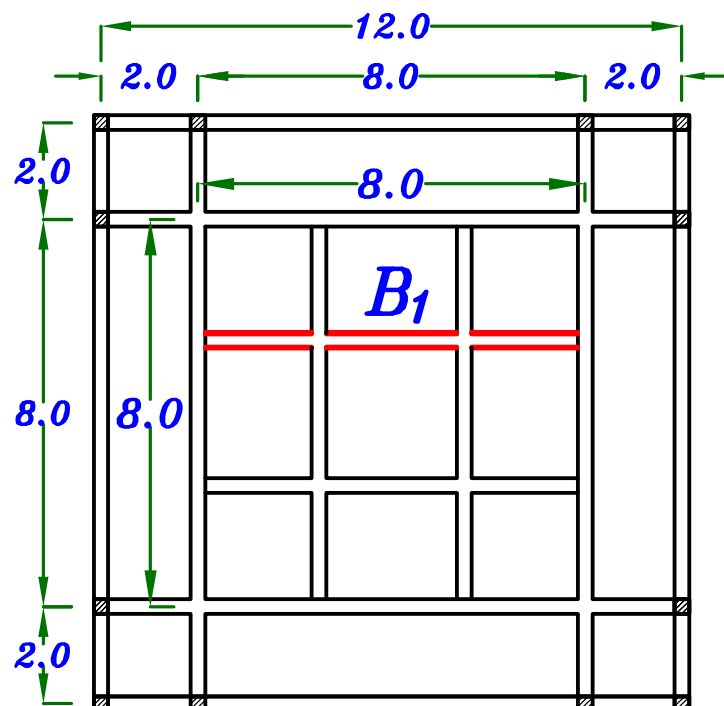
a - Get the Dimensions of the beam. (b, t)

Take $b = 0.25$ m

$$t = \frac{L_s}{16} = \frac{8.0}{16} = 0.50 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$t = 0.50 \text{ m}$$



b – Get the Loads on the Slab. (w_{av})

$$w_{av.} = w_s + \frac{\text{Total Weight of Panelled Beams}}{L * L_s}$$

$$w_{av.} = w_s + \frac{1.4 * b (t - t_s) [\text{مجموع أطوال الكمرات الداخلية}] * \delta_c}{L * L_s}$$

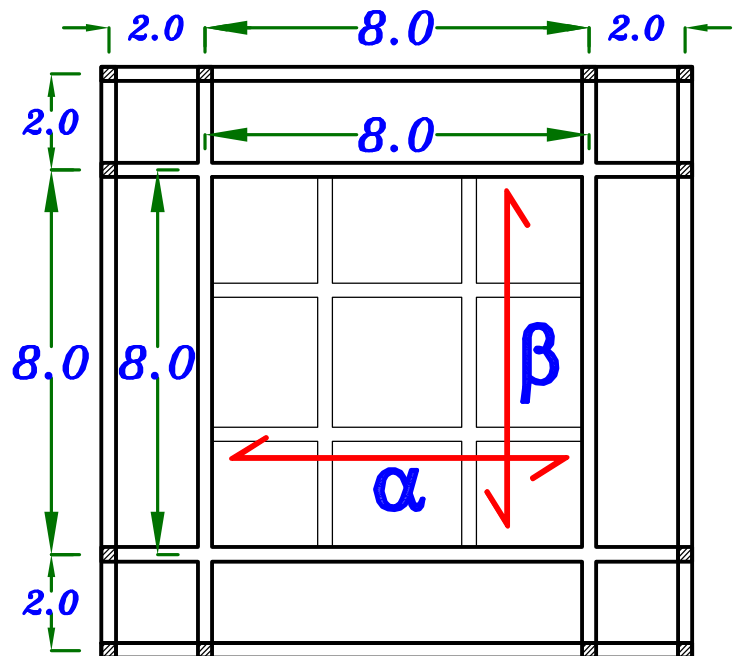
$$w_{av.} = 8.10 + \frac{1.4 * 0.25 (0.5 - 0.08) [2 * 8 + 2 * 8] * 25}{8.0 * 8.0} = 9.93 \text{ kN/m}^2$$

c – Calculate α , β By using Grashoff.

$$r = \frac{m L}{m_s L_s} = \frac{(1.0) 8.0}{(1.0) 8.0} = 1.0$$

$$\alpha = \frac{r^4}{1 + r^4} = \frac{(1.0)^4}{1 + (1.0)^4} = 0.5$$

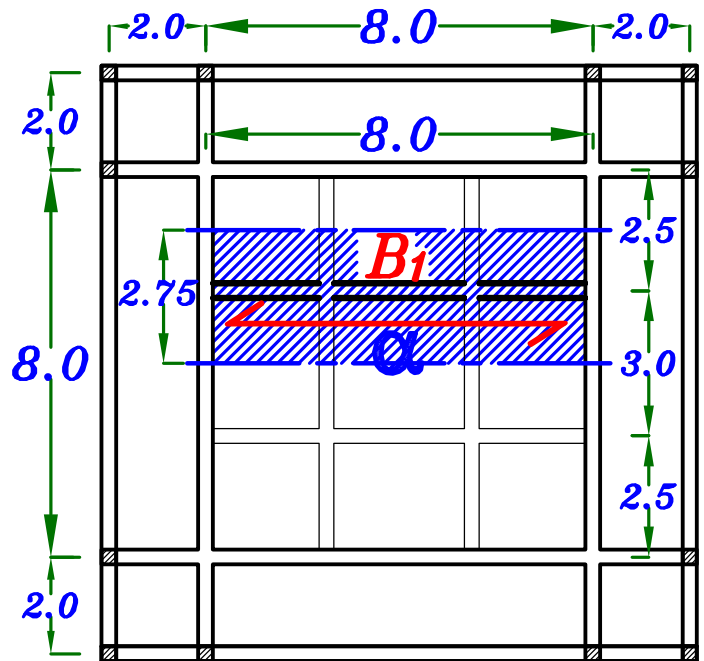
$$\beta = \frac{1}{1 + r^4} = \frac{1}{1 + (1.0)^4} = 0.5$$



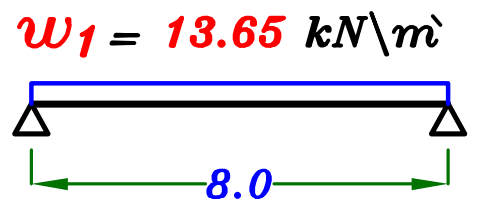
d – Get the Loads on the Panelled Beam & Calculate the B.M.

$$\alpha = 2.75 \text{ m}$$

$$\begin{aligned} w_1 &= w_{av.} * \alpha * \alpha \\ &= 9.93 * 2.75 * 0.50 \\ &= 13.65 \text{ kN/m} \end{aligned}$$



$$M = 13.65 * \frac{8.0^2}{8} = 109.2 \text{ kN.m}$$

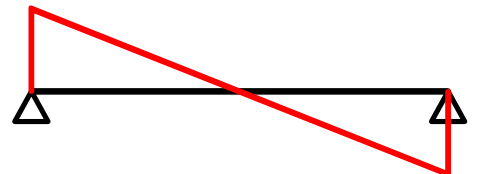


B.M.D.



54.6 kN 109.2 kN.m

S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

$$X = 2.5 \text{ m} , \quad \frac{L}{2} = 4.0 \text{ m}$$

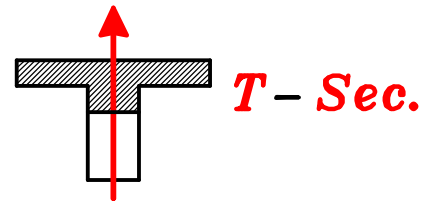
$$\theta_{B_1} = \frac{2.5}{4.0} * 90^\circ = 56.25^\circ$$

$$M_1 = 109.2 * \frac{\sin 56.25^\circ}{\sin 90^\circ} = 90.79 \text{ kN.m}$$

F- Design the Panelled Beam. B_1

∴ **Cover = 70 mm** **Symmetric**

$$t = 500 \text{ mm} \quad d = 500 - 70 = 430 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 2.75 \text{ m} = 2750 \text{ mm} \\ 16 t_s + b = 16 * 80 + 250 = 1530 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{8000}{5} + 250 = 1850 \text{ mm} \end{array} \right\} \quad \boxed{B = 1530 \text{ mm}}$$

$$430 = C_1 \sqrt{\frac{90.79 * 10^6}{25 * 1530}} \rightarrow C_1 = 8.82 \rightarrow J = 0.826$$

$$A_s = \frac{90.79 * 10^6}{0.826 * 360 * 430} = 710.0 \text{ mm}^2$$

Check $A_{s \min.}$ $A_{s \text{ req.}} = 710.0 \text{ mm}^2$

$$\mu_{\min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 430 = 335.9 \text{ mm}^2$$

∴ $A_{s \text{ req.}} > \mu_{\min.} b d$ ∴ Take $A_s = A_{s \text{ req.}} = 710.0 \text{ mm}^2$ **4 ϕ 16**

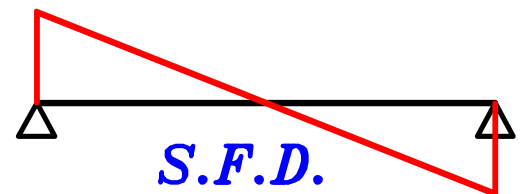
Stirrup Hangers = (0.1 → 0.2) A_s = (71 → 142 mm²) **2 ϕ 10**

Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u \text{ max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

54.6 kN



$$q_s = \frac{Q_{\text{max}}}{b d} = \frac{54.6 * 10^3}{250 * 430} = 0.507 \text{ N/mm}^2 \quad \therefore q_s < q_{cu}$$

∴ Use min. Shear RFT.

5 ϕ 8

Design the Panelled Beam. B_2

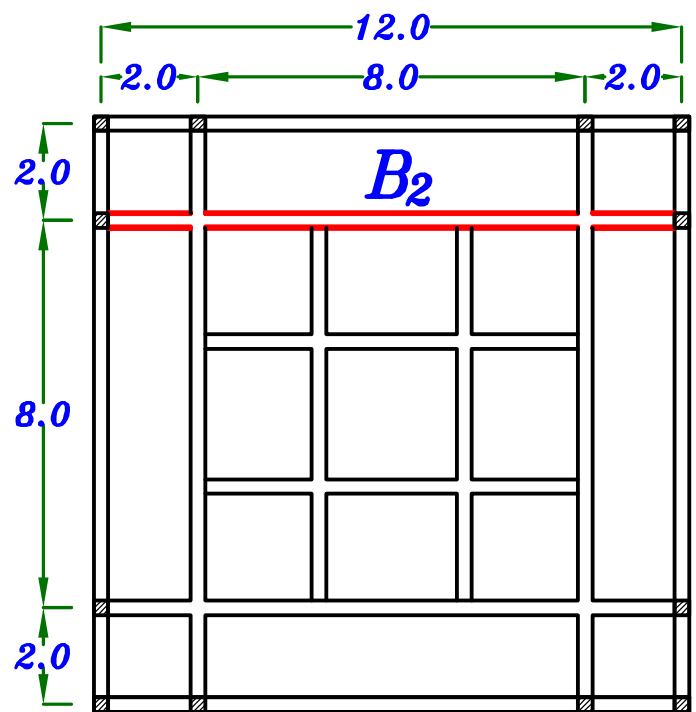
α – Get the Dimensions of the beam. (b, t)

Take $b = 0.25 \text{ m}$

$$t = \frac{L_s}{16} = \frac{12.0}{16} = 0.75 \text{ m}$$

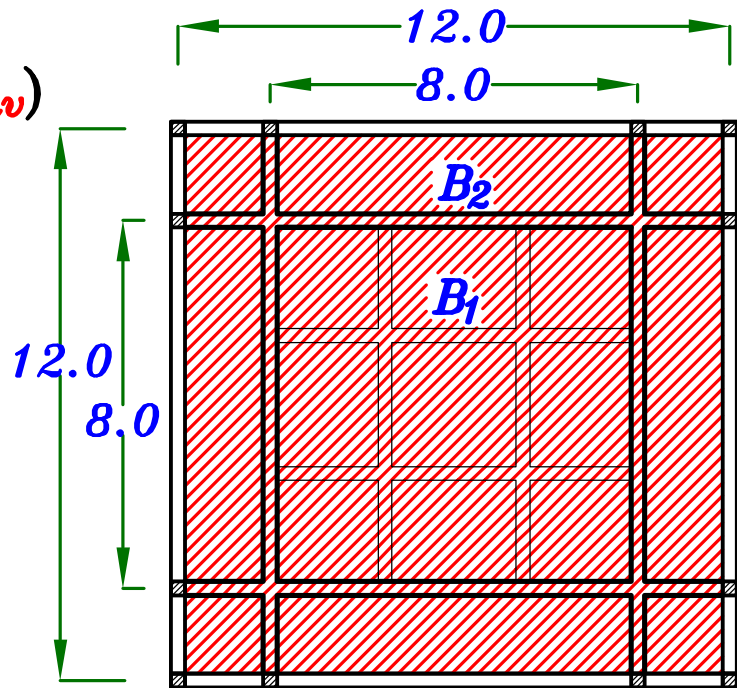
$$b = 0.25 \text{ m}$$

$$t = 0.75 \text{ m}$$



– Get the Loads on the Slab. (w_{av})

$$w_{av.} = \frac{\sum \text{Weight}}{\text{Area}}$$



$$w_{av.} = \frac{\text{Weight of slabs} + \text{Total Weight of Panelled Beams } B_1, B_2}{L * L_s}$$

$$w_{av.} = \frac{w_s * (L * L_s) + 1.4 * b * (t - t_s) [\text{مجموع أطوال الكمرات } B_1] * \delta_c + 1.4 * b * (t - t_s) [\text{مجموع أطوال الكمرات } B_2] * \delta_c}{L * L_s}$$

$$w_{av.} = \frac{8.10 (12 * 12) + 1.4 * 0.25 (0.5 - 0.08) [2 * 8 + 2 * 8] * 25 + 1.4 * 0.25 (0.75 - 0.08) [2 * 12 + 2 * 12] * 25}{12.0 * 12.0}$$

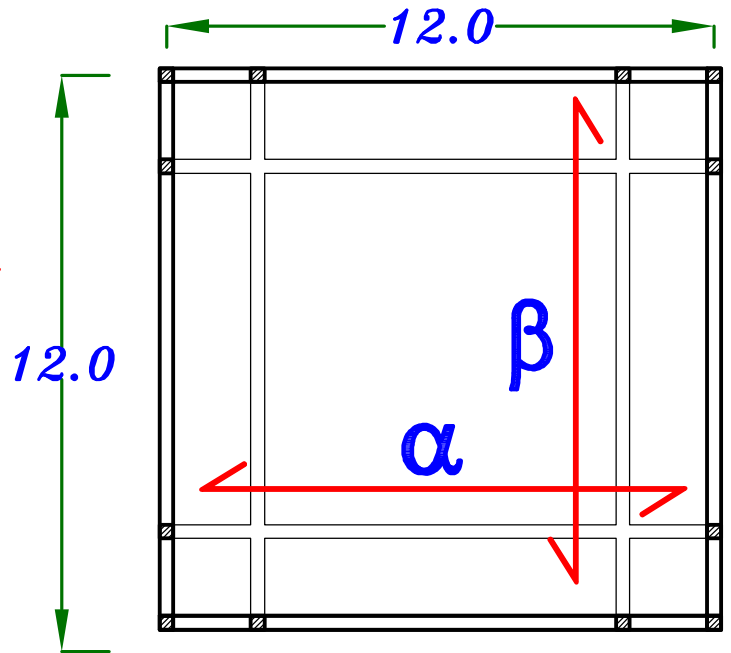
$$= 10.87 \text{ kN/m}^2$$

C – Calculate α , β By using Grashoff.

$$r = \frac{m L}{m_s L_s} = \frac{(1.0) 12.0}{(1.0) 12.0} = 1.0$$

$$\alpha = \frac{r^4}{1+r^4} = \frac{(1.0)^4}{1+(1.0)^4} = 0.5$$

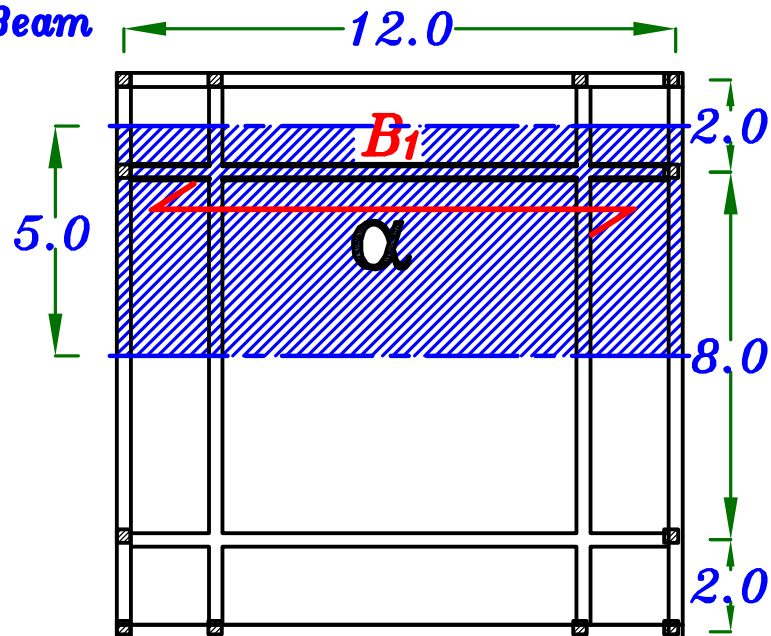
$$\beta = \frac{1}{1+r^4} = \frac{1}{1+(1.0)^4} = 0.5$$



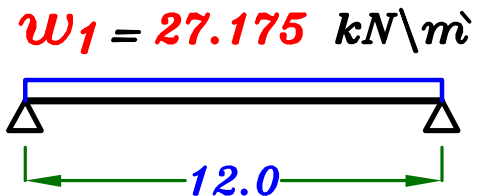
d– Get the Loads on the Panelled Beam & Calculate the B.M.

$$a = 5.0 \text{ m}$$

$$\begin{aligned} w_1 &= w_{av.} * a * \alpha \\ &= 10.87 * 5.0 * 0.50 \\ &= 27.175 \text{ kN/m} \end{aligned}$$



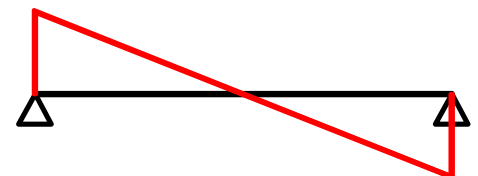
$$M = 27.175 * \frac{12.0^2}{8} = 489.15 \text{ kN.m}$$



B.M.D.



S.F.D.



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

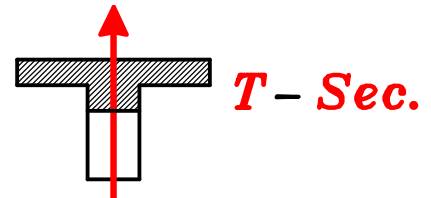
$$X = 2.0 \text{ m} , \quad \frac{L}{2} = 6.0 \text{ m} \quad \theta_{B_2} = \frac{2.0}{6.0} * 90^\circ = 30^\circ$$

$$M_2 = 489.15 * \frac{\sin 30^\circ}{\sin 90^\circ} = 244.57 \text{ kN.m}$$

F – Design the Panelled Beam. B_2

\therefore Cover = 70 mm Symmetric

$$t = 750 \text{ mm} \quad d = 750 - 70 = 680 \text{ mm}$$



$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 5.0 \text{ m} = 5000 \text{ mm} \\ 16 t_s + b = 16 * 80 + 250 = 1530 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{12000}{5} + 250 = 2650 \text{ mm} \end{array} \right\} \quad B = 1530 \text{ mm}$$

$$680 = C_1 \sqrt{\frac{244.57 * 10^6}{25 * 1530}} \rightarrow C_1 = 8.50 \rightarrow J = 0.826$$

$$A_s = \frac{244.57 * 10^6}{0.826 * 360 * 680} = 1209.5 \text{ mm}^2$$

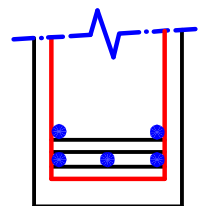
Check $A_{s_{min.}}$ $A_{s_{req.}} = 1209.5 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 680 = 531.25 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1209.5 \text{ mm}^2 \quad 5 \phi 18$$

$$\text{Stirrup Hangers} = (0.1 \rightarrow 0.2) A_s = (120 \rightarrow 240 \text{ mm}^2)$$

$$3 \phi 10$$

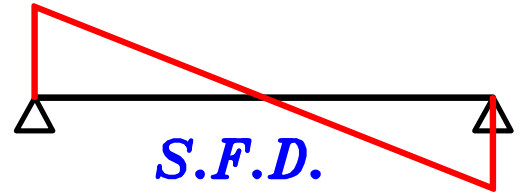


Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

163.05 kN



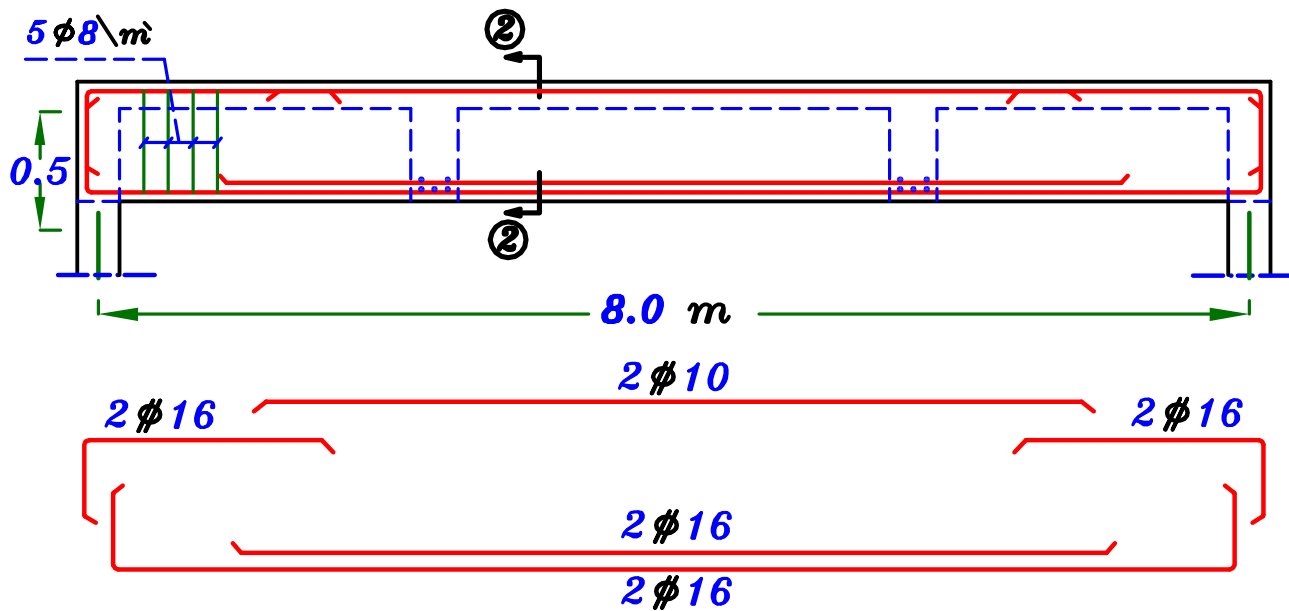
$$q_s = \frac{Q_{max}}{b d} = \frac{163.05 * 10^3}{250 * 680} = 0.96 \text{ N/mm}^2 \quad \therefore q_s < q_{cu}$$

\therefore Use min. Shear RFT.

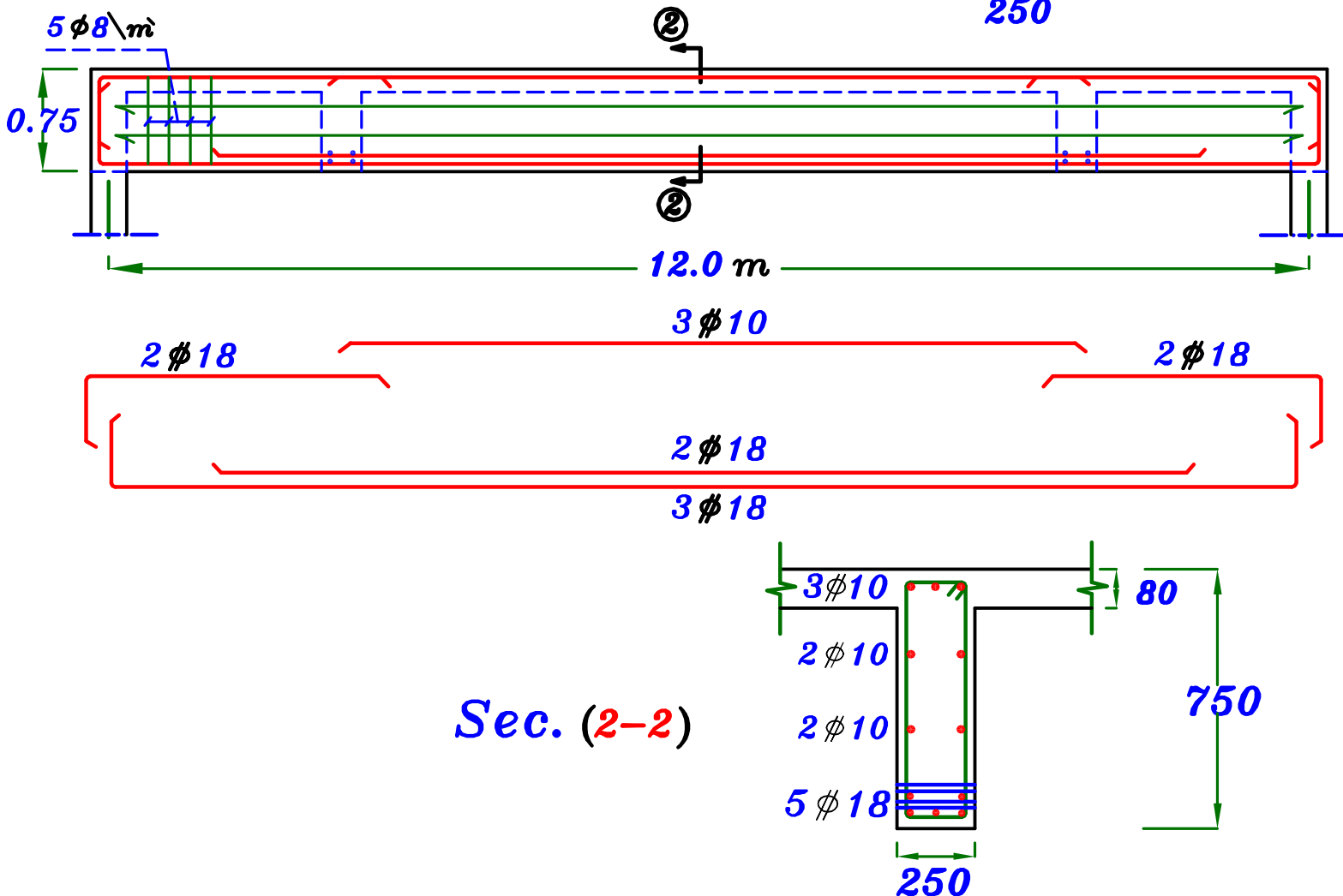
5 ϕ 8/m

g - Draw Details of RFT. For the Beams.

B₁



B₂



Example.

Data to be used in all the exam.

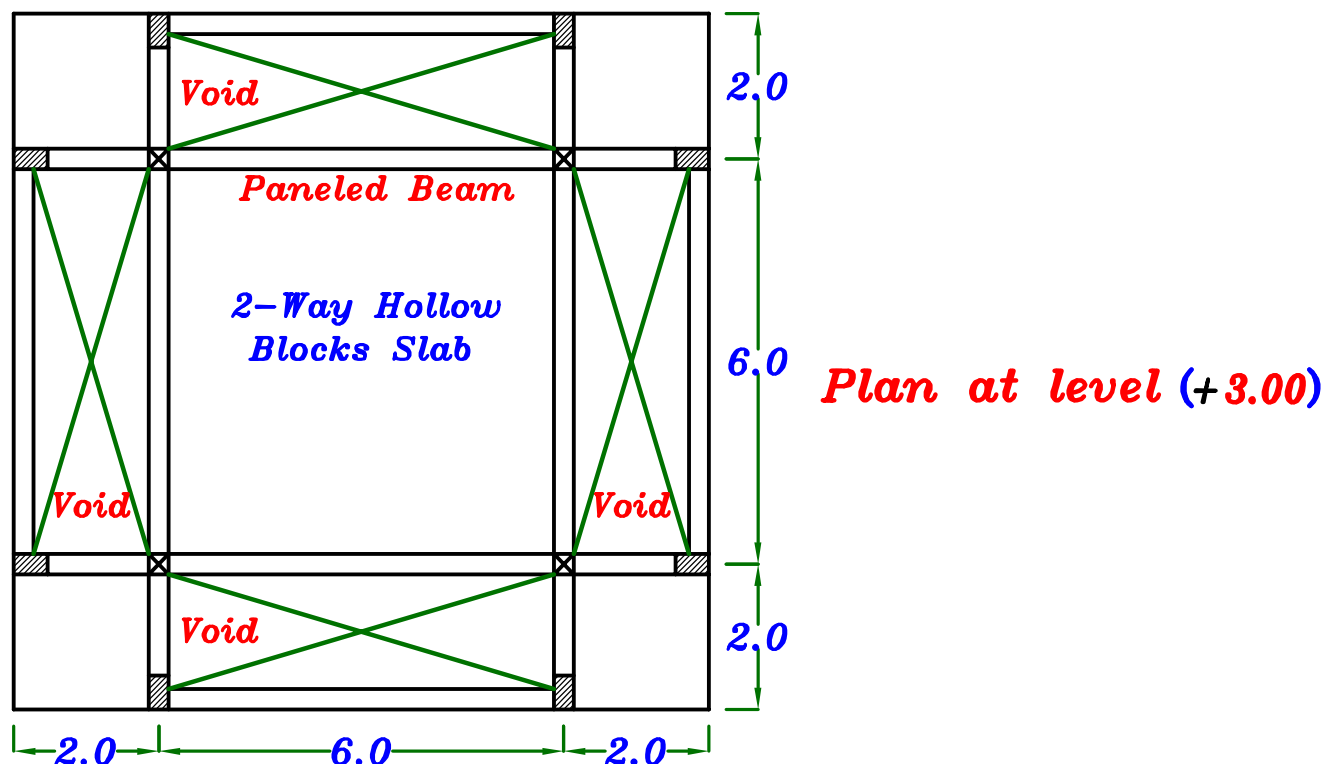
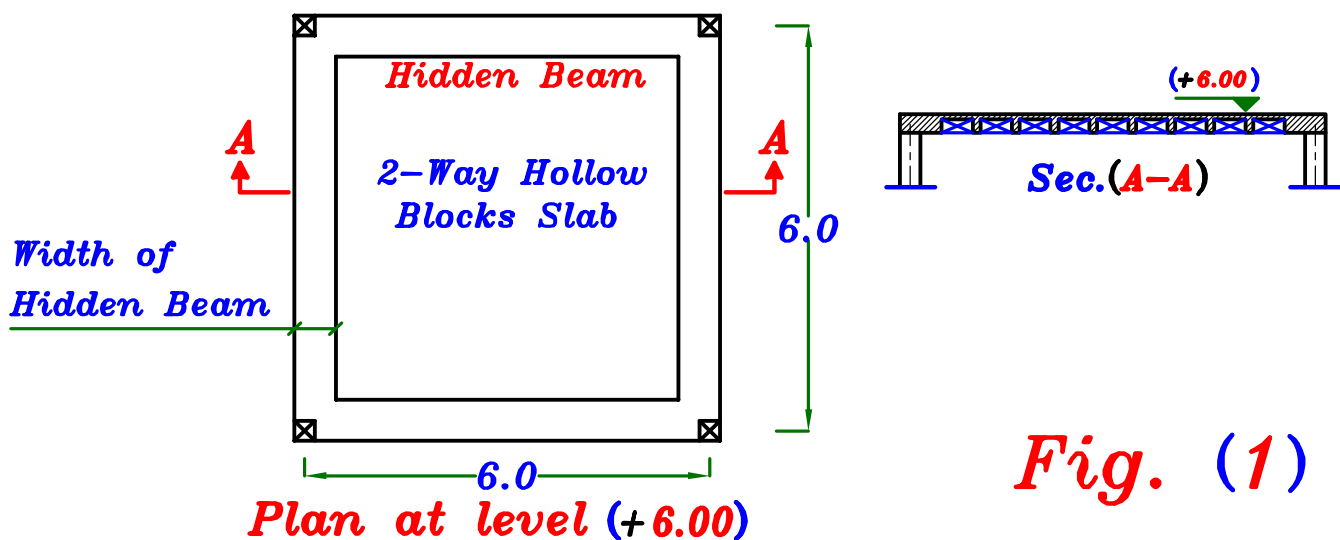
$F_{cu} = 25 \text{ MPa}$, $F_y = 420 \text{ MPa}$, $F.C. = 3.0 \text{ KPa}$, $L.L. = 1.0 \text{ KPa}$

Block ($200 * 400 * 200$)

Weight of Block. = 170 N

For the given reinforced concrete hall shown in Fig.(1) It is required to :

- 1- Design all slabs at level (+3.00) and (+6.00).
- 2- Draw Details of reinforcement in quarter plan (scale 1:50) and cross section (scale 1:25)
- 3- Design the panelled beams at level(+3.00).
- 4- Draw Details of reinforcement of one of the panelled beams in elevation(scale 1:50) and cross section (scale 1:25).



1- Design all slabs at level (+3.00) and (+6.00).

1- Solid Slabs. $t_s = \frac{2000}{10} = 200 \text{ mm}$ $t_s = 200 \text{ mm}$

$$w_s = 1.4(0.20 * 25 + 3.0) + 1.6(1.0) = 12.80 \text{ kN/m}^2$$

2- Two way Hollow Blocks.

$$b = 0.1 \text{ m} \quad e = 0.4 \text{ m}$$

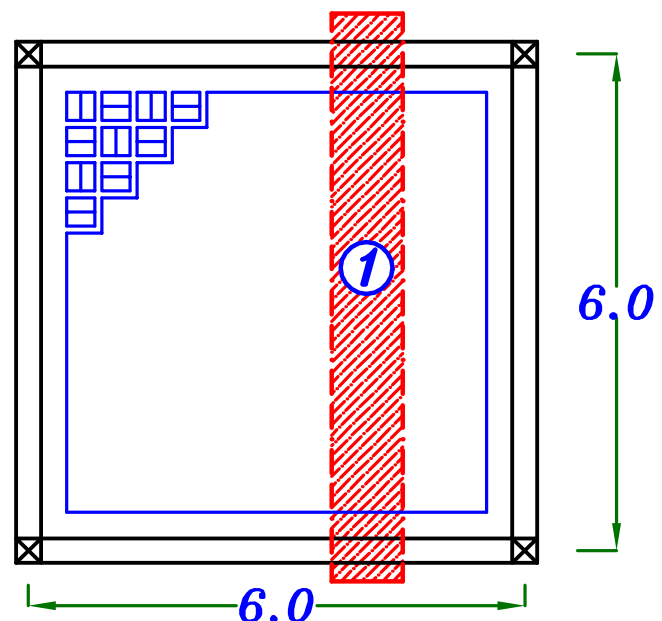
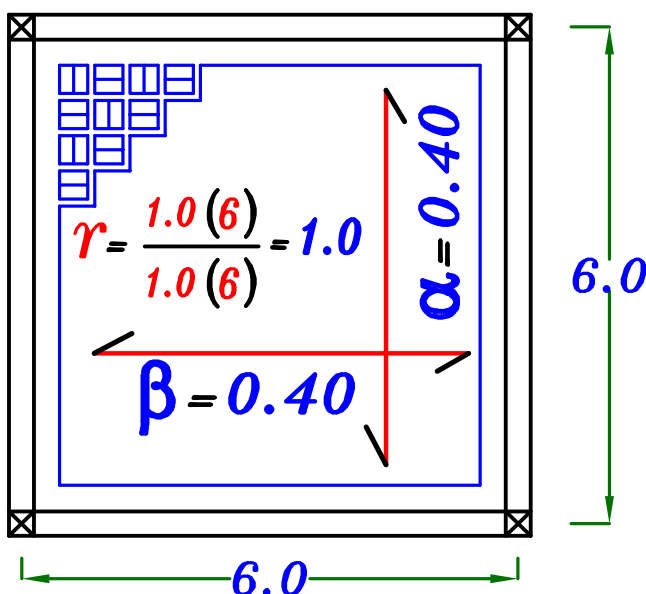
$$S = e + b = 0.4 + 0.1 = 0.5 \text{ m}$$

$$w_{ribT} = [1.4(t_s \delta_c + F.C.) + 1.6(L.L.)](S * S) + 1.4 * b * h * (2S - b) * \delta_c + 1.4 * (\text{وزن الكتل}) * \left(\frac{e}{a}\right)$$

$$\therefore w_{ribT} = [1.4(0.05 * 25 + 3.0) + 1.6(1.0)](0.5 * 0.5) + 1.4(0.1 * 0.20 * (2 * 0.5 - 0.1) * 25) + 1.4\left(\frac{170}{1000}\right)\left(\frac{0.4}{0.2}\right) = 2.99 \text{ (kN / (S * 2S))}$$

$$w_{rib} = \frac{w_{ribT}}{S} = \frac{2.99}{0.5} = 5.98 \text{ kN / (S * m)}$$

Two way Hollow Blocks slabs at levels (+3.00) and (+6.00) are the same.



Strip ①

$$M = 10.75 \text{ kN.m/rib}$$

$$d = t - 40 \text{ mm} = 250 - 40 = 210 \text{ mm}$$

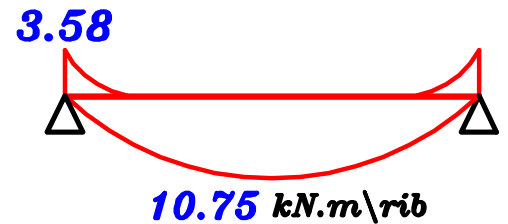
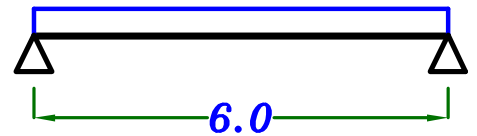
$$\therefore 210 = C_1 \sqrt{\frac{10.75 \cdot 10^6}{25 \cdot 500}}$$

$$\rightarrow C_1 = 7.16 \rightarrow J = 0.826$$

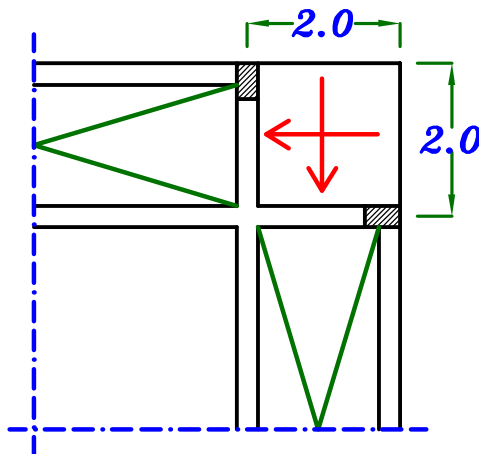
$$A_s = \frac{M}{J F_y d} = \frac{10.75 \cdot 10^6}{0.826 \cdot 420 \cdot 210} = 147.5 \text{ mm}^2/\text{rib}$$

$$\boxed{2\phi 10/\text{rib}}$$

$$\alpha w_{rib} = 0.40 (5.98) = 2.39 \text{ kN/m}$$



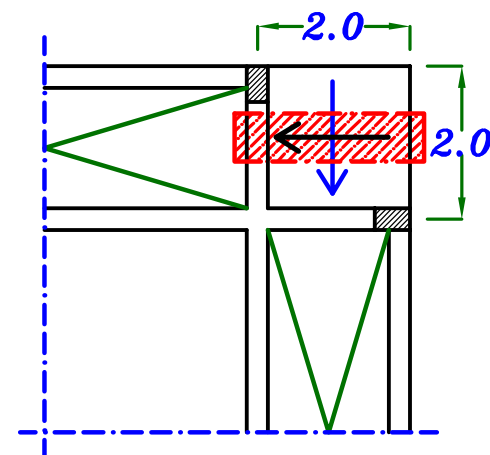
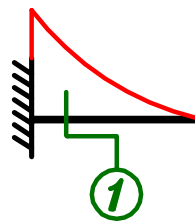
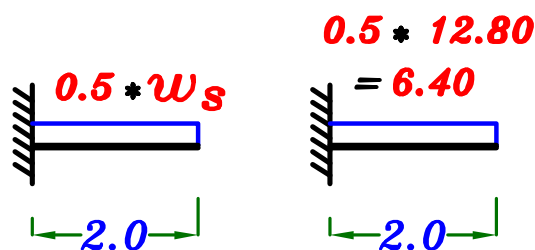
Cantilever Solid Slab.



يتوزع حمل البلاطه على الـ **two cantilevers**
أى يتوزع الحمل فى الاتجاهين كل اتجاه $0.5 w_s$

تعمل **Torsion** على الكمره

$$M_t = 12.80$$



Sec. ① $M_{U.L.} = 12.80 \text{ kN.m/m}$

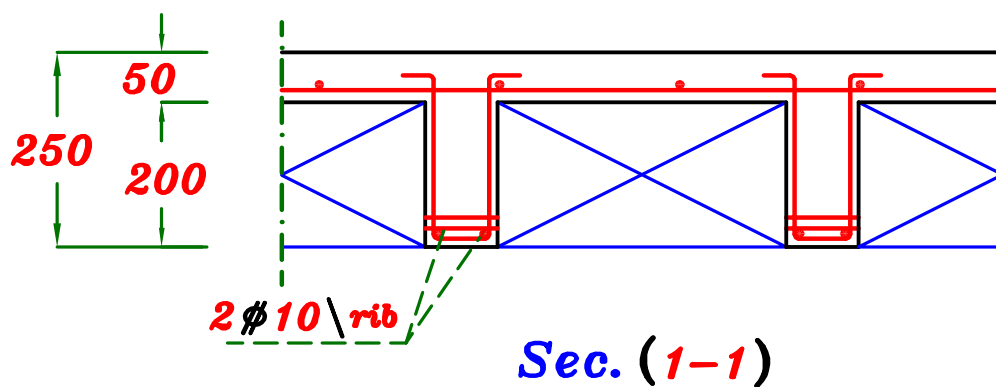
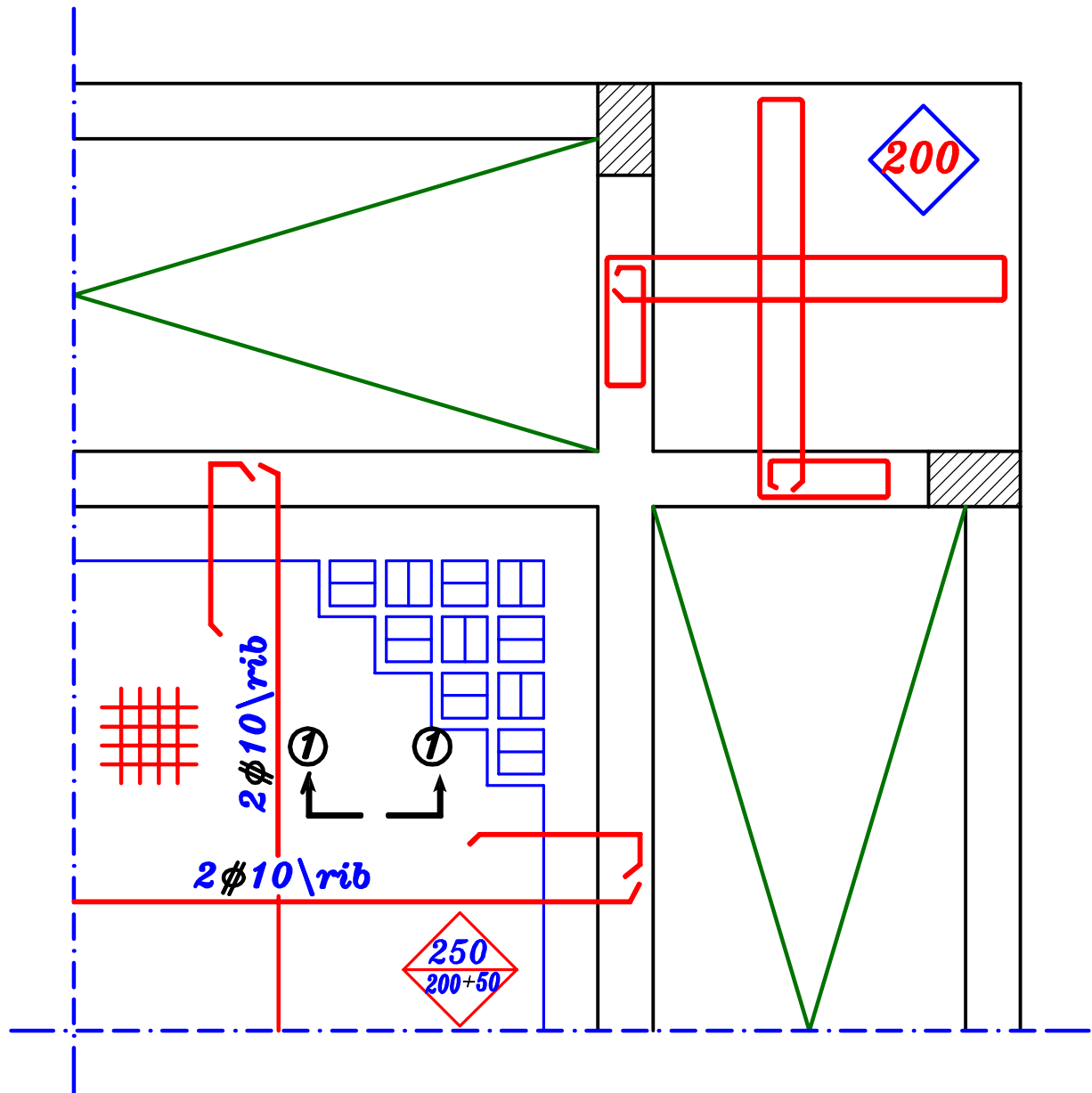
$$t_s = 200 \text{ mm}, d = 200 - 20 = 180 \text{ mm}$$

$$180 = C_1 \sqrt{\frac{12.80 \cdot 10^6}{25 \cdot 1000}} \rightarrow C_1 = 7.95 \rightarrow J = 0.826$$

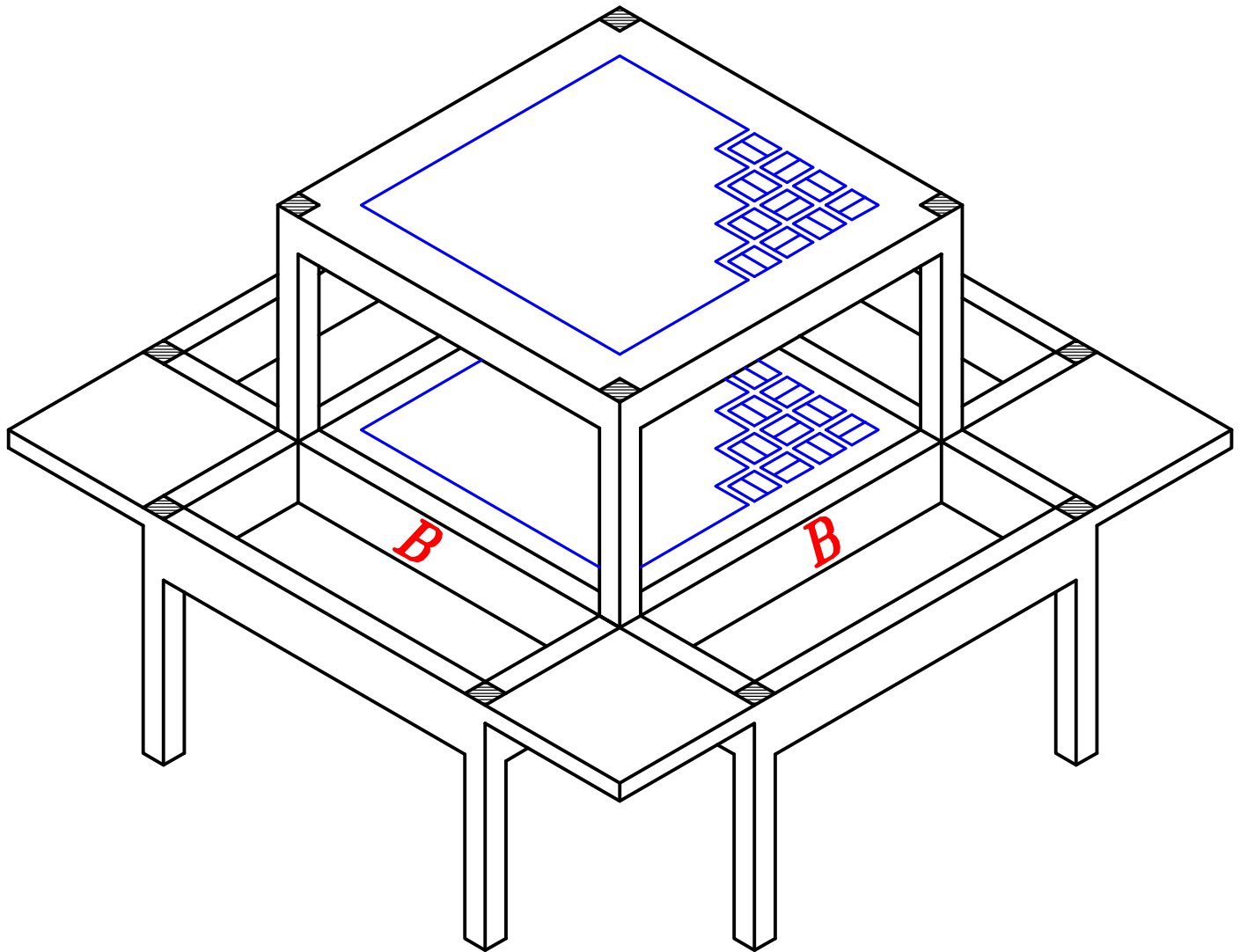
$$A_s = \frac{12.80 \cdot 10^6}{0.826 \cdot 420 \cdot 180} = 204.9 \text{ mm}^2/\text{m}$$

$$\boxed{5\phi 10/\text{m}}$$

**2 – Draw Details of reinforcement in quarter plan (scale 1:50)
and cross section (scale 1:25)**



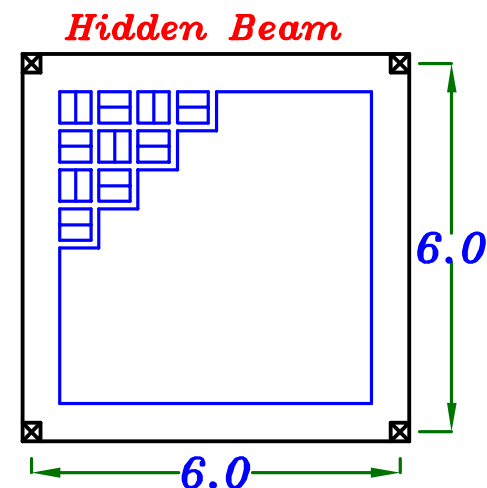
3- Design the panelled beams at level (+3.00).



Get the total weight For the upper plan.

Take $O.W. (Hidden Beam) = 6.0 \text{ kN/m} \quad (U.L.)$

$Post = 0.25 * 0.25 * 3.0 * 25 * 1.4 = 6.5 \text{ kN}$



$Total Weight = \left(\frac{w_{rib}}{S} \right) * H.B. \text{ area} + o.w. * Length + 4 Posts$
(Beam) (Beams)

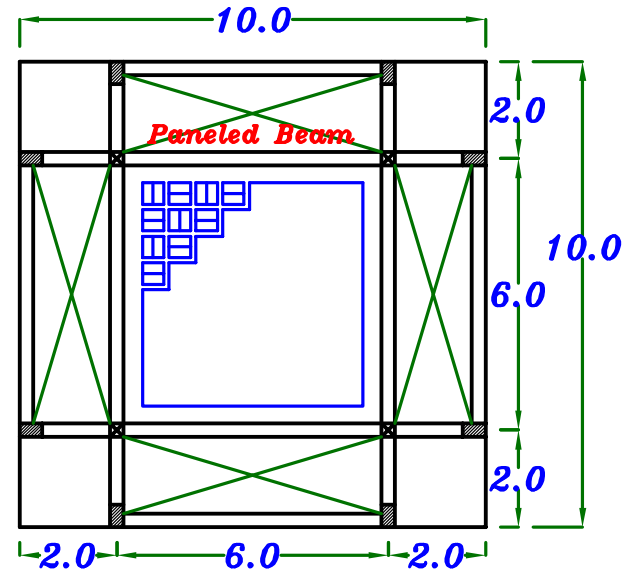
$Total Weight = \left(\frac{5.98}{0.5} \right) (6 * 6) + 6.0 (6 * 4) + 4 * 6.5 = 600.56 \text{ kN}$

$Load From one Post (P) = \frac{600.56}{4} = 150.14 \text{ kN} \quad (U.L.)$

α – Get the Dimensions of the beam. (**b, t**)

Take **$b = 0.25$ m.**

$$t = \frac{10}{16} = 0.65 \text{ m.}$$



b – Get the Loads on the Slab. (**w_{av}**)

$$(w_{av})_{U.L.} = \frac{w_s \cdot \text{area (s.s.)} + \left(\frac{w_{rib}}{S}\right) \cdot \text{area (H.B.)} + \text{Panelled Beams}}{\text{Total area}}$$

$$= \frac{12.80 \cdot 4(2 \cdot 2) + \left(\frac{5.98}{0.5}\right) (6 \cdot 6) + 1.4 [0.25 (0.65 - 0.20) (4 \cdot 10) \cdot 25]}{10 \cdot 10 - 4(2 \cdot 6)}$$

$$= 15.25 \text{ kN/m}^2$$

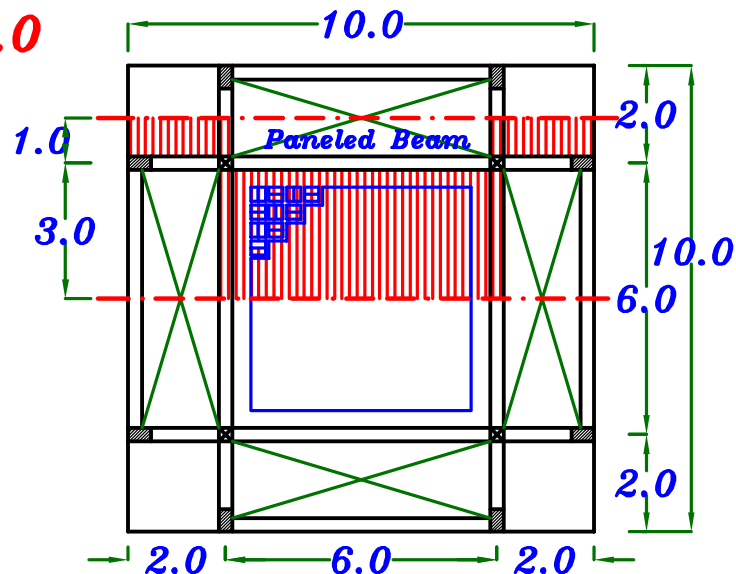
C – Calculate **α, β** By using Grashoff.

$$\gamma = \frac{m L}{m_s L_s} = \frac{(1.0) 10}{(1.0) 10} = 1.0$$

$$\alpha = \beta = 0.50$$

$$\alpha_1 = 1.0 \text{ m}$$

$$\alpha_2 = 3.0 \text{ m}$$



$$\alpha P = \beta P = 0.50 \cdot 150.14 = 75.07 \text{ kN}$$

$$w_1 = w_{av.} * \alpha_1 * \alpha$$

$$= 15.25 * 1.0 * 0.50 = 7.625 \text{ kN/m}$$

$$w_2 = w_{av.} * \alpha_2 * \alpha$$

$$= 15.25 * 3.0 * 0.50 = 22.87 \text{ kN/m}$$

$$\theta_{B_2} = \frac{2.0}{5.0} * 90^\circ = 36^\circ$$

$$M_1 = 405.6 * \frac{\sin 36^\circ}{\sin 90^\circ} = 238.4 \text{ kN.m}$$

$$d = 650 - 50 = 600 \text{ mm} \quad b = 250 \text{ mm}$$

Sec. ① $M_{U.L.} = 238.4 \text{ kN.m}$ *R-Sec.*

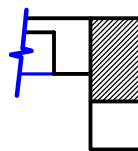
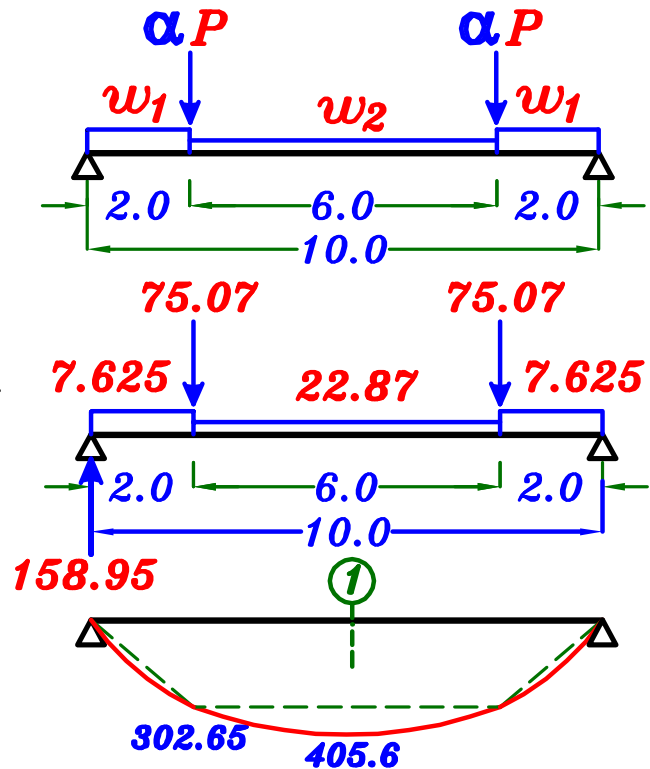
$$600 = C_1 \sqrt{\frac{238.4 * 10^6}{25 * 250}} \rightarrow C_1 = 3.07 \rightarrow J = 0.75$$

$$A_s = \frac{238.4 * 10^6}{0.75 * 420 * 600} = 1261.37 \text{ mm}^2$$

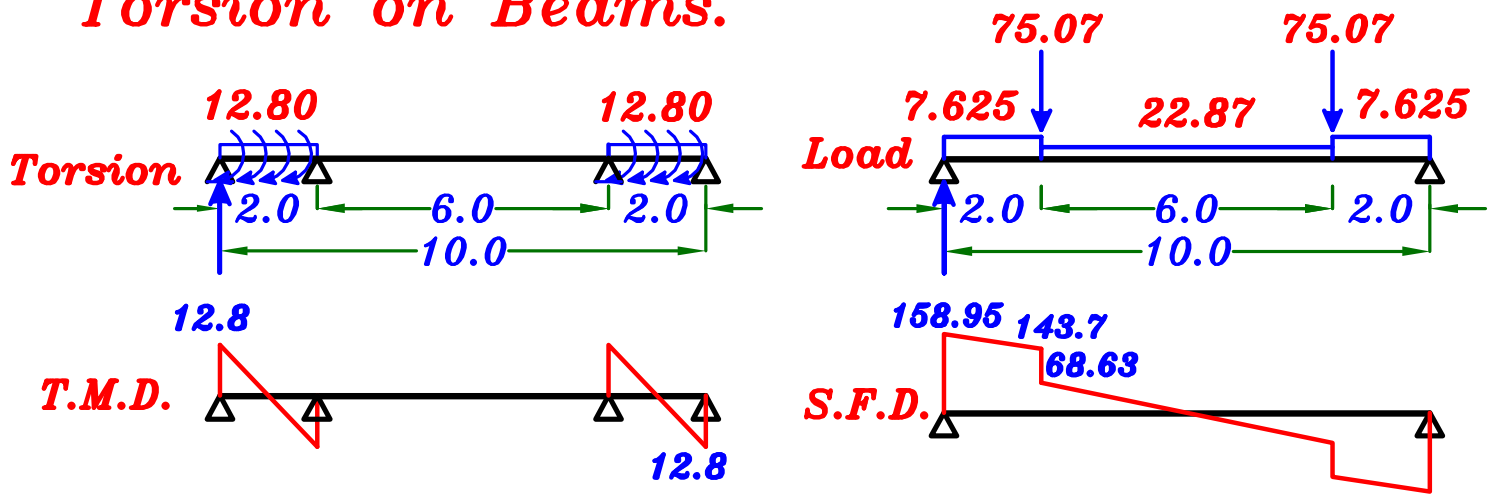
Check $A_{s_{min.}}$ $A_{s_{req.}} = 1261.37 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{420} \right) 250 * 600 = 401.8 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1261.37 \text{ mm}^2$$



Torsion on Beams.



$$q_u = \frac{Q}{bd} = \frac{158.95 * 10^3}{250 * 600} = 1.06 \text{ N/mm}^2$$

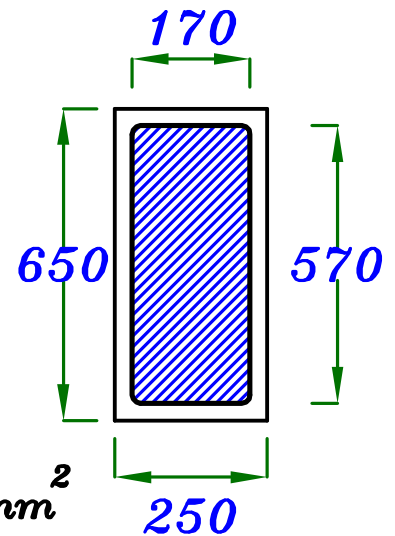
$$A_{oh} = 170 * 570 = 96900 \text{ mm}^2$$

$$A_o = 0.85 * A_{oh} = 0.85 * 96900 = 82365 \text{ mm}^2$$

$$P_h = 2 * 170 + 2 * 570 = 1480 \text{ mm}$$

$$t_e = \frac{A_{oh}}{P_h} = \frac{96900}{1480} = 65.47 \text{ mm}$$

$$q_{tu} = \frac{M_{tu}}{2 A_o t_e} = \frac{25.6 * 10^6}{2 * 82365 * 65.47} = 2.37 \text{ N/mm}^2$$



$$q_{cu} = (0.24) \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$q_{tmin} = (0.06) \sqrt{\frac{25}{1.5}} = 0.245 \text{ N/mm}^2$$

$$q_{u_{max}} = (0.7) \sqrt{\frac{25}{1.5}} = 2.85 \text{ N/mm}^2$$

$$\sqrt{q_u^2 + q_{tu}^2} = \sqrt{1.06^2 + 2.37^2} = 2.60 \text{ N/mm}^2 < q_{u_{max}} \therefore \text{o.k.}$$

$$q_u > q_{cu}, q_{tu} > q_{tmin} \therefore \text{Use RFT. For Shear + Torsion}$$

Check IF stirrups $5 \phi 10 \setminus m 2 b$
are enough to resist **Shear + Torsion**

@ Torsion.

$$x_1 = 220 \text{ mm} , y_1 = 620 \text{ mm} , A_{oh} = 220 * 620 = 136400 \text{ mm}^2$$

$$A_{str} = \frac{M_{tu} S_t}{(1.7) A_{oh} \left(\frac{F_y}{\delta_s} \right)} \therefore A_{str} = \frac{(25.6 * 10^6) S_t}{(1.7)(96900)(420/1.15)}$$

$$\therefore A_{str} = 0.425 S_t$$

⑥ Shear.

$$q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y / \delta_s)}{b S_s} \therefore 1.06 - \frac{0.98}{2} = \frac{n A_s (420/1.15)}{(250) S_s}$$

$$\text{By using } 5 \phi 10 \setminus m 2 b \therefore A_s = 0.397 \frac{S_s}{n}$$

$$n = 2 , S_t = S_s = \frac{1000}{5.0} = 200 \text{ mm}$$

$$\therefore A_{str} = 0.425 S_t = 0.425 * 200 = 85.0 \text{ mm}^2$$

$$A_s = 0.397 \frac{S_s}{n} = 0.397 * \frac{200}{2.0} = 39.7 \text{ mm}^2$$

$$A_{s_{outer}} = A_{str} + A_s = 85.0 + 39.7 = 124.7 > \phi 10 = 78.5 \text{ mm}^2$$

Take RFT. of the slab. $8 \phi 10 \setminus m$

$$n = 2 , S_t = S_s = \frac{1000}{8.0} = 125 \text{ mm}$$

$$\therefore A_{str} = 0.425 S_t = 0.425 * 125 = 53.1 \text{ mm}^2$$

$$A_s = 0.397 \frac{S_s}{n} = 0.397 * \frac{125}{2.0} = 24.8 \text{ mm}^2$$

$$A_{s_{outer}} = A_{str} + A_s = 53.1 + 24.8 = 77.9 < \phi 10 = 78.5 \text{ mm}^2$$

$\therefore \text{o.k.}$

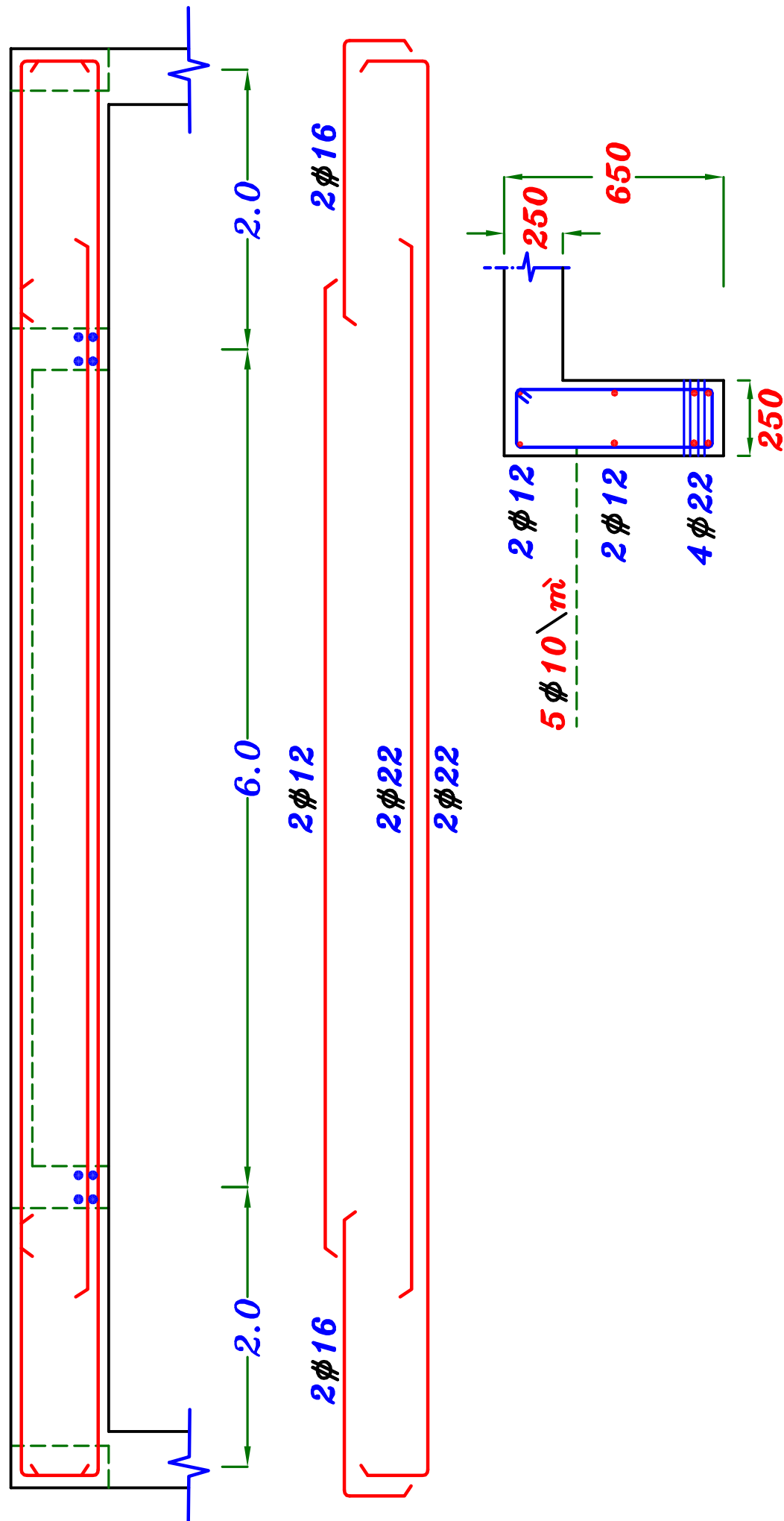
Longitudinal Bars.

$$A_{sl} = \frac{A_{str} * P_h}{S_t} \left(\frac{F_{y_{str.}}}{F_{y_{L.b.}}} \right) = \frac{(78.5 * 1480)}{125} \left(\frac{420}{420} \right) \therefore A_{sl} = 929.4 \text{ mm}^2$$

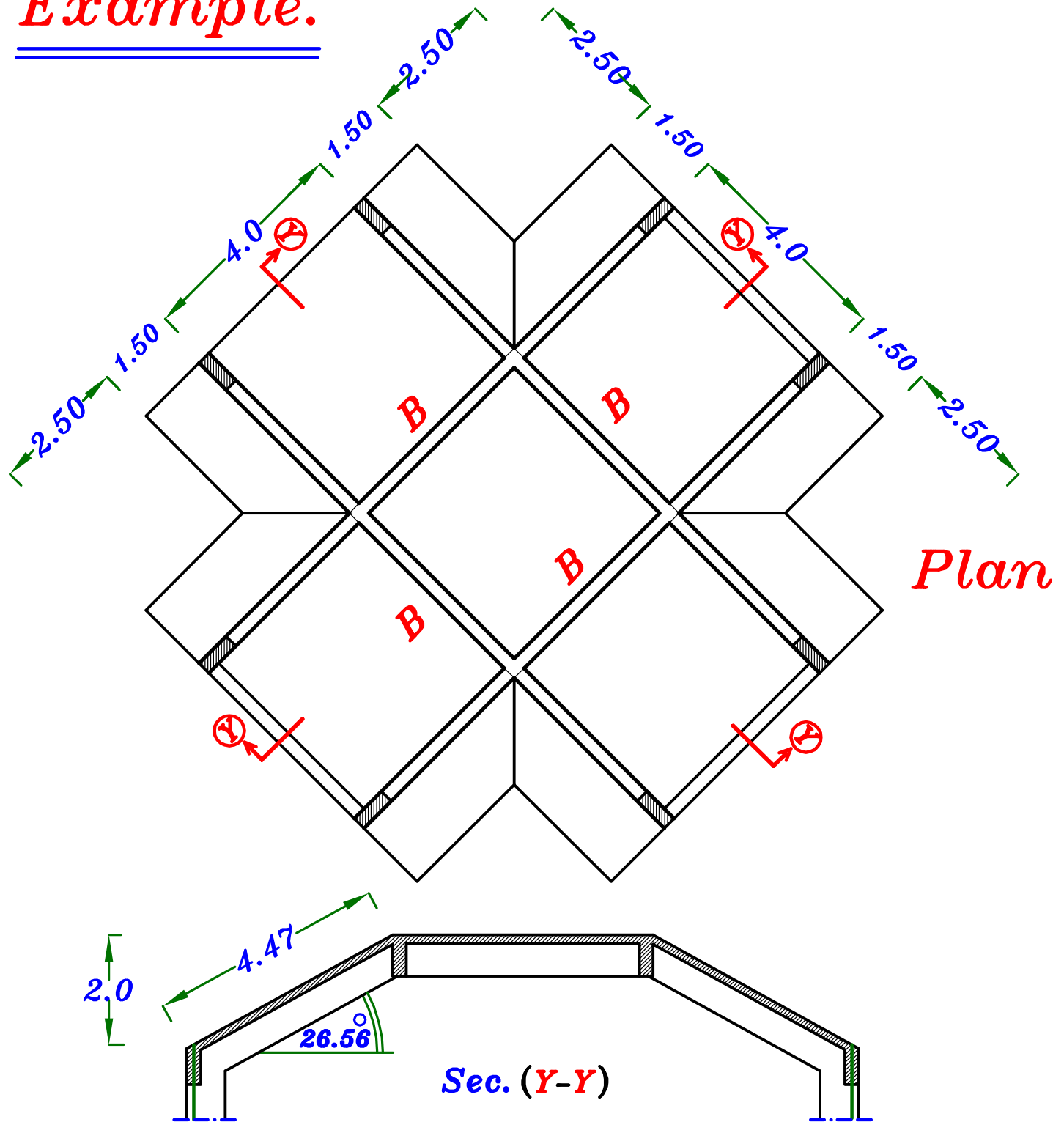
$$A_s = A_{S_{beam}} + \frac{A_{sl}}{4} = 1261.37 + \frac{929.4}{4} = 1493.72 \text{ mm}^2$$

4 ϕ 22

4 – Draw Details of reinforcement of one of the paneled beams.



Example.



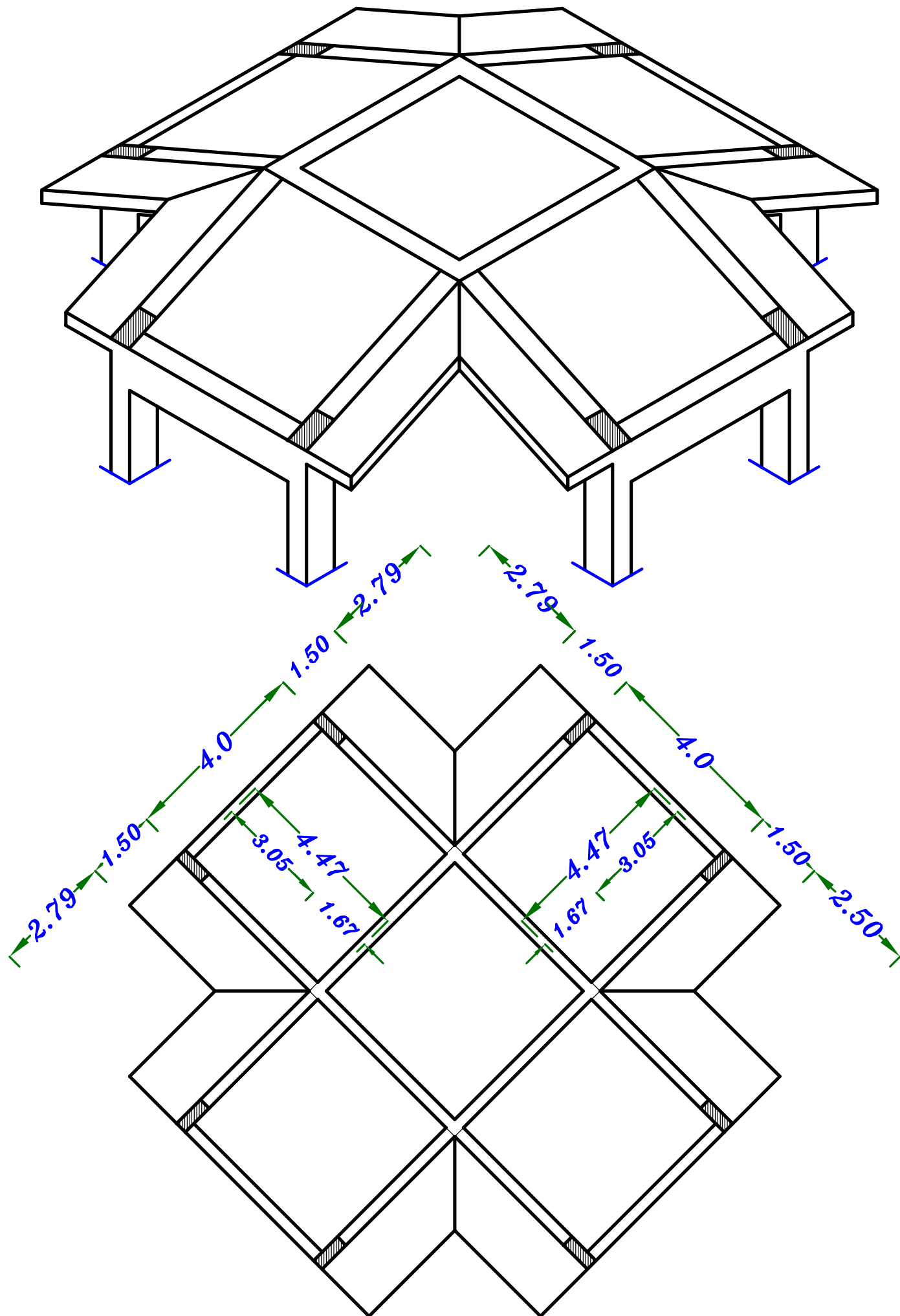
Data.

$$F_{cu} = 25 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

$$F.C. + L.L. = 2.5 \text{ kN/m}^2 \text{ Horizontal Projection}$$

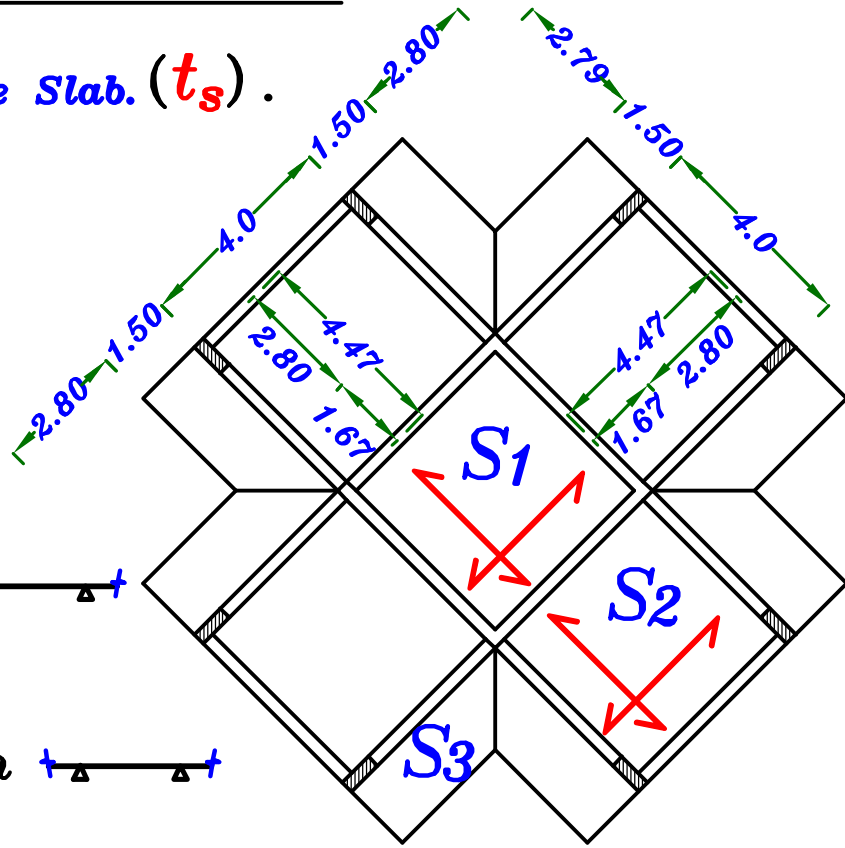
Req.

- ① Design all Slabs & Draw RFT. in plan.
- ② Design the panelled Beams & Draw RFT. in elevation.



① Design the Slabs as Solid Slabs.

a- Choose the Thickness of the Slab. (t_s).



S1 two way $L_s = 4.0$ m

$$t_s = \frac{4000}{45} = 88.9 \text{ mm}$$

S2 two way $L_s = 4.0$ m

$$t_s = \frac{4000}{45} = 88.9 \text{ mm}$$

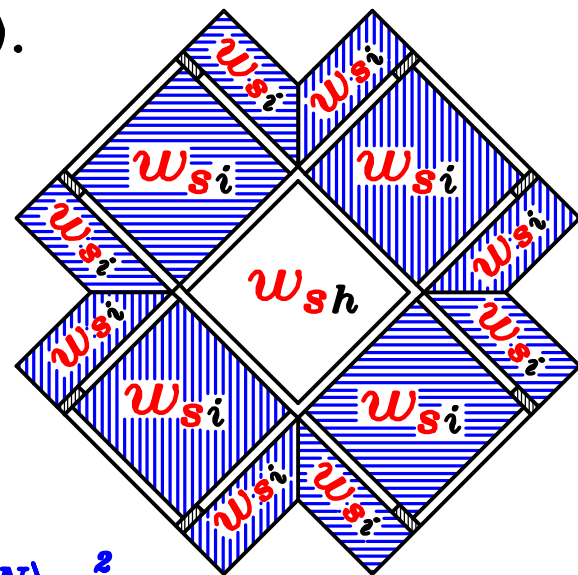
S3 Cantilever $L_c = 1.5$ m

$$t_s = \frac{1500}{10} = 150 \text{ mm}$$

Take (t_s) the bigger value

$$t_s = 150 \text{ mm}$$

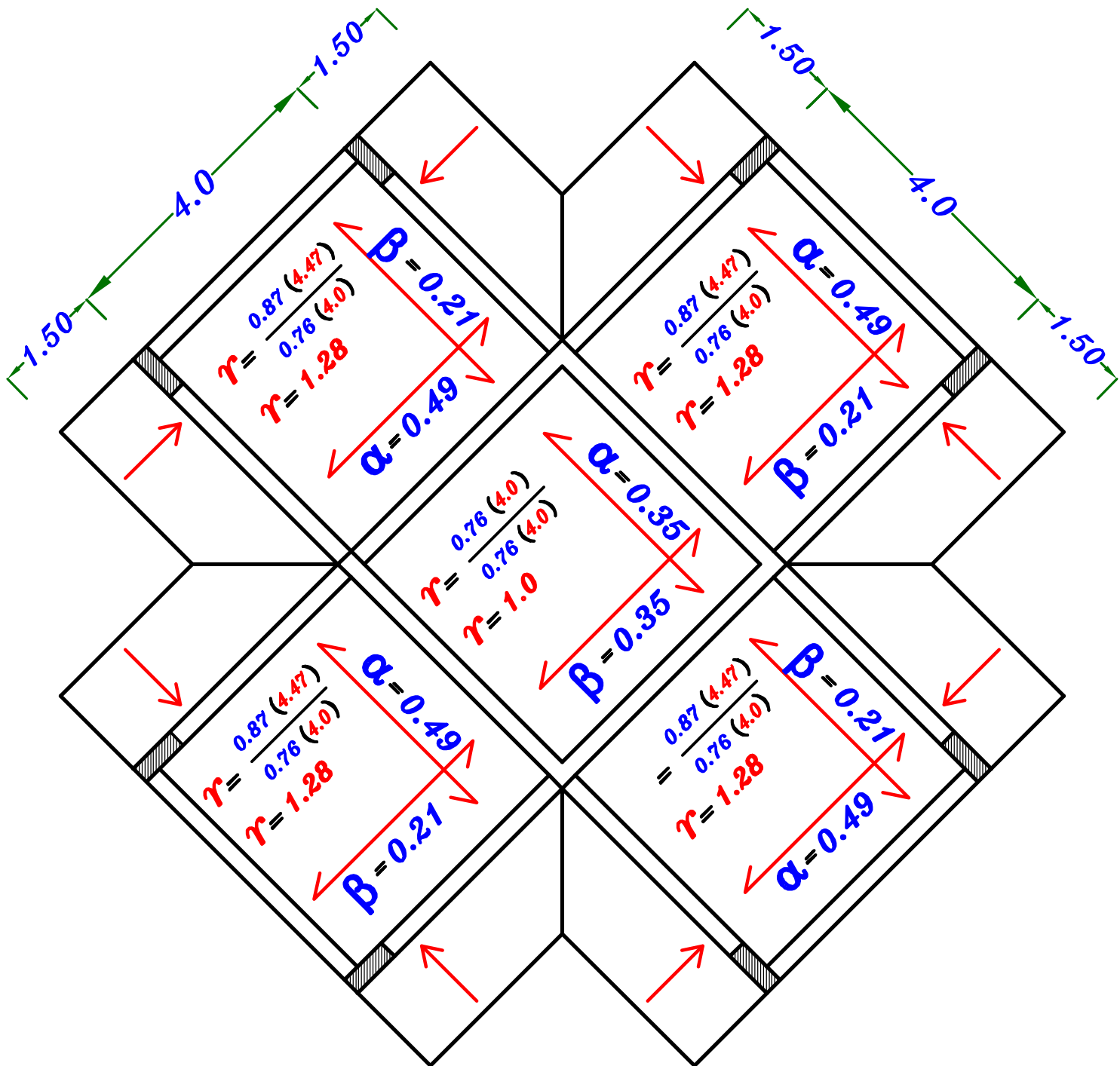
b- Get the Loads on the Slab (w_s).



$$w_{sh} = 1.5 (0.15 * 25 + 2.5) = 9.37 \text{ kN/m}^2$$

$$w_{si} = 1.5 (0.15 * 25 + 2.5 * \cos 26.56^\circ) = 8.98 \text{ kN/m}^2$$

c – Get the Load Factors α , β



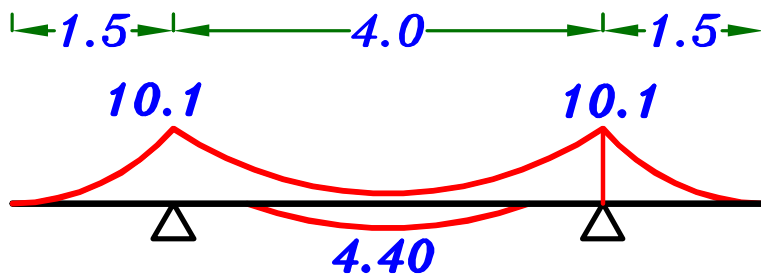
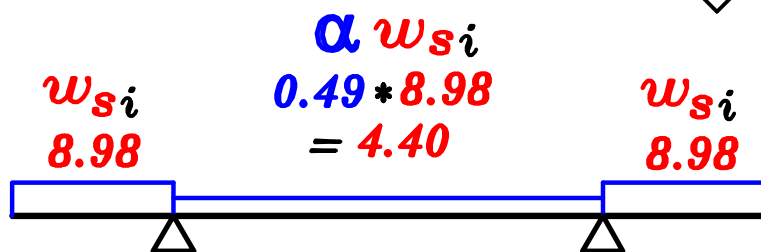
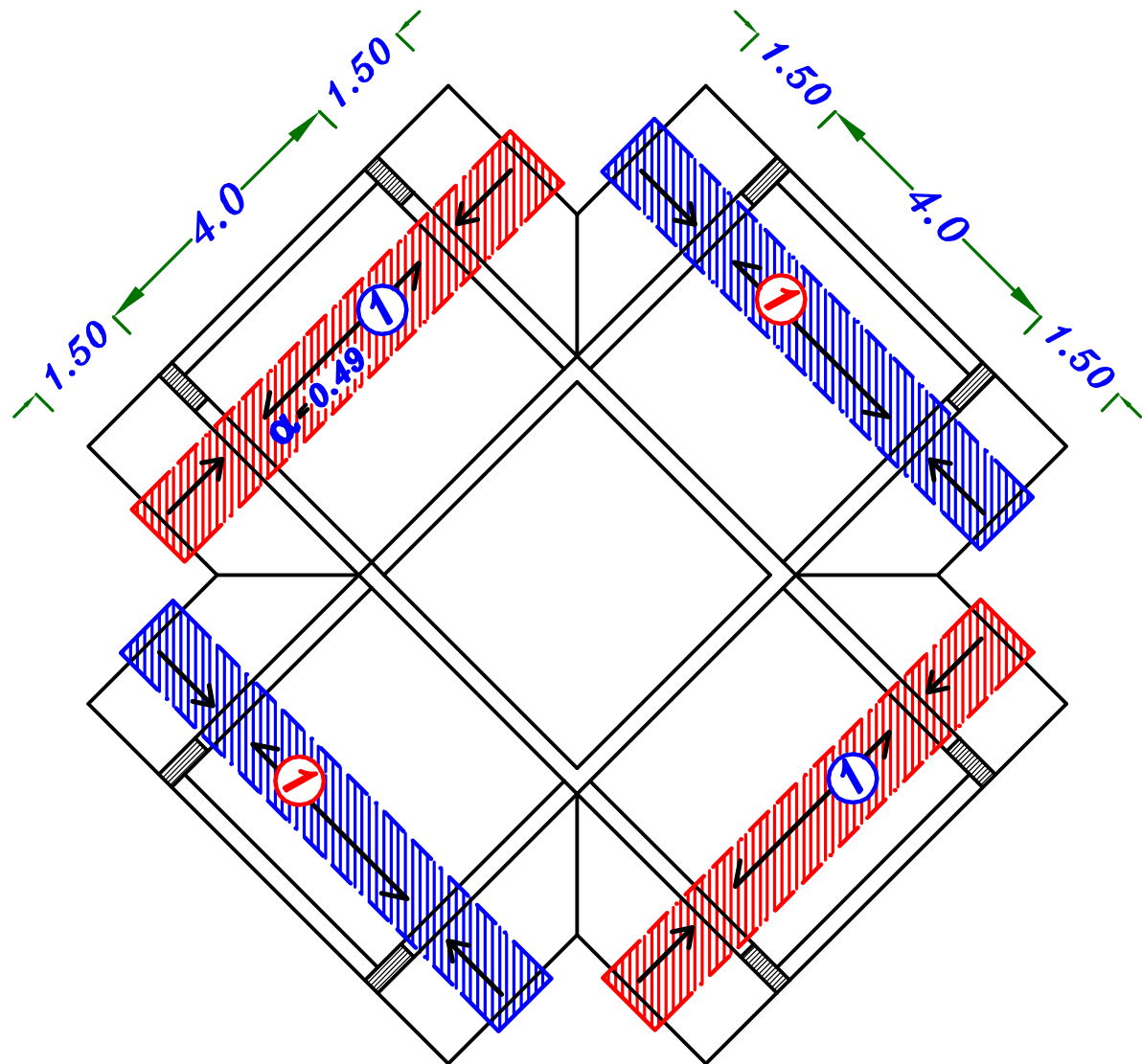
$$\alpha = 0.5 r - 0.15$$

$$\beta = \frac{0.35}{r^2}$$

d- Take a strips in the slab (at the Load direction)

And then Get (B.M.) on the Slab & Design the slab.

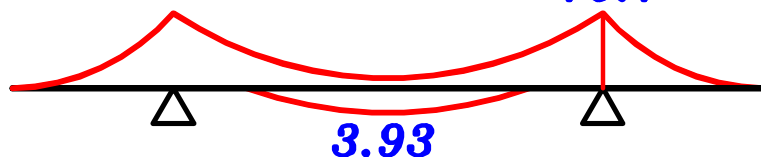
Strip ①



شريحة أفقية في بلاطة مائلة

$$10.1 \cos 26.56^\circ = 9.03$$

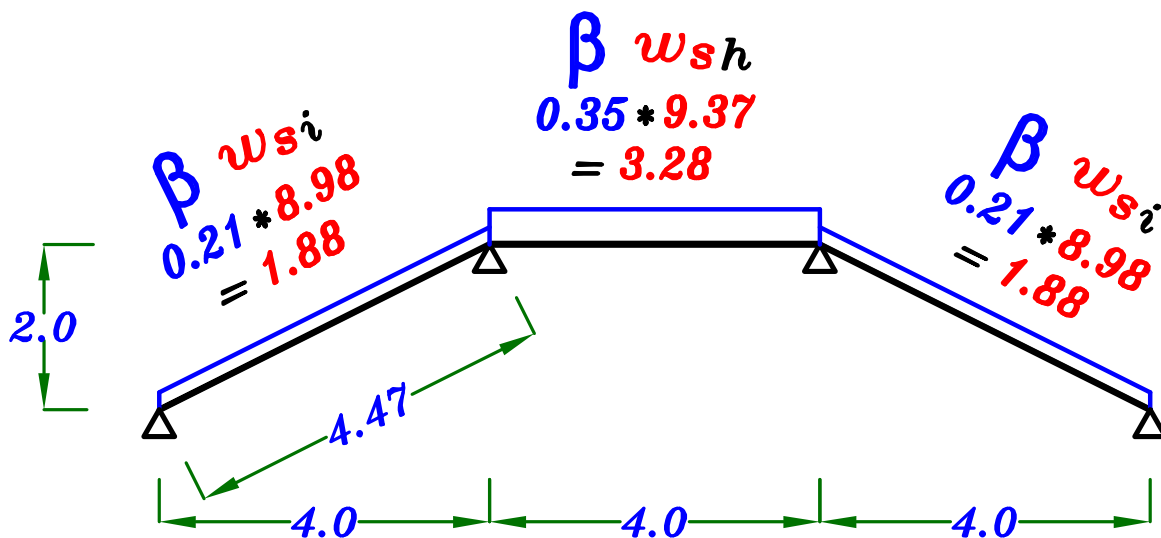
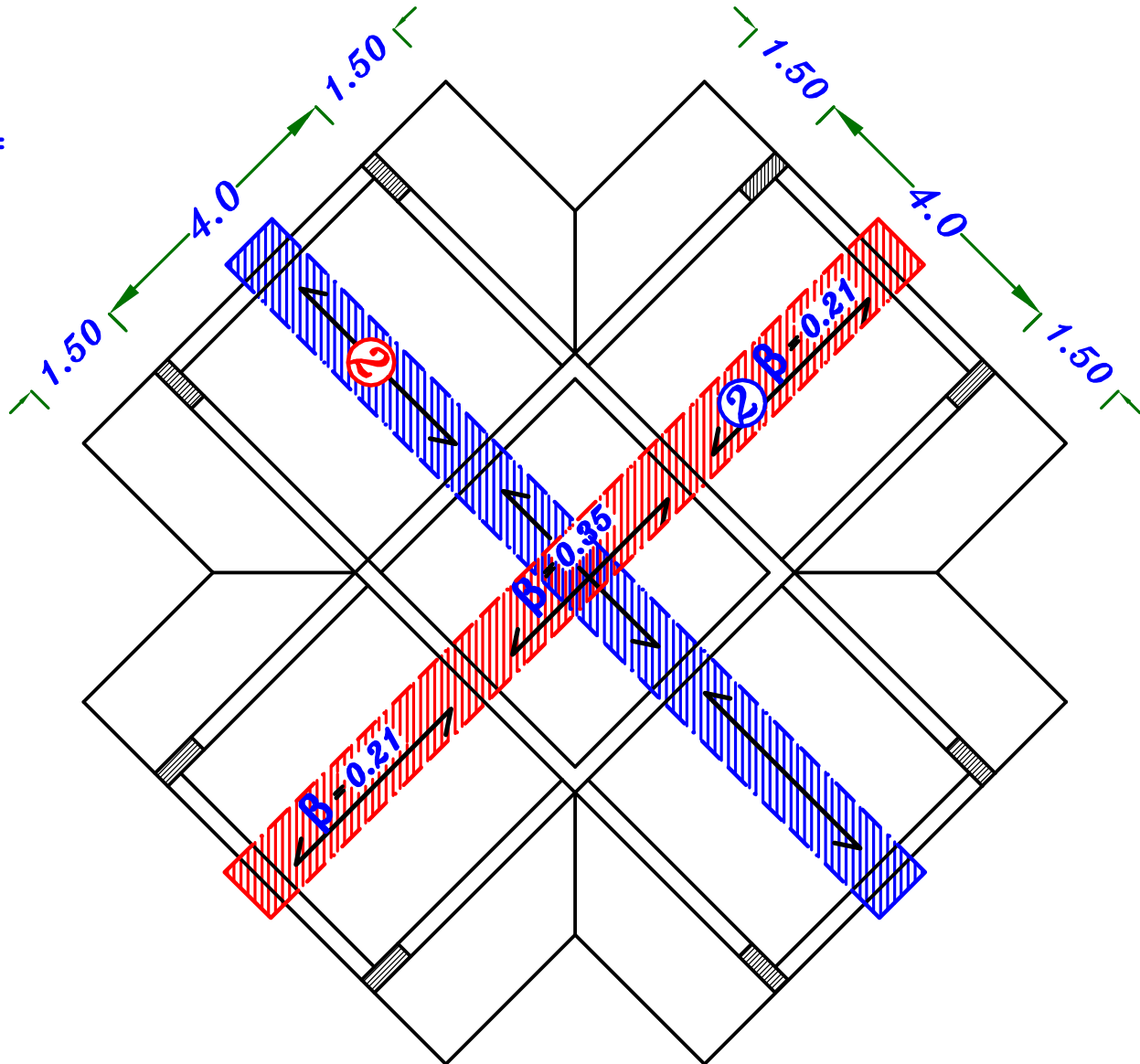
$$10.1 \cos 26.56^\circ = 9.03$$

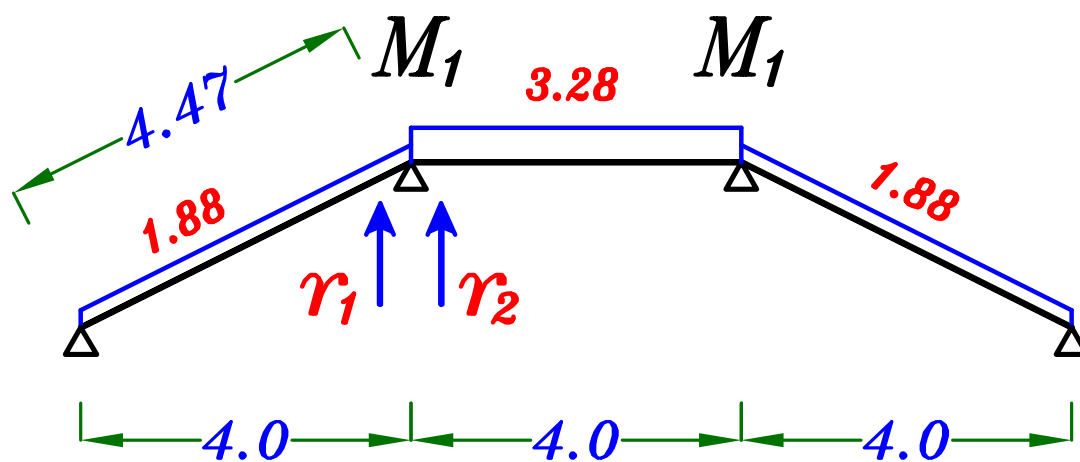


d - Take a strips in the slab (at the Load direction)

And then Get (B.M.) on the Slab & Design the slab.

Strip ①



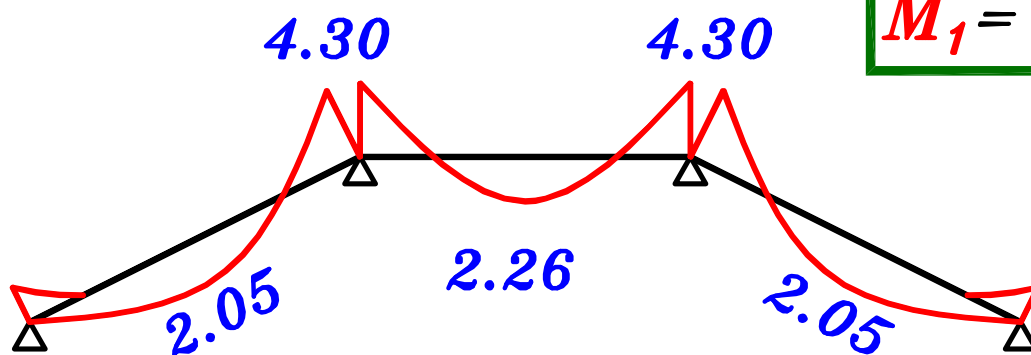


$$r_1 = \frac{wLL^2}{24} = \frac{1.88 \cdot 4.0 \cdot 4.47^2}{24} = 6.26 \quad , \quad r_2 = \frac{wL^3}{24} = \frac{3.28 \cdot 4.0^3}{24} = 8.74$$

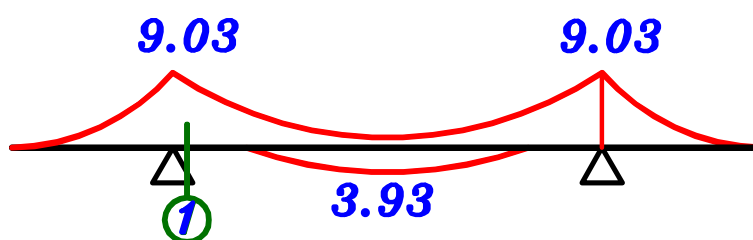
Equation of M_1

$$0.0 + 2M_1(4.47 + 4.0) + M_1(4.0) = -6(6.26 + 8.74)$$

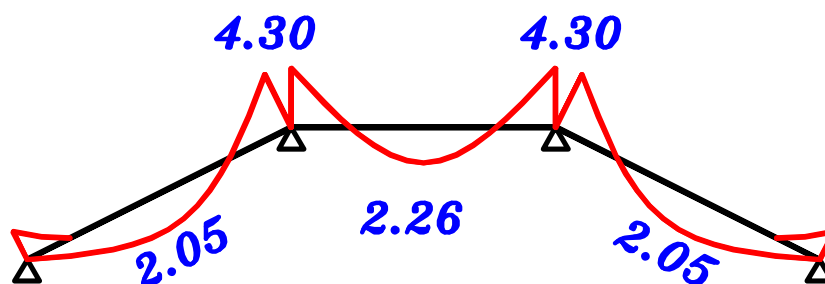
$$M_1 = -4.30 \text{ kN.m.}$$



Strip ①



Strip ②



Sec. ①

$$M_{U.L.} = 9.03 \text{ kN.m/m}$$

$t_s = 150 \text{ mm}$, $d = 150 - 20 = 130 \text{ mm}$, $B = 1000 \text{ mm}$ عرض الشريحة

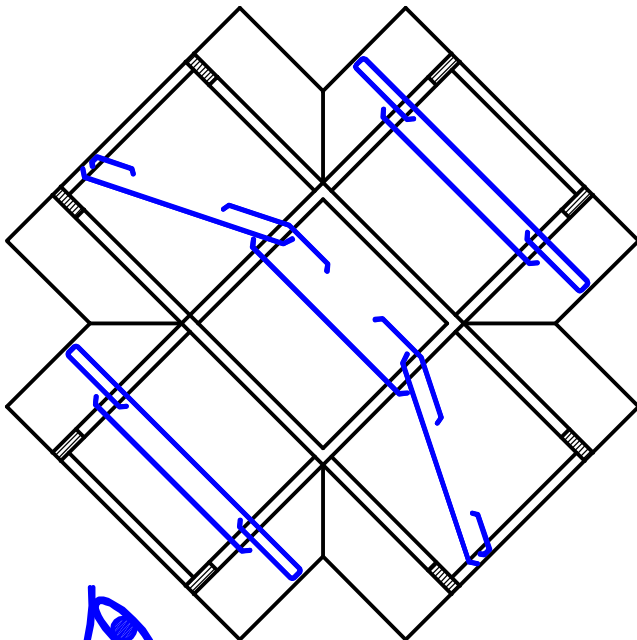
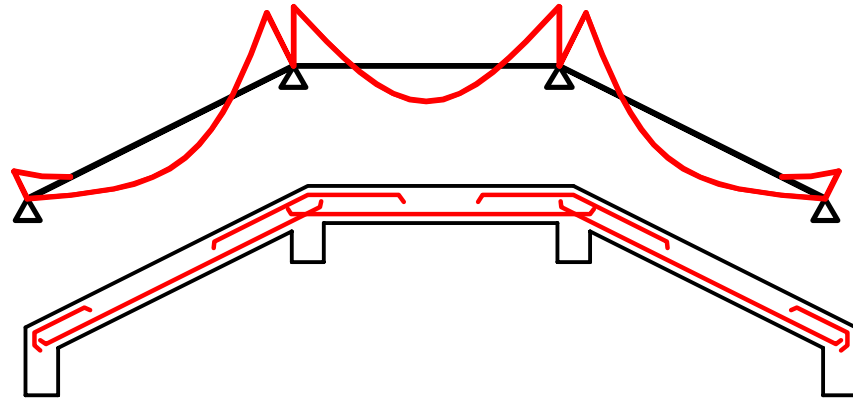
$$130 = C_1 \sqrt{\frac{9.03 \cdot 10^6}{25 \cdot 1000}} \rightarrow C_1 = 6.84 \rightarrow J = 0.826$$

$$A_s = \frac{9.03 \cdot 10^6}{0.826 \cdot 360 \cdot 130} = 233.6 \text{ mm}^2/\text{m}$$

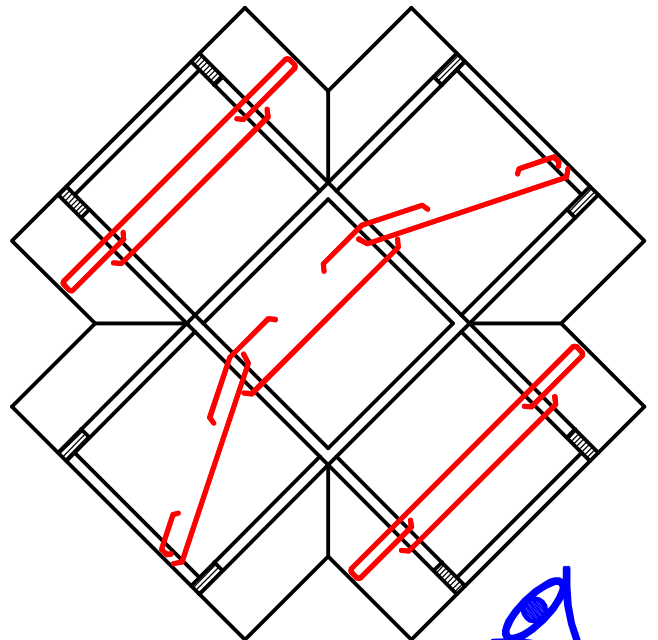
5 $\phi 10$ / m

∴ سيؤخذ تسليح باقى القطاعات 5 $\phi 10$ / m

Details of RFT. For the Slab.

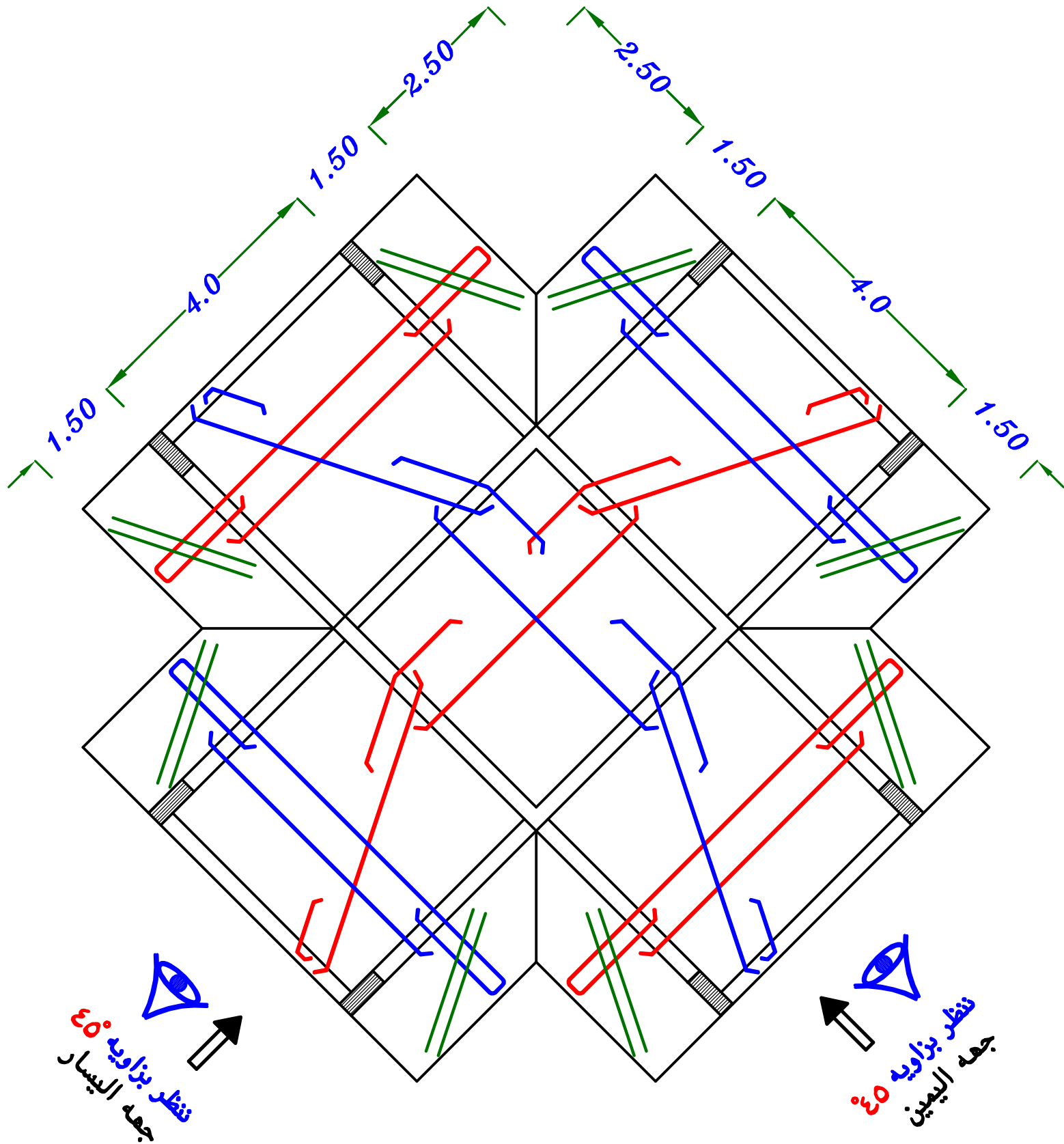


نظير بزايه ٤٥°
جبه اليسار



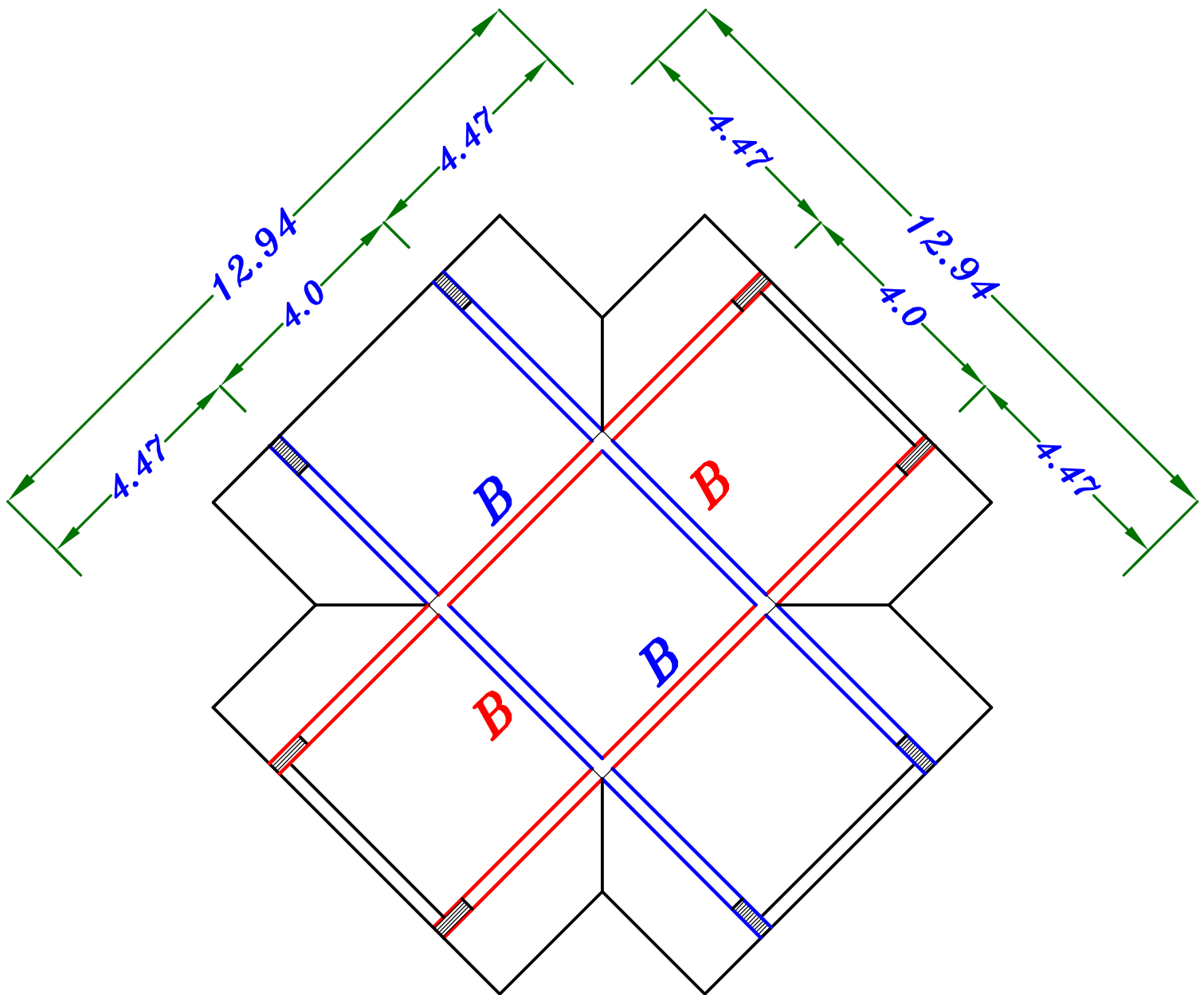
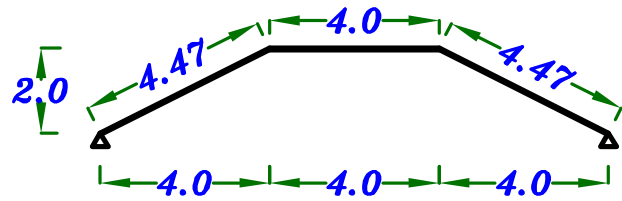
نظير بزايه ٤٥°
جبه اليمين

Details of RFT. For the Slab.



② Design of Panelled Beams.

$$L' = 4.47 + 4.0 + 4.47 = 12.94 \text{ m}$$



a – Get the Dimensions of the beam. (b, t)

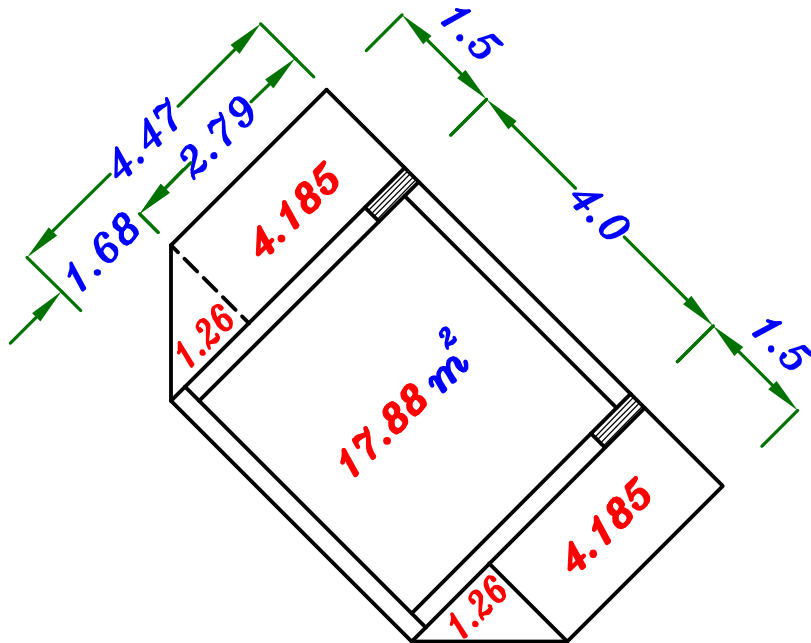
Take $b = 0.25 \text{ m}$

$$t = \frac{L_s}{16} = \frac{12940}{16} = 0.808 \text{ m}$$

$$b = 0.25 \text{ m}$$

$$t = 0.85 \text{ m}$$

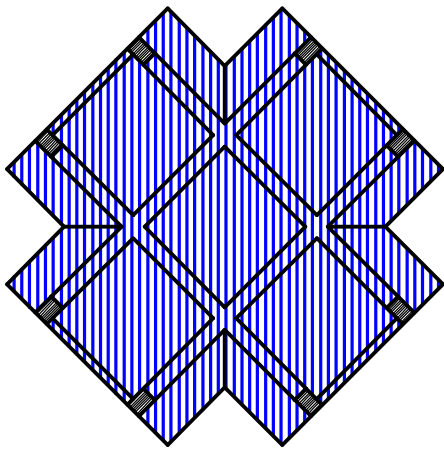
b – Get the Loads on the Slab. (W_{av})



Inclined area

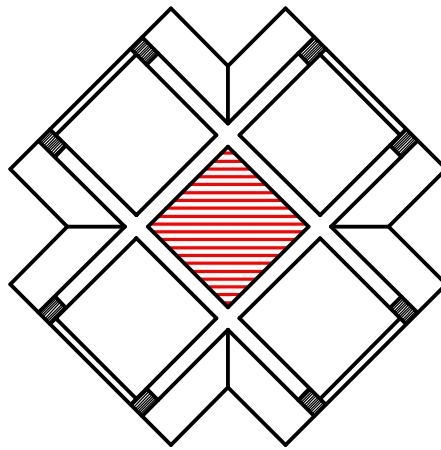
$$= 4 [2 * 1.26 + 2 * 4.185 + 17.88]$$

$$= 115.08 \text{ m}^2$$



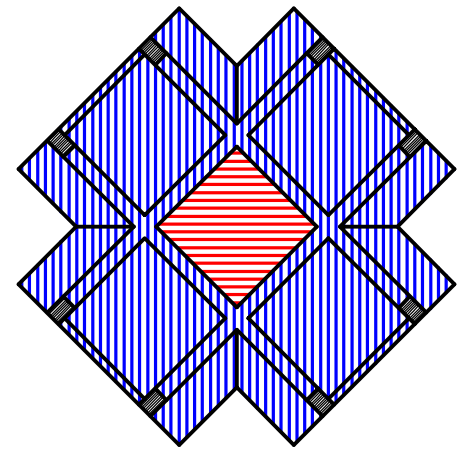
Inclined area

$$= 115.08 \text{ m}^2$$



Horizontal area

$$= 16.0 \text{ m}^2$$



Total area

$$= 131.08 \text{ m}^2$$

$$W_{av.} = \frac{\sum \text{Weight}}{\text{Area}}$$

$$W_{av.} = \frac{w_{sh} * \text{HL. area} + w_{si} * \text{Inclined area} + \text{Panelled Beams}}{\text{Total area}}$$

$$W_{av.} = \frac{9.37 * 16.0 + 8.98 * 115.08 + 1.4 (0.25 (0.85 - 0.15) [4 * 12.94] * 25)}{131.08}$$

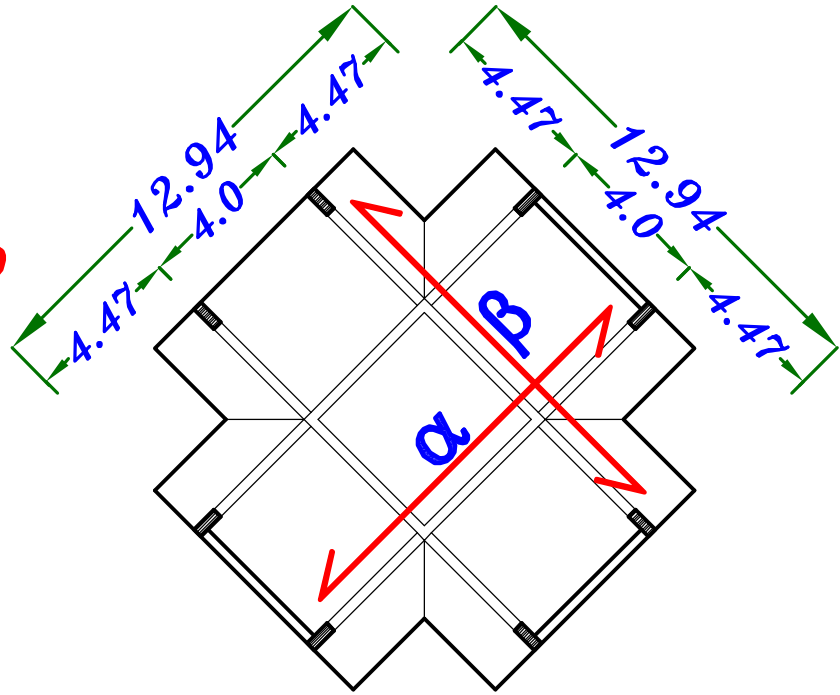
$$W_{av.} = 11.44 \text{ kN/m}^2$$

C – Calculate α , β By using Grashoff.

$$r = \frac{m L}{m_s L_s} = \frac{(1.0) 12.94}{(1.0) 12.94} = 1.0$$

$$\alpha = \frac{r^4}{1+r^4} = \frac{(1.0)^4}{1+(1.0)^4} = 0.50$$

$$\beta = \frac{1}{1+r^4} = \frac{1}{1+(1.0)^4} = 0.50$$

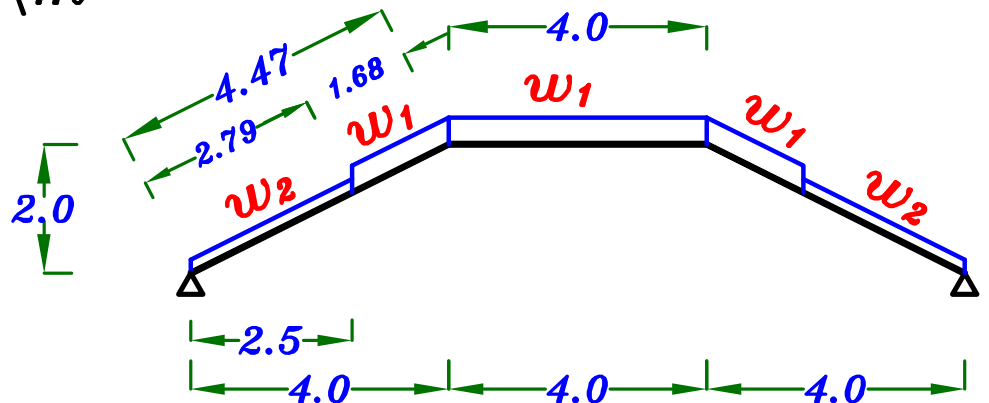
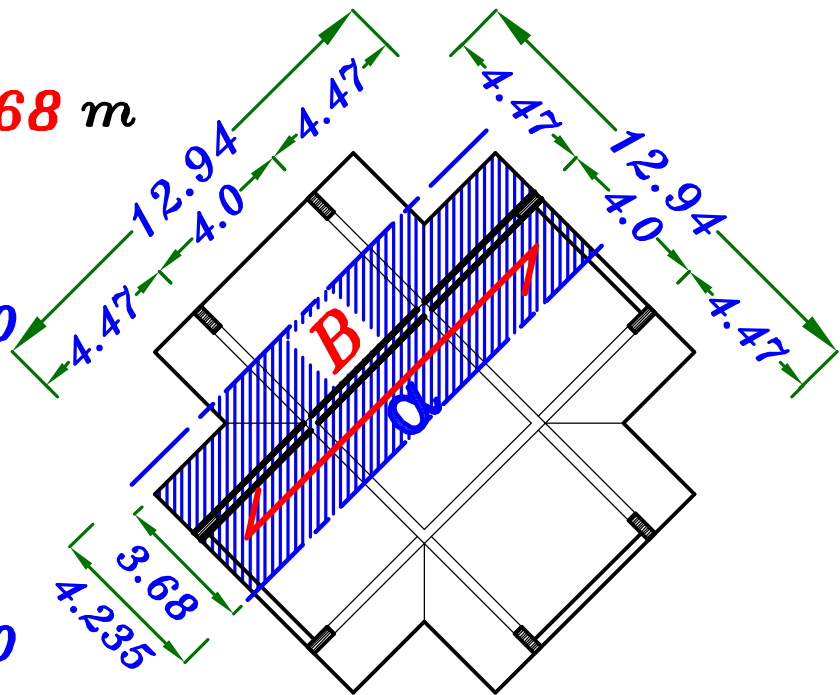


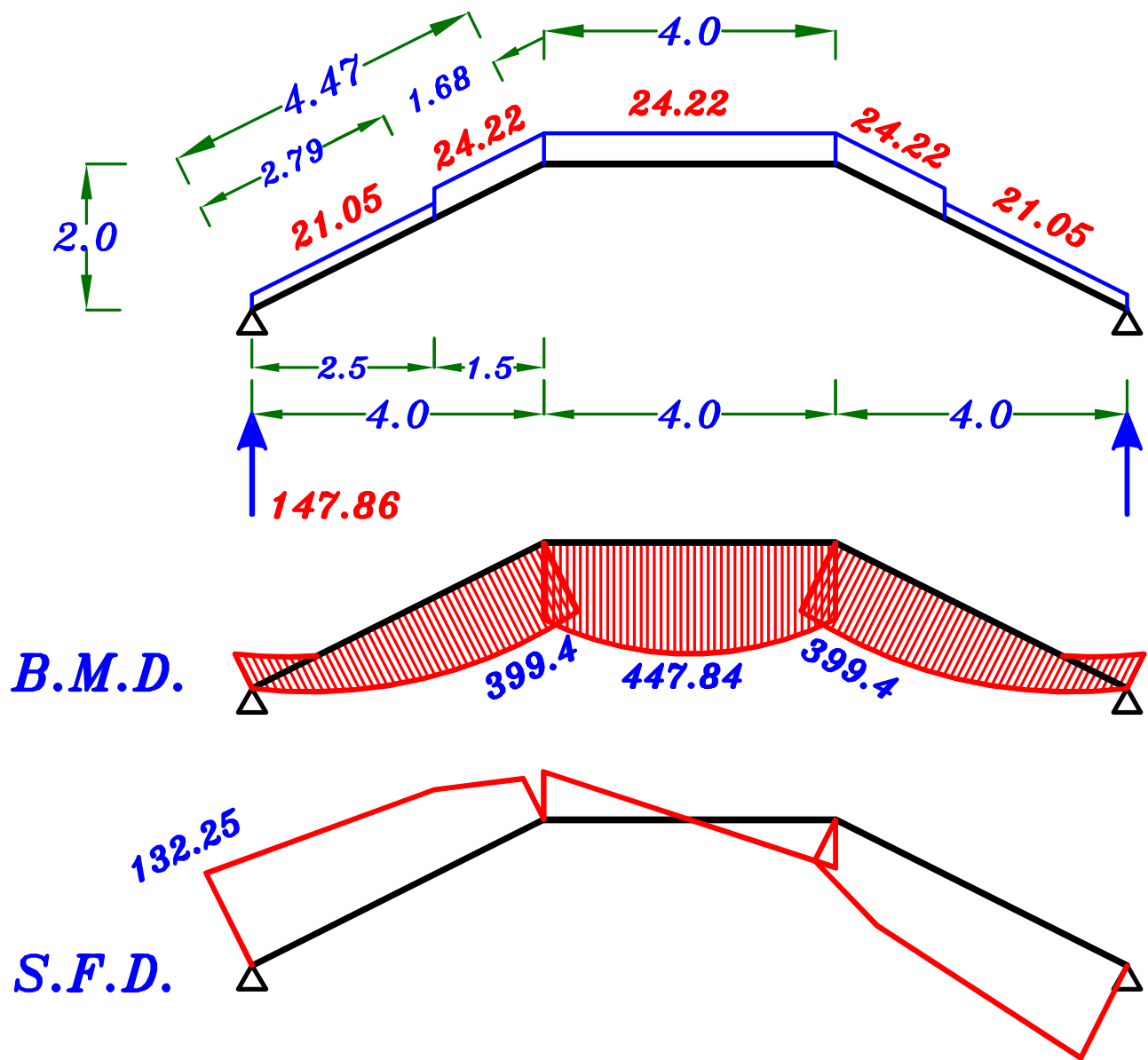
B

$$\alpha_1 = 4.235 \text{ m} , \alpha_2 = 3.68 \text{ m}$$

$$\begin{aligned} w_1 &= w_{av} * \alpha_1 * \alpha \\ &= 11.44 * 4.235 * 0.50 \\ &= 24.22 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} w_2 &= w_{av} * \alpha_2 * \alpha \\ &= 11.44 * 3.68 * 0.50 \\ &= 21.05 \text{ kN/m} \end{aligned}$$





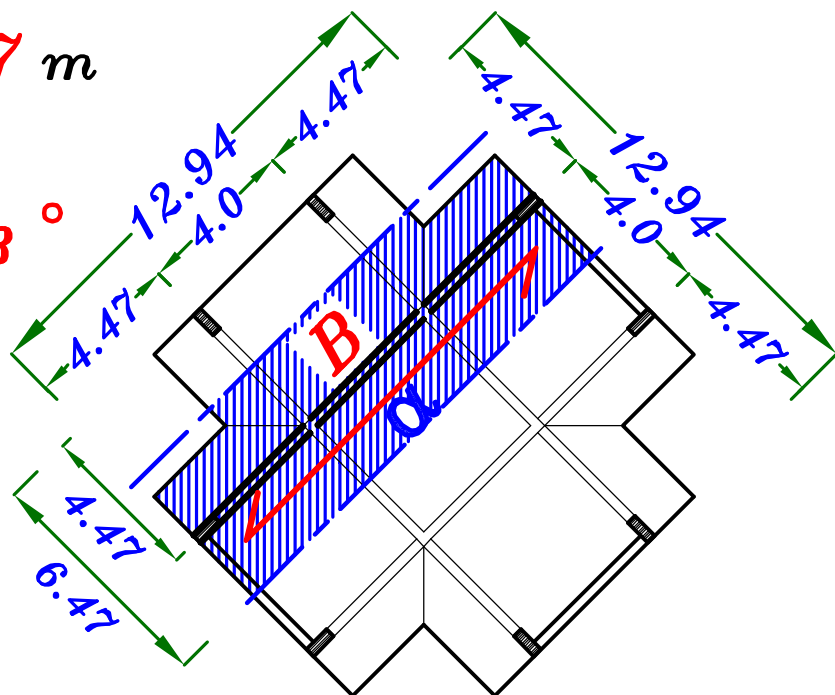
e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90} \right)$

$$X = 4.47 \text{ m} , \quad \frac{L}{2} = 6.47 \text{ m}$$

$$\theta_{B_1} = \frac{4.47}{6.47} * 90^\circ = 62.18^\circ$$

$$M_1 = 447.84 * \frac{\sin 62.18^\circ}{\sin 90^\circ}$$

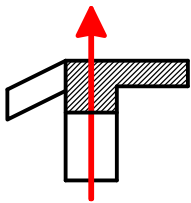
$$= 396.07 \text{ kN.m}$$



F- Design the Panelled Beam. B

Cover = 70 mm Symmetric

$$t = 850 \text{ mm} \quad d = 850 - 70 = 780 \text{ mm}$$

$$B = \left\{ \begin{array}{l} \text{C.L.-C.L.} = 2.0 \text{ m} = 2000 \text{ mm} \\ 6 t_s + b = 6 * 150 + 250 = 1150 \text{ mm} \\ K \frac{L}{10} + b = 1.0 * \frac{12940}{10} + 250 = 1544 \text{ mm} \end{array} \right\} \quad \boxed{B = 1150 \text{ mm}}$$


$$780 = C_1 \sqrt{\frac{396.07 * 10^6}{25 * 1150}} \rightarrow C_1 = 6.64 \rightarrow J = 0.826$$

$$A_s = \frac{396.07 * 10^6}{0.826 * 360 * 780} = 1707.6 \text{ mm}^2$$

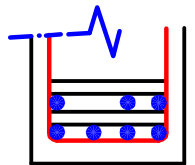
Check $A_{s \min}$. $A_{s \text{ req.}} = 1707.6 \text{ mm}^2$

$$\mu_{\min} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 250 * 780 = 609.3 \text{ mm}^2$$

$\therefore A_{s \text{ req.}} > \mu_{\min} b d \therefore \text{Take } A_s = A_{s \text{ req.}} = 1707.6 \text{ mm}^2$ **7 ϕ 18**

Stirrup Hangers = (0.1 \rightarrow 0.2) A_s = (170 \rightarrow 340 mm²)

4 ϕ 10

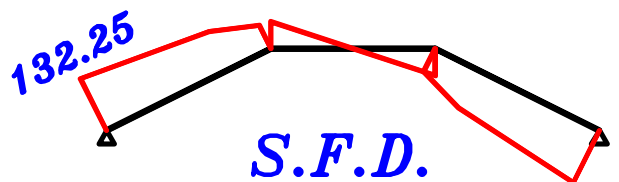


Check Shear.

$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

$$q_{u \text{ max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

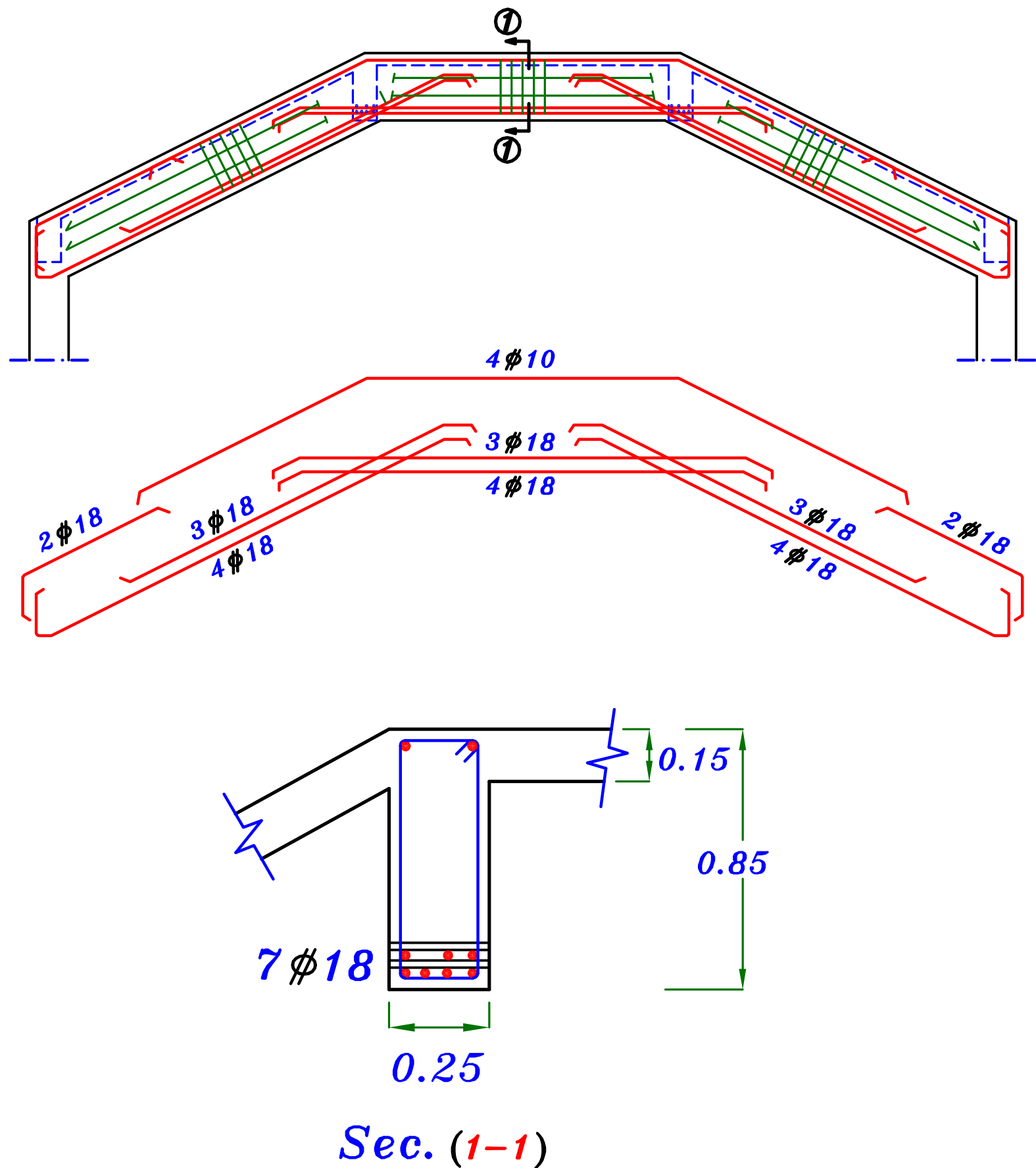
$$q_s = \frac{Q_{\text{max}}}{b d} = \frac{132.25 * 10^3}{250 * 780} = 0.67 \text{ N/mm}^2 \therefore q_s < q_{cu}$$



\therefore Use min. Shear RFT.

5 ϕ 8

g - Draw Details of RFT. For the Beam.



Note.

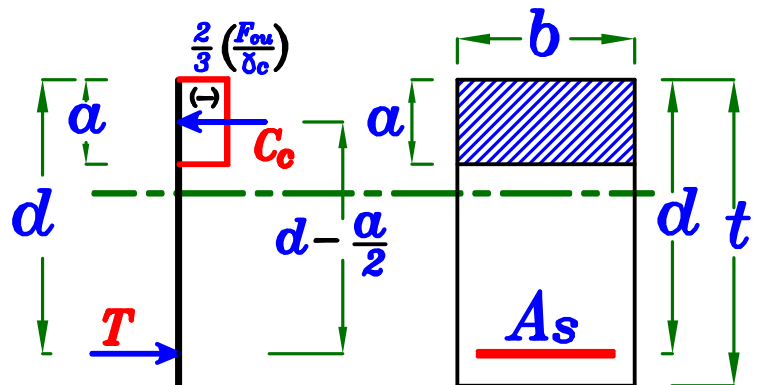
إذا احتجنا حساب ال **moment** المصمم عليه القطاع و يسمى $M_{U.L.}$

Calculation of $M_{U.L.}$

For R - Sec.

$$C_c = \frac{2}{3} \frac{F_{cu}}{\delta_c} a b$$

$$T = \frac{F_y}{\delta_s} * A_s$$



From $\frac{2}{3} \frac{F_{cu}}{\delta_c} * a * b = \frac{F_y}{\delta_s} * A_s \rightarrow a$ get

IF a

IF $a \leq 0.1 d$

take $a = 0.1 d$

$$\therefore M_{U.L.} = A_s \frac{F_y}{\delta_s} (d - \frac{a}{2})$$

$$\therefore M_{U.L.} = A_s \frac{F_y}{\delta_s} (d - \frac{0.1 d}{2})$$

$$\therefore M_{U.L.} = A_s F_y d \frac{1}{1.15} (1 - \frac{0.1}{2})$$

$$\therefore M_{U.L.} = 0.826 A_s F_y d$$

IF $a > 0.1 d$

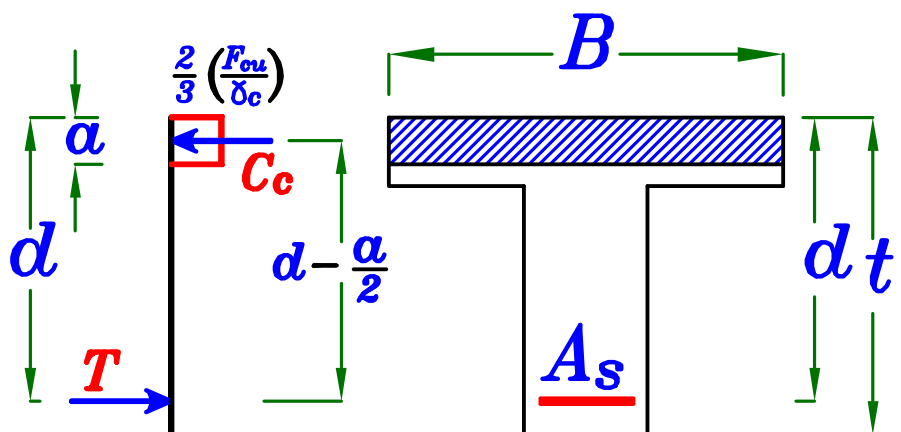
$$M_{U.L.} = \frac{2}{3} \frac{F_{cu}}{\delta_c} a b (d - \frac{a}{2})$$
$$= A_s * \frac{F_y}{\delta_s} (d - \frac{a}{2})$$

For T - Sec.

the same as R-sec.
but with B

$$C_c = \frac{2}{3} \frac{F_{cu}}{\delta_c} a B$$

$$T = \frac{F_y}{\delta_s} * A_s$$





$$F_{cu} = 25 \text{ N/mm}^2$$

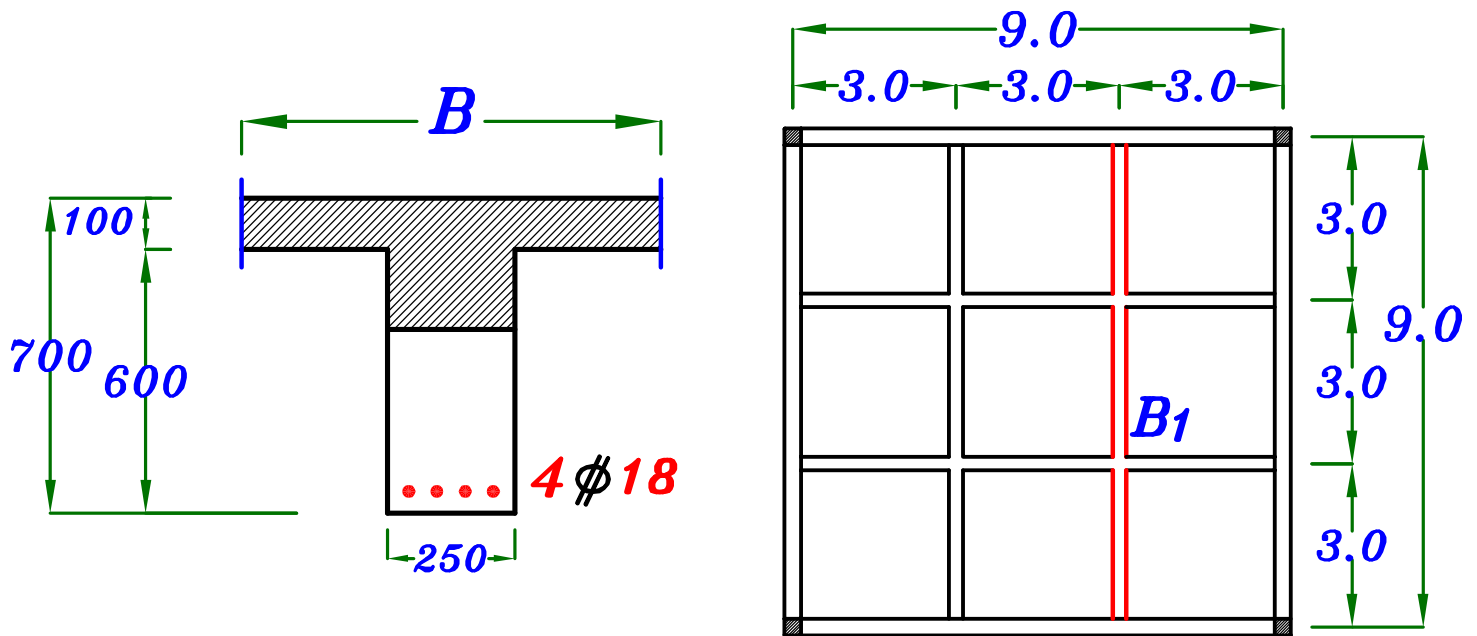
$$F_y = 360 \text{ N/mm}^2$$

$$F.C. = 1.5 \text{ kN/m}^2$$

$L.L. = ?? \text{ kN}\cdot\text{m}^2$

Req.

Calculate the maximum **Live Load** Could be applied to the roof.



$$A_s = 4 \phi 18 = 1018 \text{ mm}^2$$

$$B = \left\{ \begin{array}{l} \text{C.L.} - \text{C.L.} = 3.0 \text{ m} = 3000 \text{ mm} \\ 16 t_s + b = 16 * 100 + 250 = 1850 \text{ mm} \\ K \frac{L}{5} + b = 1.0 * \frac{9000}{5} + 250 = 2050 \text{ mm} \end{array} \right\} \quad \boxed{B = 1850 \text{ mm}}$$

Calculate $M_{U.L.}$ ----- أكبر *moment* يتحمله هذا القطاع

$$C_c = T$$

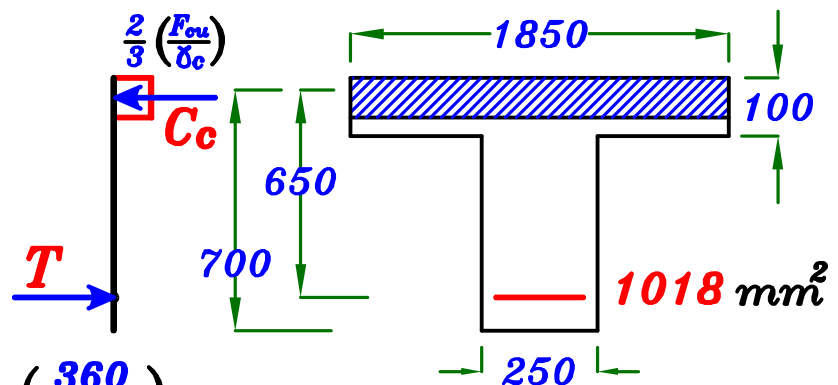
$$\frac{2}{3} \frac{F_{cu}}{\delta_c} \alpha B = \frac{F_y}{\delta_s} * A_s$$

$$\frac{2}{3} \left(\frac{25}{1.5} \right) (\alpha) (1850) = (1018) \left(\frac{360}{1.15} \right)$$

$$\therefore \alpha = 15.5 \text{ mm} < 0.1 d \xrightarrow{\text{Take}} \alpha = 0.1 d = 65 \text{ mm}$$

$$\therefore M_{U.L.} = 0.826 A_s F_y d = 0.826 * 1018 * 360 * 650 = 196763112 \text{ N.mm}$$

$$\therefore \boxed{M_{U.L.} = 196.76 \text{ kN.m.}}$$

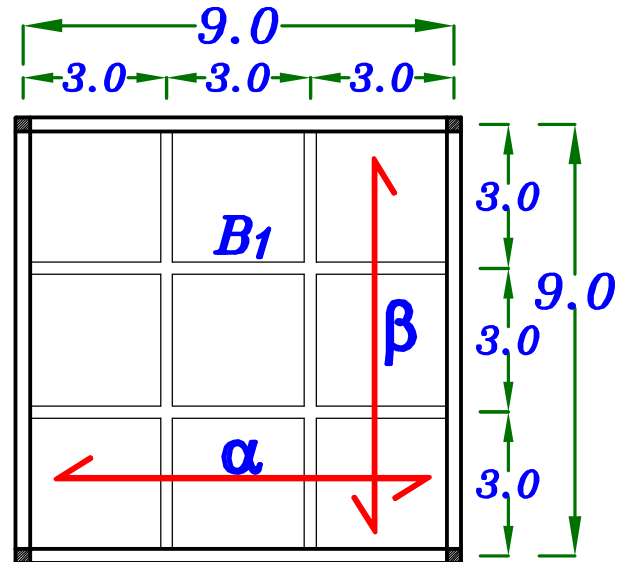


C – Calculate α , β By using Grashoff.

$$r = \frac{m L}{m L_s} = \frac{(1.0) 9.0}{(1.0) 9.0} = 1.0$$

$$\alpha = \frac{r^4}{1+r^4} = \frac{(1.0)^4}{1+(1.0)^4} = 0.50$$

$$\beta = \frac{1}{1+r^4} = \frac{1}{1+(1.0)^4} = 0.5$$



e – Calculate the reduction Factor of the B.M. $\left(\frac{\sin \theta}{\sin 90}\right)$

$$X = 3.0 \text{ m} , \quad \frac{L}{2} = 4.5 \text{ m}$$

$$\theta_{B_1} = \frac{3.0}{4.5} * 90^\circ = 60^\circ$$

$$M_{des.} = \frac{w * L^2}{8} * \frac{\sin \theta^\circ}{\sin 90^\circ} = M_{U.L.}$$

$$\frac{w * 9^2}{8} * \frac{\sin 60^\circ}{\sin 90^\circ} = 196.76 \text{ kN.m.} \rightarrow w = 22.44 \text{ kN/m}$$

$$w = 22.44 = w_{av.} * \alpha * \alpha = w_{av.} * 3.0 * 0.5 \rightarrow w_{av.} = 14.96 \text{ kN/m}$$

$$w_{av.} = w_s + \frac{\text{Total Weight of Panelled Beams}}{L * L}$$

$$w_{av.} = \left[1.4(t_s \delta_c + F.C.) + 1.6(L.L.) \right] + 1.4 \left[\frac{b(t-t_s) [2 * L + 2 * L_s] * \delta_c}{L * L_s} \right]$$

$$14.96 = \left[1.4(0.1 * 25 + 1.5) + 1.6(L.L.) \right] + 1.4 \left[\frac{0.25(0.7 - 0.1) [2 * 9.0 + 2 * 9.0] * 25}{9.0 * 9.0} \right]$$

$$\therefore \boxed{L.L. = 4.39 \text{ kN/m}^2}$$

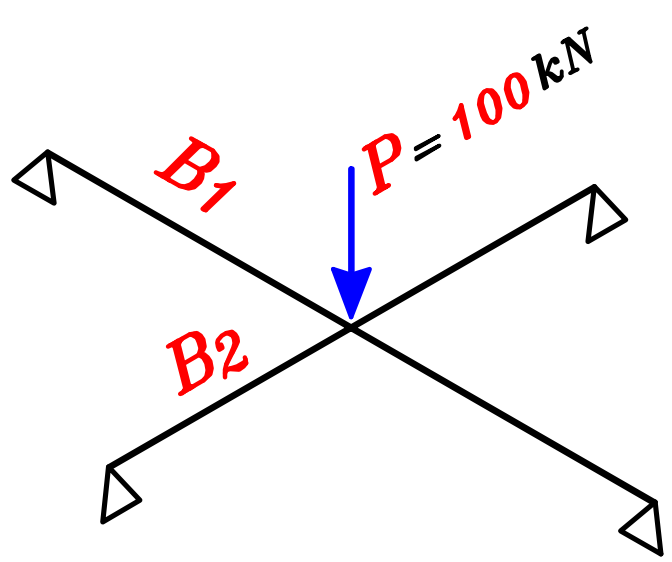
Example.

$$B_1 \text{ (} 250 * 600 \text{)}$$

$$L_1 = 7.0 \text{ m}$$

$$B_2 \text{ (} 300 * 700 \text{)}$$

$$L_2 = 5.50 \text{ m}$$



Deflection of beams B_1 , B_2

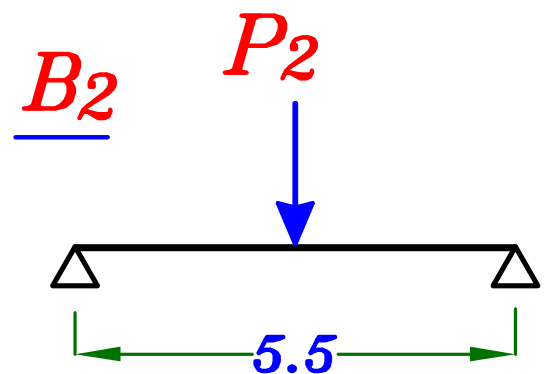
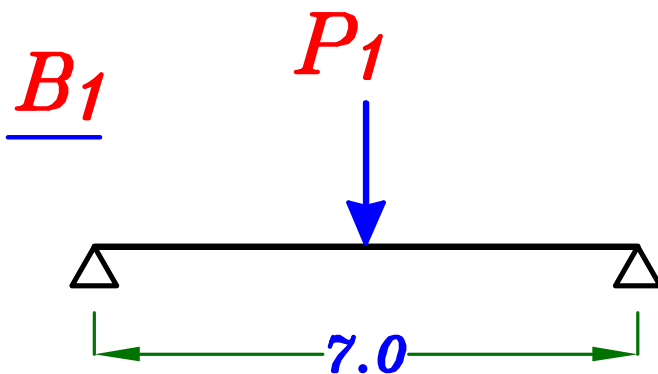
$$\delta = \frac{P L^3}{48 E I}$$

Required.

Find the amount of concentrated load will act on each beam.

Solution.

الحمل P سيتوزع على الكمرتين B_1 & B_2



$$\therefore P_1 + P_2 = P = 100 \text{ kN}$$

$$P_1 = 100 - P_2 \text{ ----- ①}$$

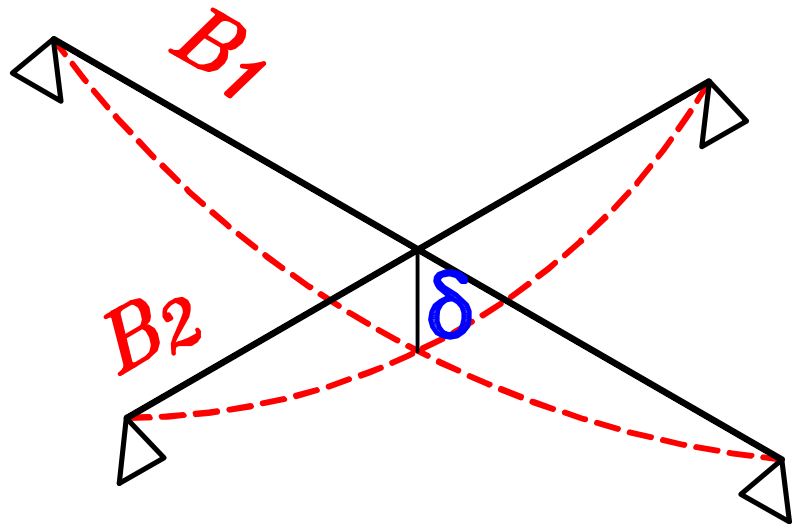
$$B_1 (250 * 600) \longrightarrow I_1 = \frac{0.25 * 0.60^3}{12} = 4.5 * 10^{-3}$$

$$\delta_1 = \frac{P_1 L_1^3}{48 E I_1} = \frac{P_1 (7.0)^3}{48 E (4.5 * 10^{-3})} = 1587.9 \frac{P_1}{E}$$

$$B_2 (300 * 700) \longrightarrow I_2 = \frac{0.30 * 0.70^3}{12} = 8.57 * 10^{-3}$$

$$\delta_2 = \frac{P_2 L_2^3}{48 E I_2} = \frac{P_2 (5.5)^3}{48 E (8.57 * 10^{-3})} = 404.4 \frac{P_2}{E}$$

$$\therefore \delta_1 = \delta_2 = \delta$$



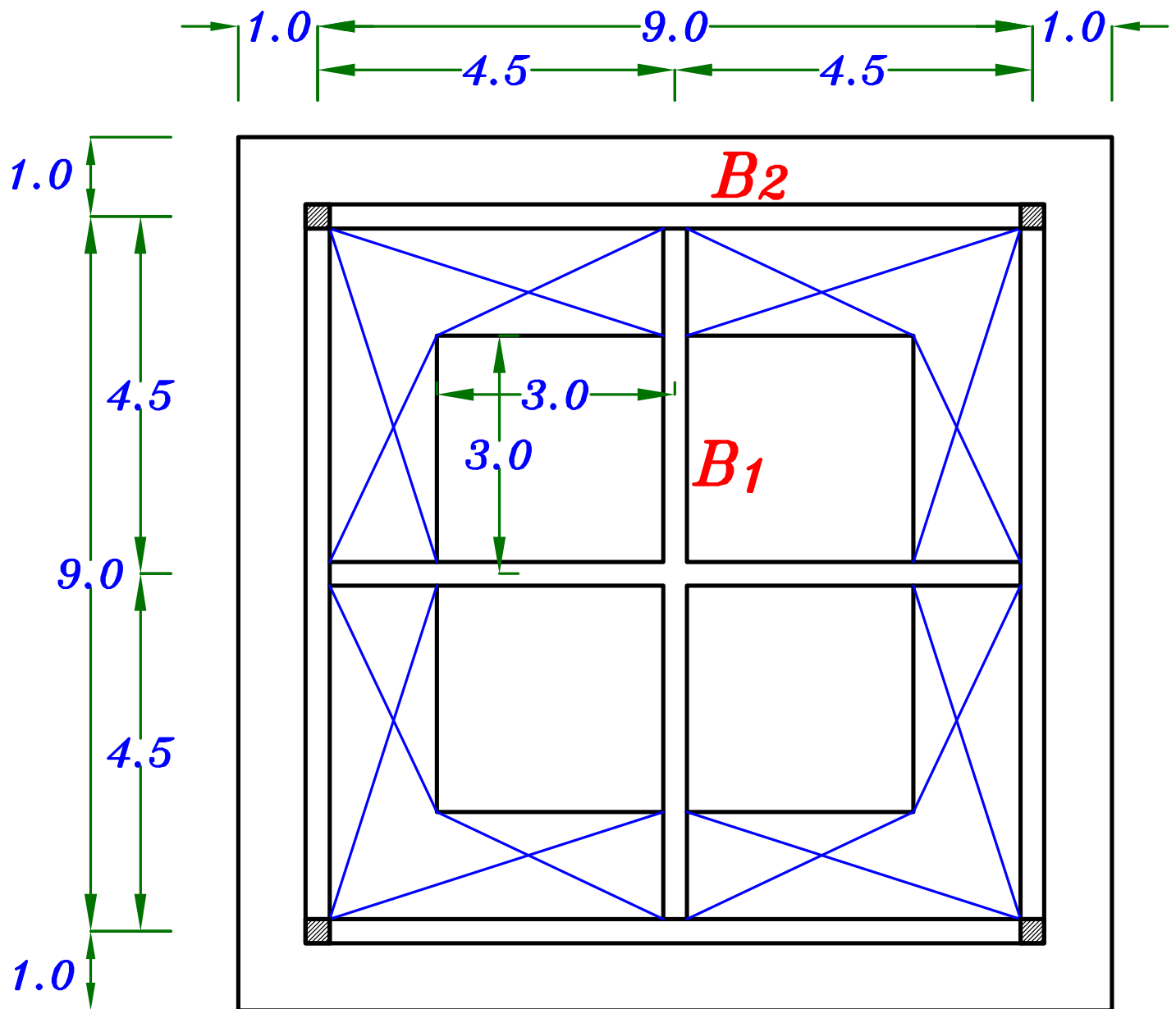
$$\therefore 1587.9 \frac{P_1}{E} = 404.4 \frac{P_2}{E} \text{ ----- } \textcircled{2}$$

From $\textcircled{1}$ & $\textcircled{2}$

$$P_1 = 20.3 \text{ kN}$$

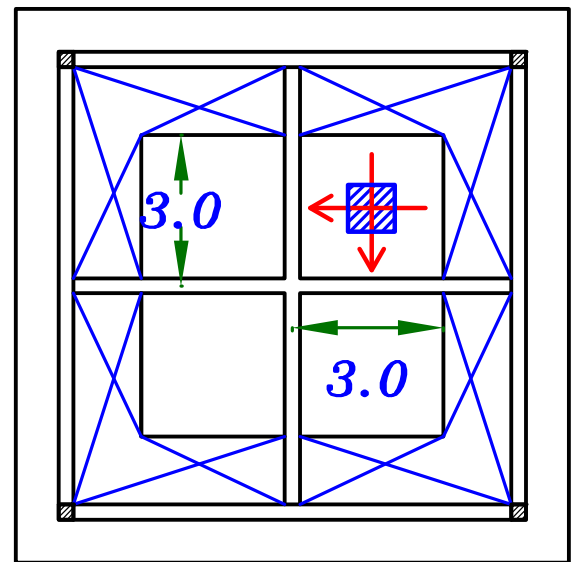
$$P_2 = 79.7 \text{ kN}$$

Example.



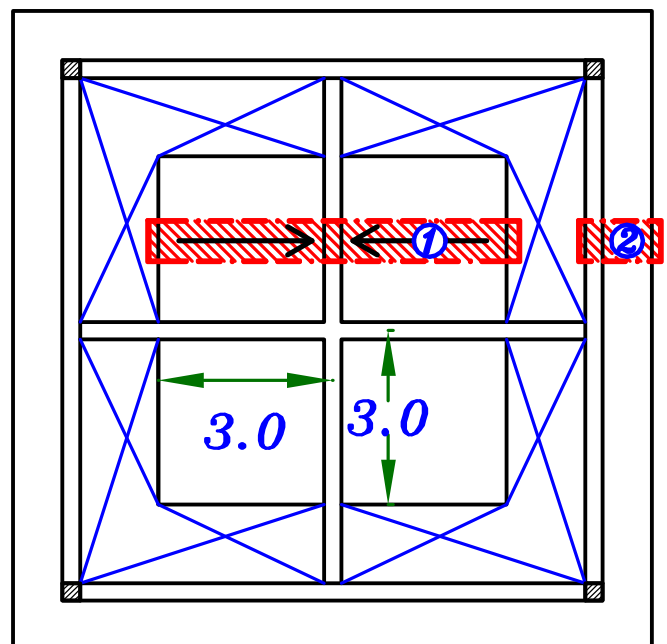
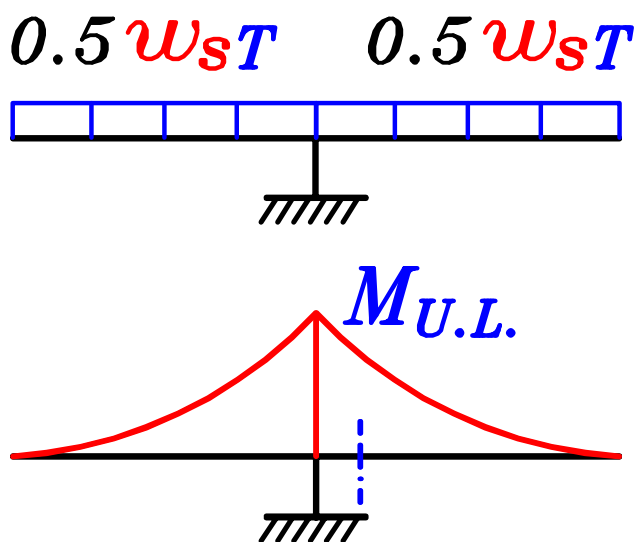
- 1 – Design the slabs & draw details of RFT. in plan.
- 2 – Design Beam B_1 & draw RFT. in elevation.
- 3 – Design Beam B_2 & draw RFT. in elevation.

يتوزع حمل البلاطه على ال **two cantilevers**
 أى يتوزع الحمل فى الاتجاهين كل اتجاه $0.5 w_s$

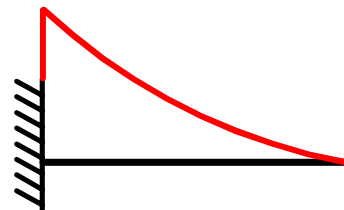
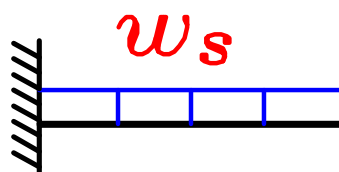


Slabs.

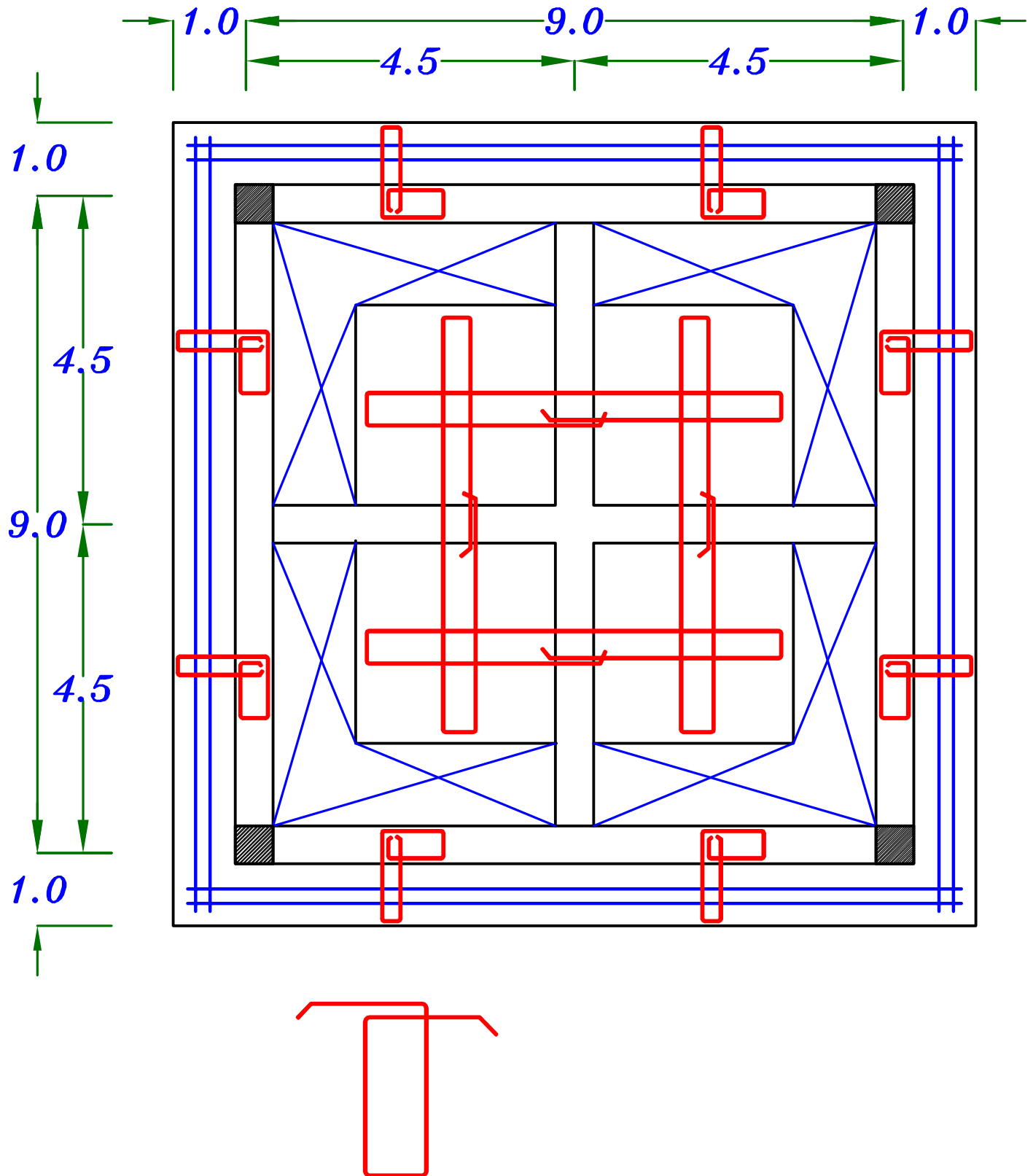
Strip ①



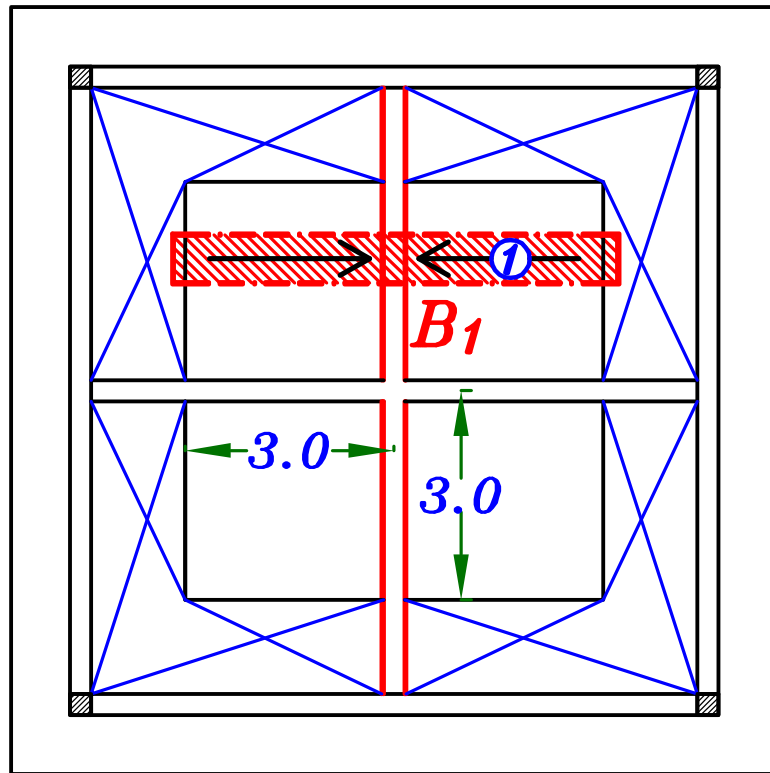
Strip ②



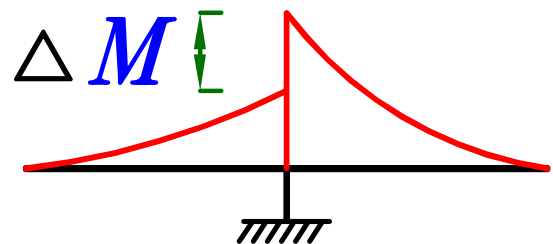
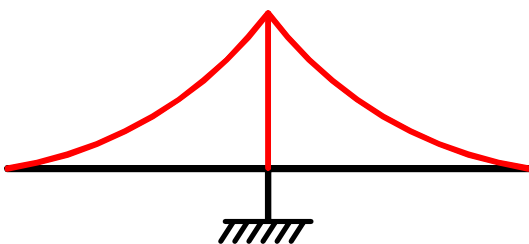
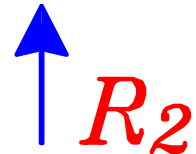
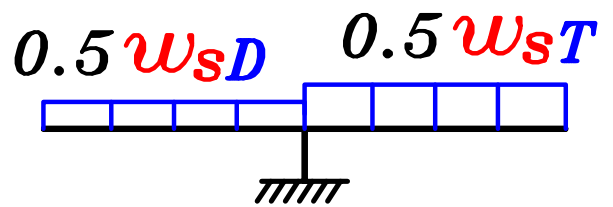
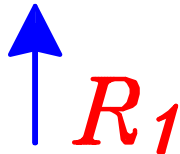
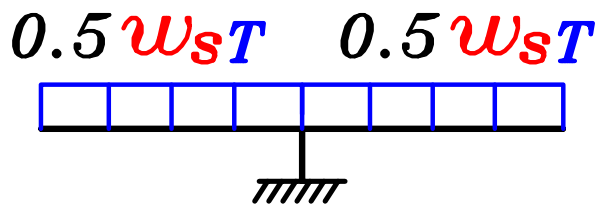
RFT. of Slabs.

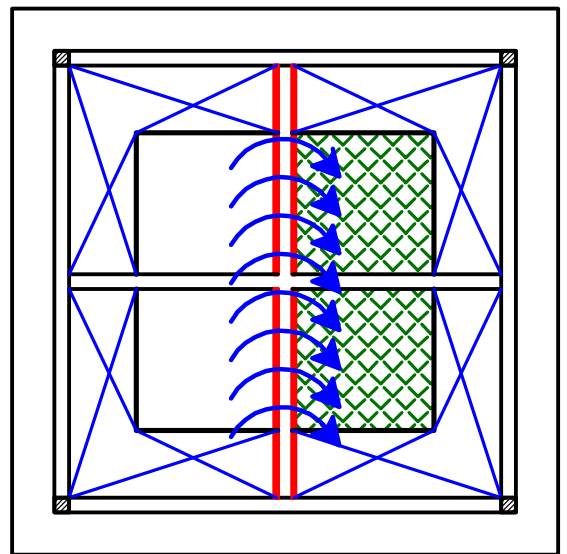
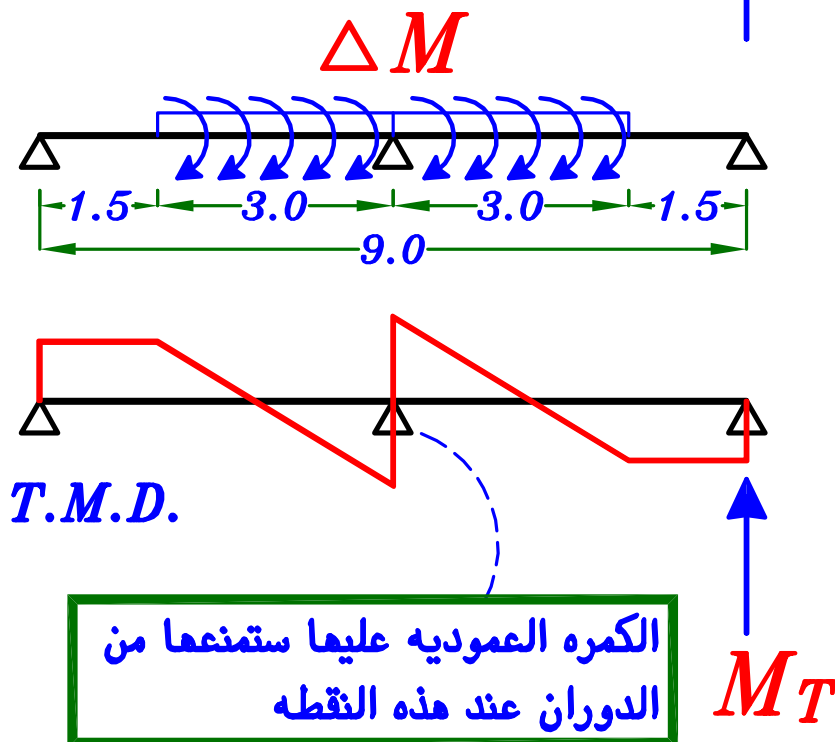
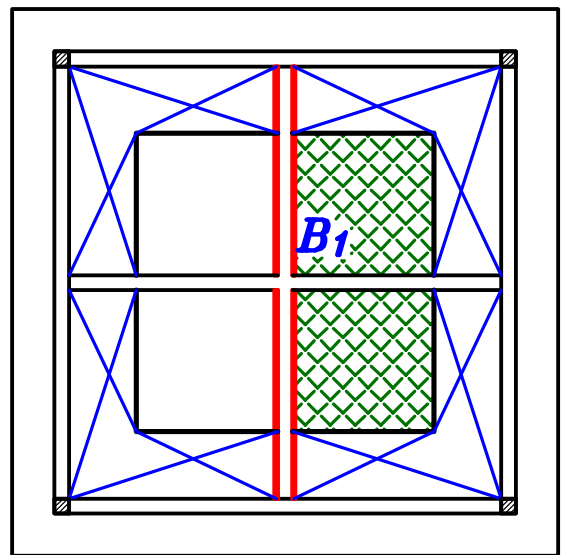
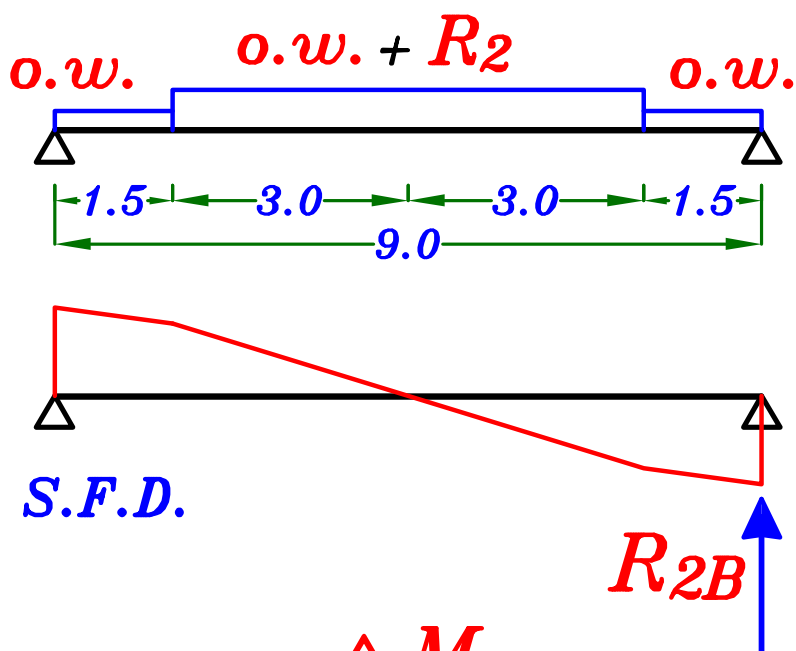
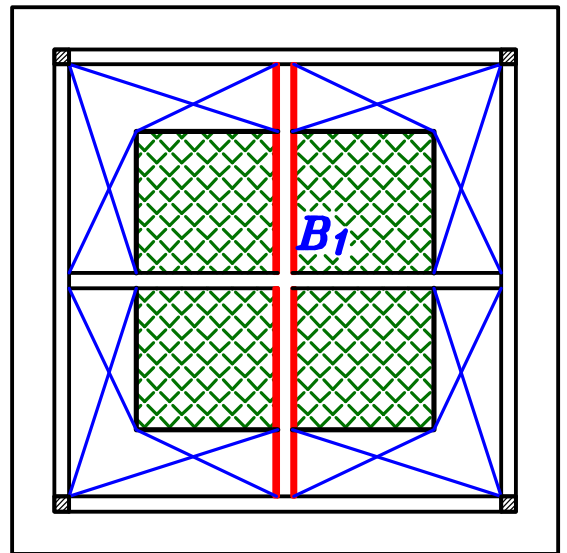
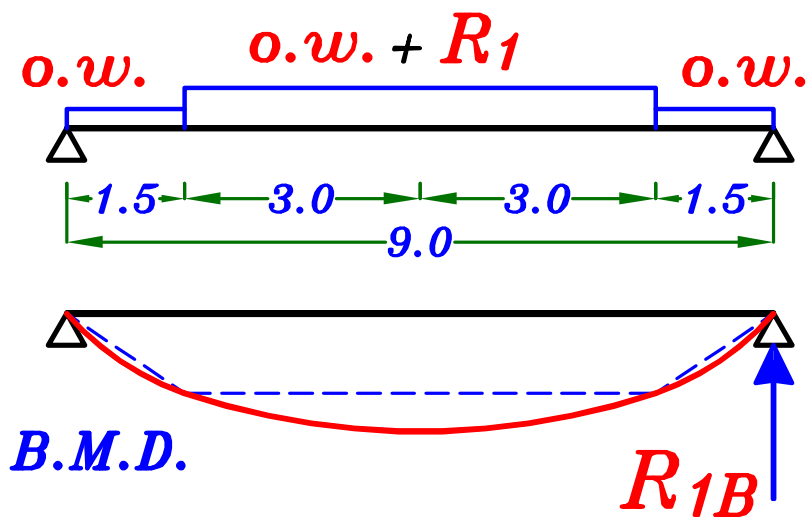


Panelled Beams B_1



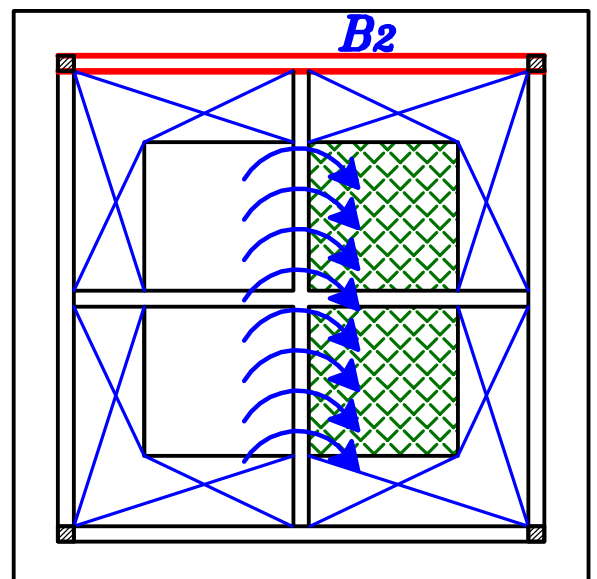
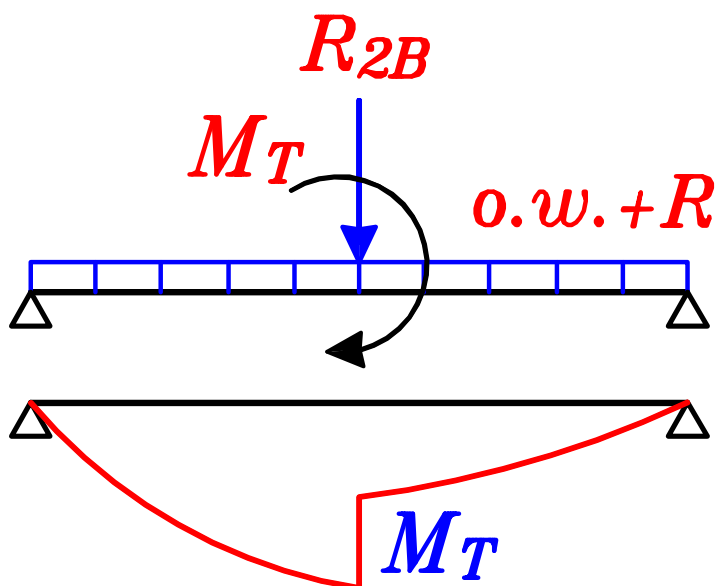
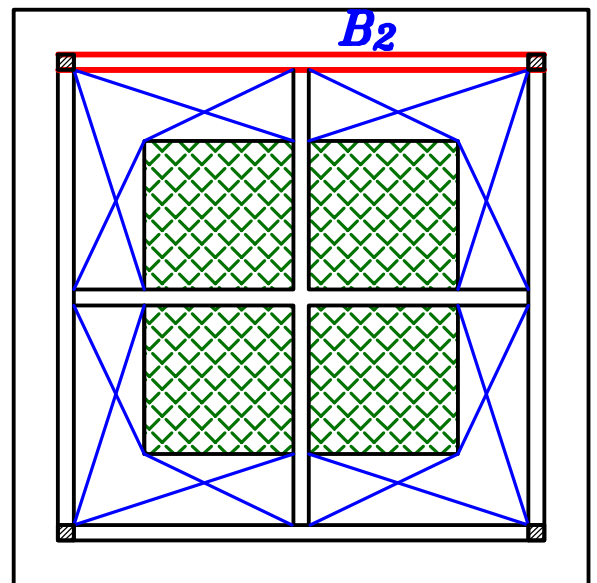
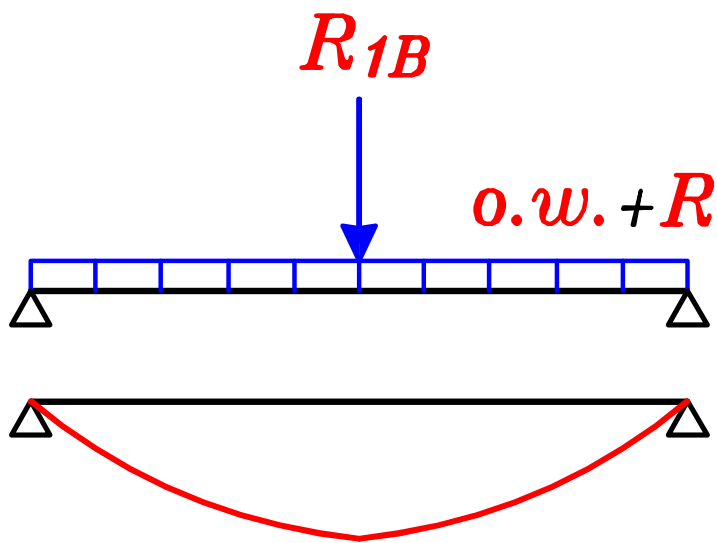
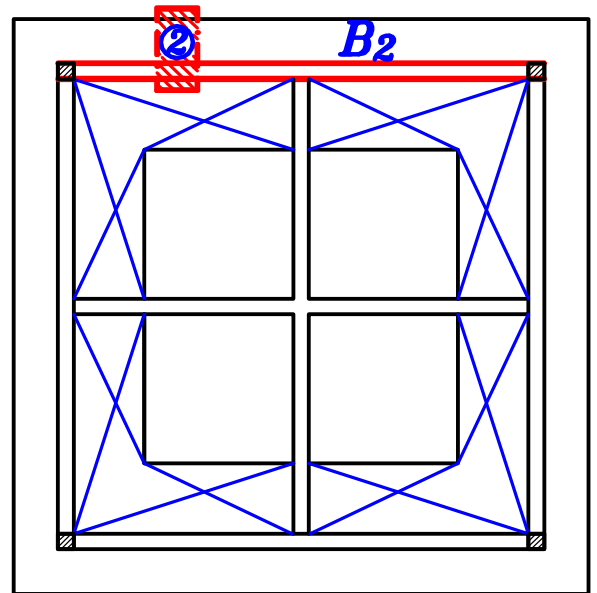
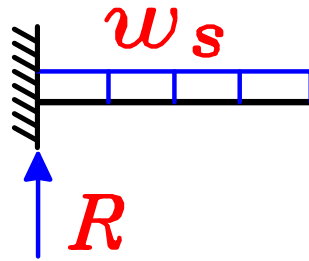
Strip ①



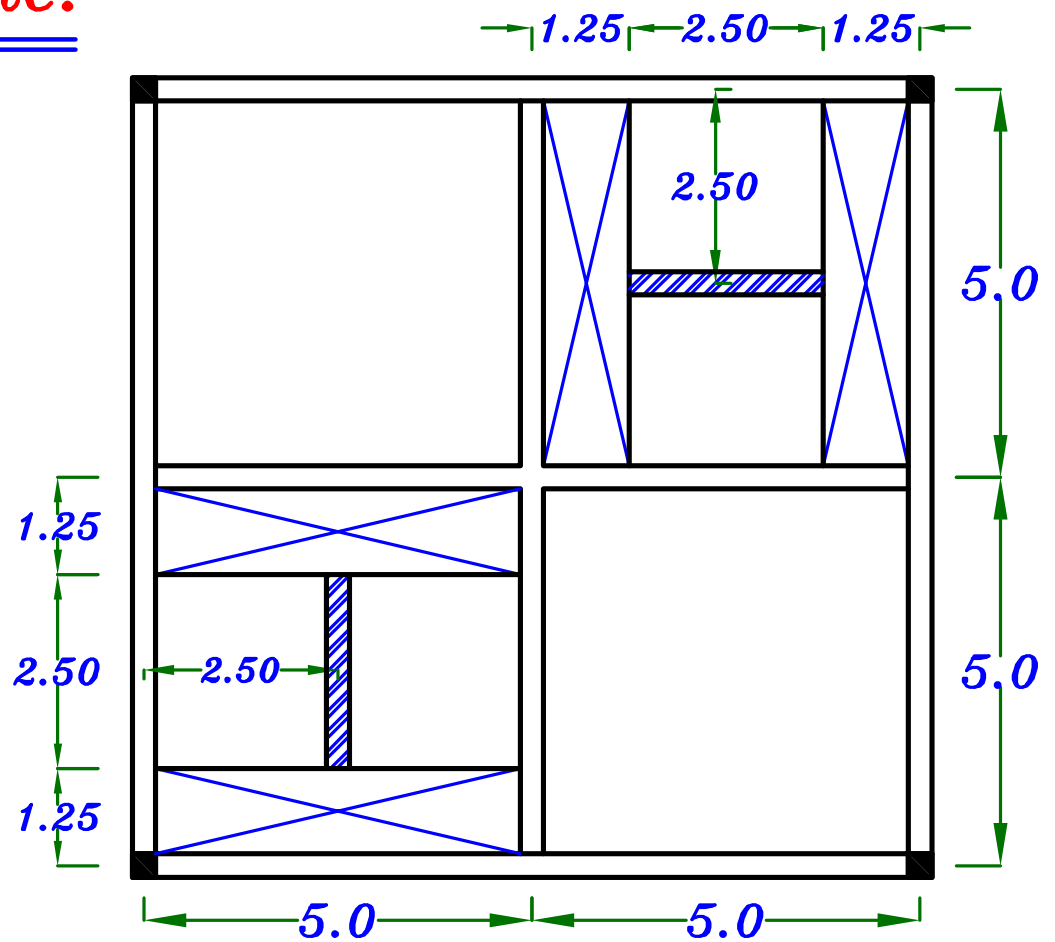


Edge Beam. B_2

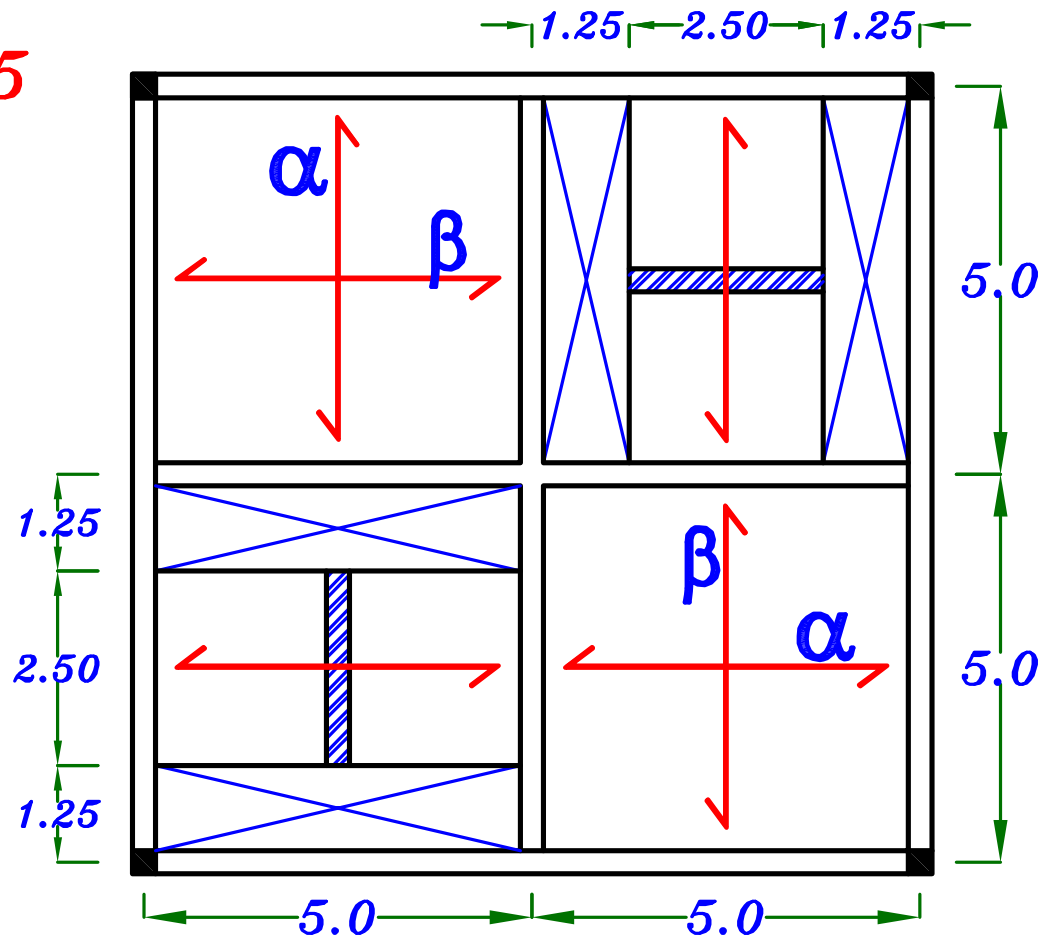
Strip ②



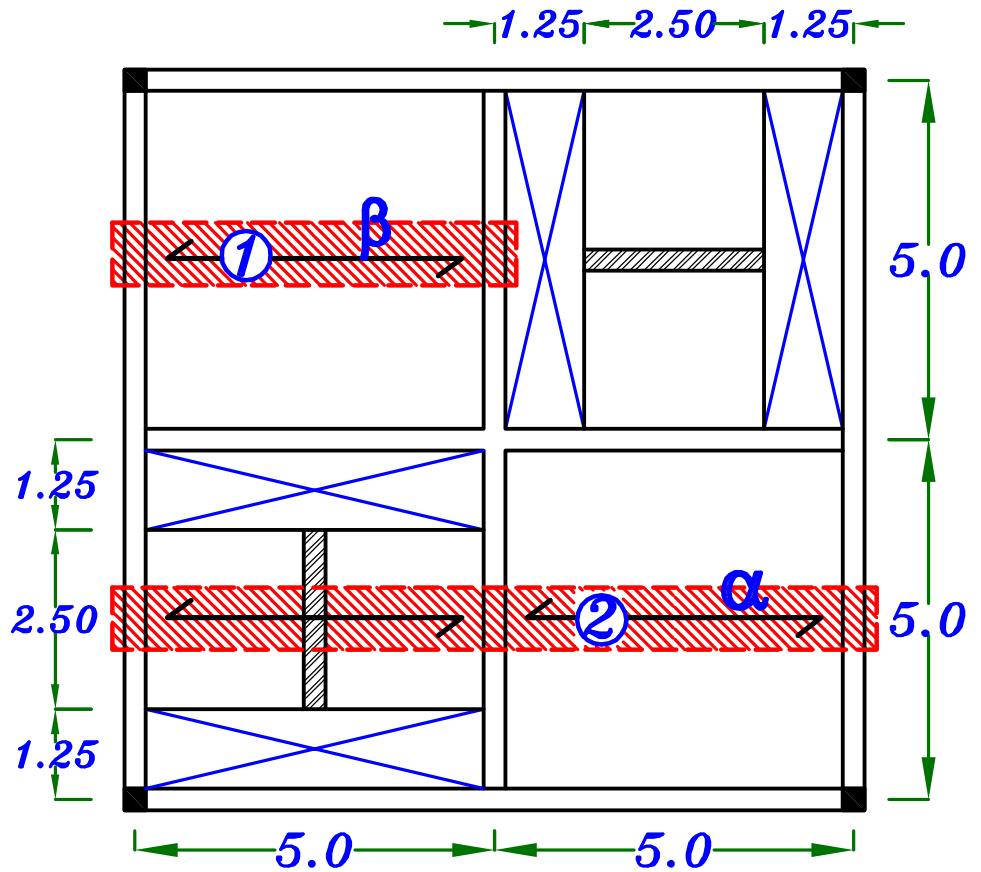
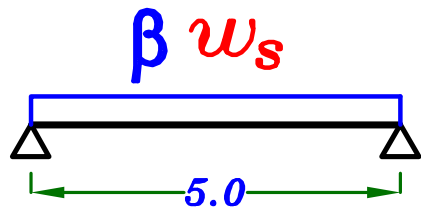
Example.



$$\alpha = \beta = 0.35$$

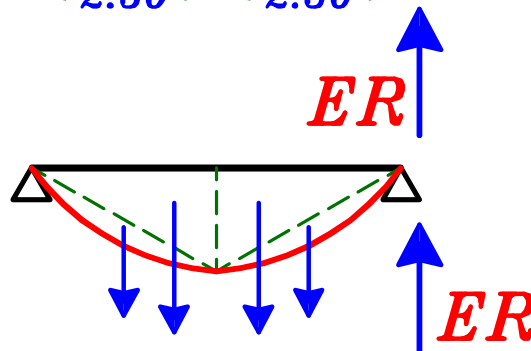
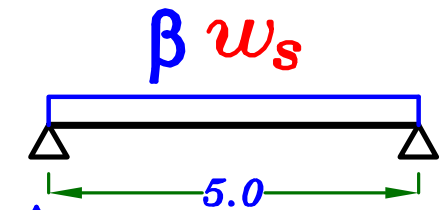
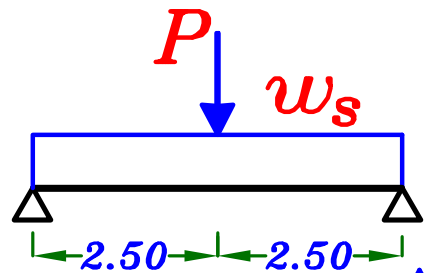
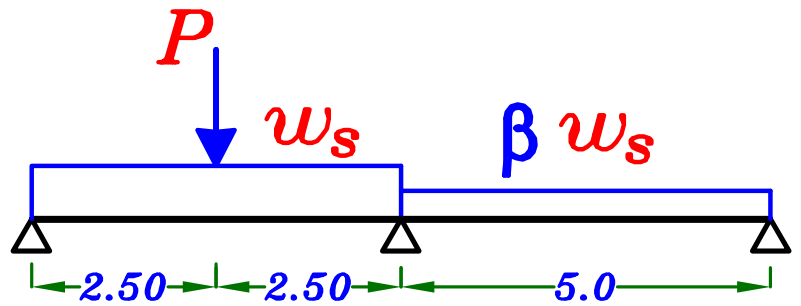


Strip ①

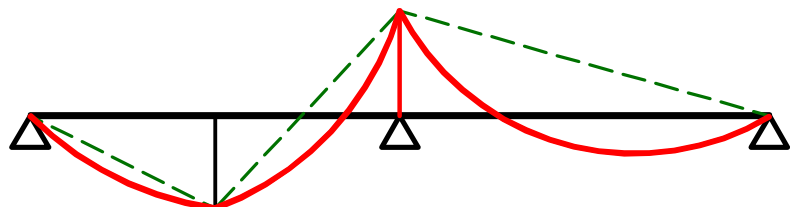


Strip ②

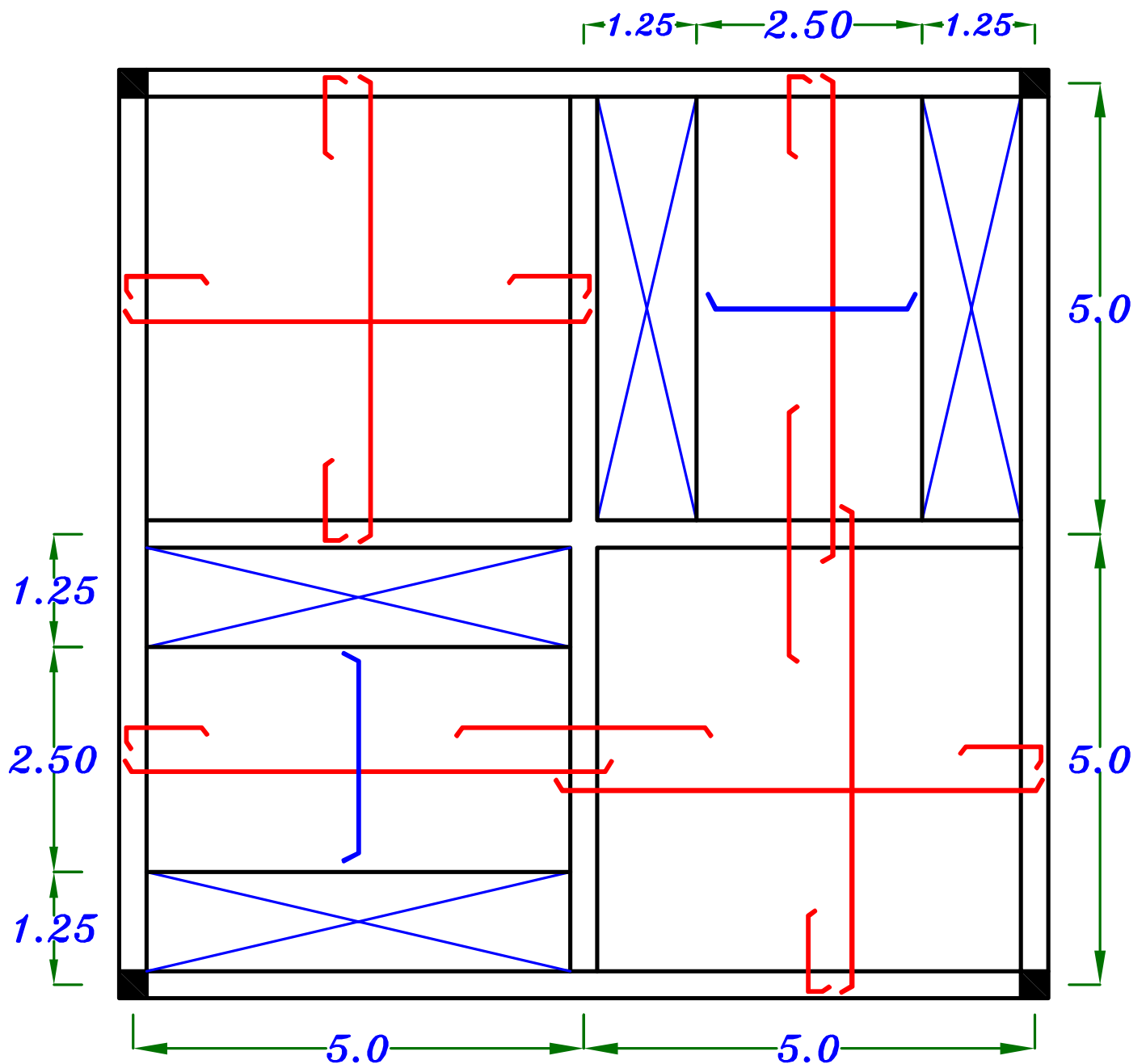
$$P = b H \delta_w * 1.4$$



$$\frac{w L^3}{24}$$

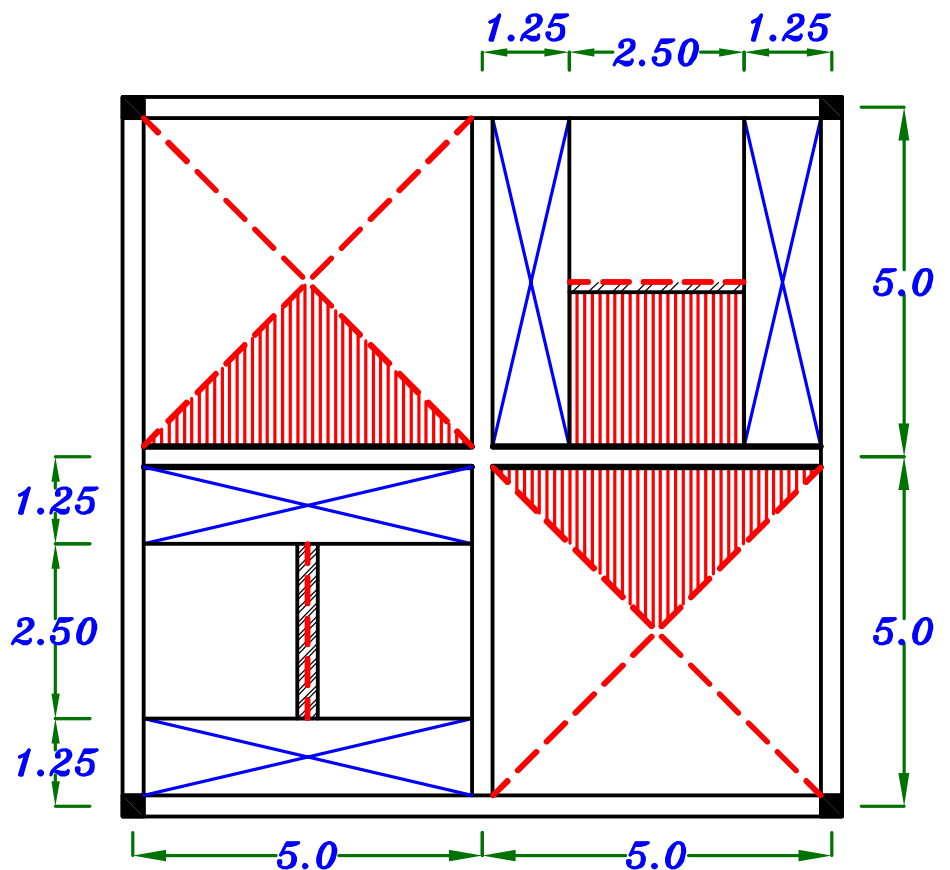
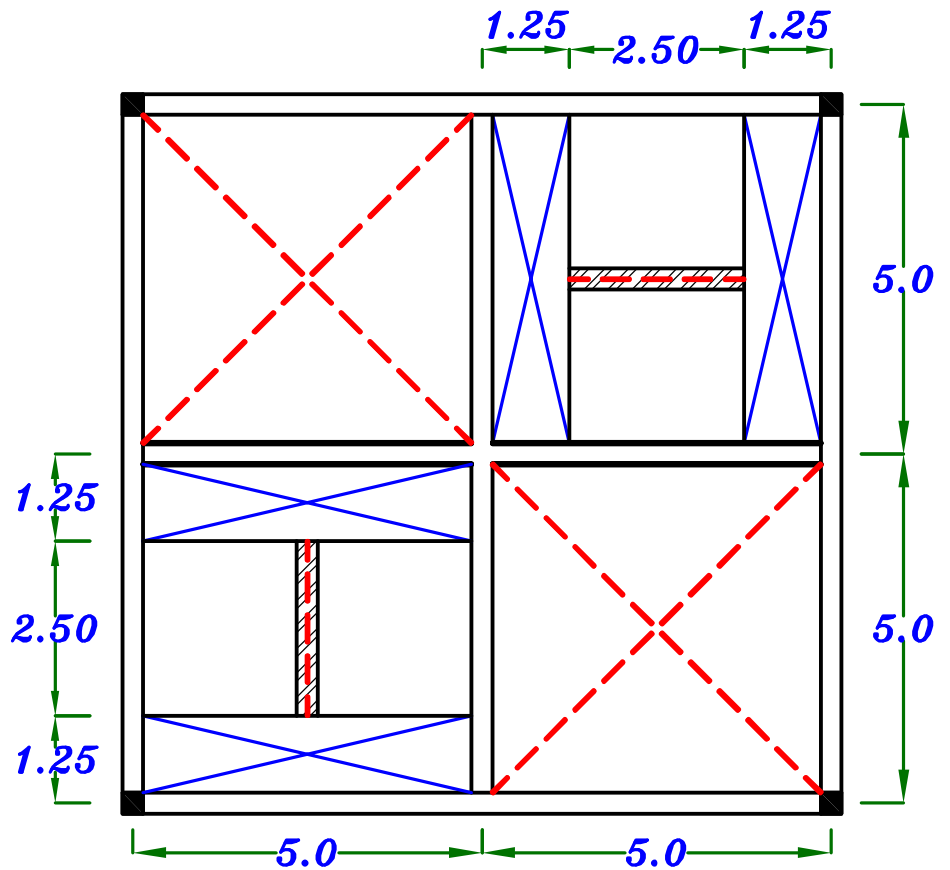


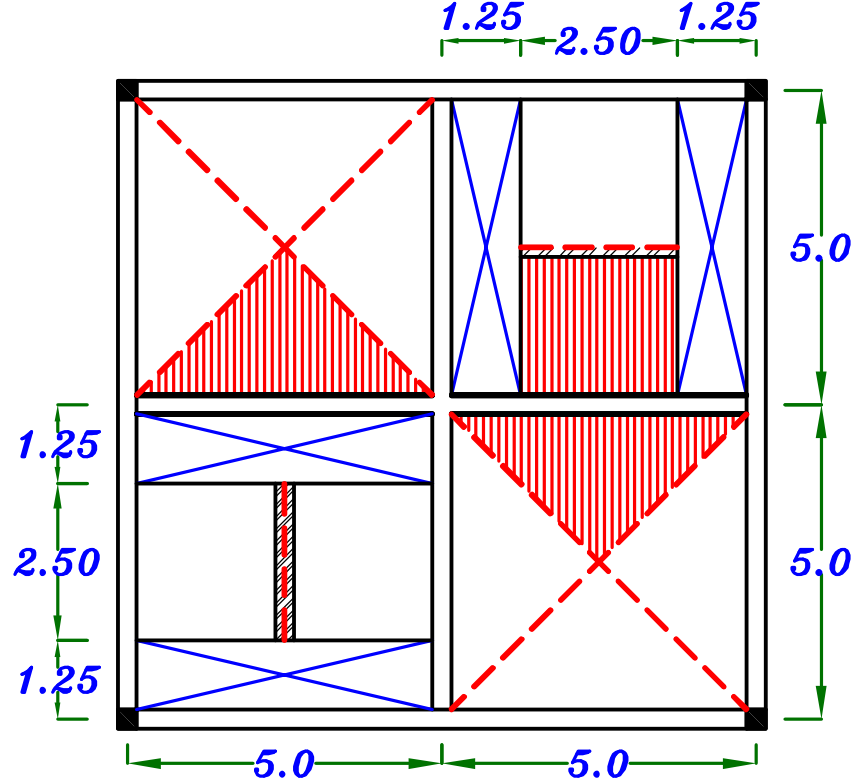
RFT. of the slab.



Panelled Beam.

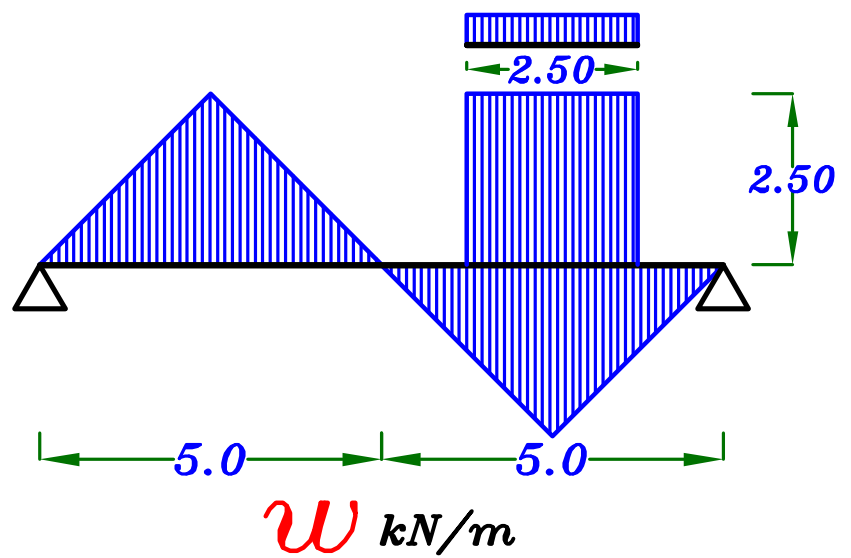
لان الكمرتين فى المنتصف فمن الممكن حساب الاحمال عن طريق **Load Distribution**





$$wall = (bH\delta_w * 1.4) * 2.5 * 0.5$$

نصف الحائط فقط



$$W = o.w. + \sum \frac{\text{area}}{\text{span}} * W_s + \sum \frac{\text{weight}}{\text{span}}$$

wall

